

Low Energy Tests of the Standard Model with Spin Degrees of Freedom

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Outline

- Introduction
- Polarized electron scattering and the weak neutral current
- Muon decay
- g-2
- Electric Dipole Moments (advertisement)
- Conclusions

Introduction

- $SU(3) \times SU(2) \times U(1)$ SM is well tested (0.1% level).
- **New Physics:** small deviation and of decoupling type.
- **Motivation (theory):** instability of EW scale, gravity.
- **Motivation (observation):** dark matter and energy, and matter anti-matter asymmetry in the universe.
- **Strategies:** high energy or **high precision**.
- 2 general types of precision test: SM allowed (PV scattering) or SM forbidden/highly suppressed (EDMs).

The Standard Model

$$\mathcal{L}_F = \sum \bar{\Psi}_f \left(i \not{\partial} - m_f - \frac{\lambda_f}{\sqrt{2}} \right) \psi_f$$

$$- \frac{g}{2\sqrt{2}} \sum \bar{\Psi}_f \gamma^\mu (1 - \gamma_5) (T^+ W_\mu^+ + T^- W_\mu^-) \psi_f$$

$$- e \sum Q_f \bar{\Psi}_f \gamma^\mu \psi_f A_\mu$$

$$- \frac{\sqrt{g^2 + g'^2}}{2} \sum \bar{\Psi} \gamma^\mu (v_f - a_f \gamma_5) \psi Z_\mu^0$$

$$v_f \equiv T_3^f - 2Q_f \sin^2 \theta_W \quad \quad a_f \equiv T_3^f$$

Weak Mixing Angle

$$\begin{aligned} Z_\mu^0 &= \cos \theta_W W_\mu^3 - \sin \theta_W B_\mu \\ A_\mu &= \sin \theta_W W_\mu^3 + \cos \theta_W B_\mu \end{aligned}$$

$$\sin^2 \theta_W = \frac{g'^2}{g^2 + g'^2} = 1 - \frac{M_W^2}{M_Z^2}$$

$$e = g \sin \theta_W = g' \cos \theta_W$$

SM parameters

- Besides Yukawa sector, SM described by
 - 3 gauge couplings ($\alpha, \sin^2 \theta_W, \alpha_s$)
 - 2 parameters from Higgs potential (G_F, M_H)
- α, G_F, M_Z known with negligible uncertainty
 α_s, M_H (or alternatively $\sin^2 \theta_W$) from precision EW data

Some Background

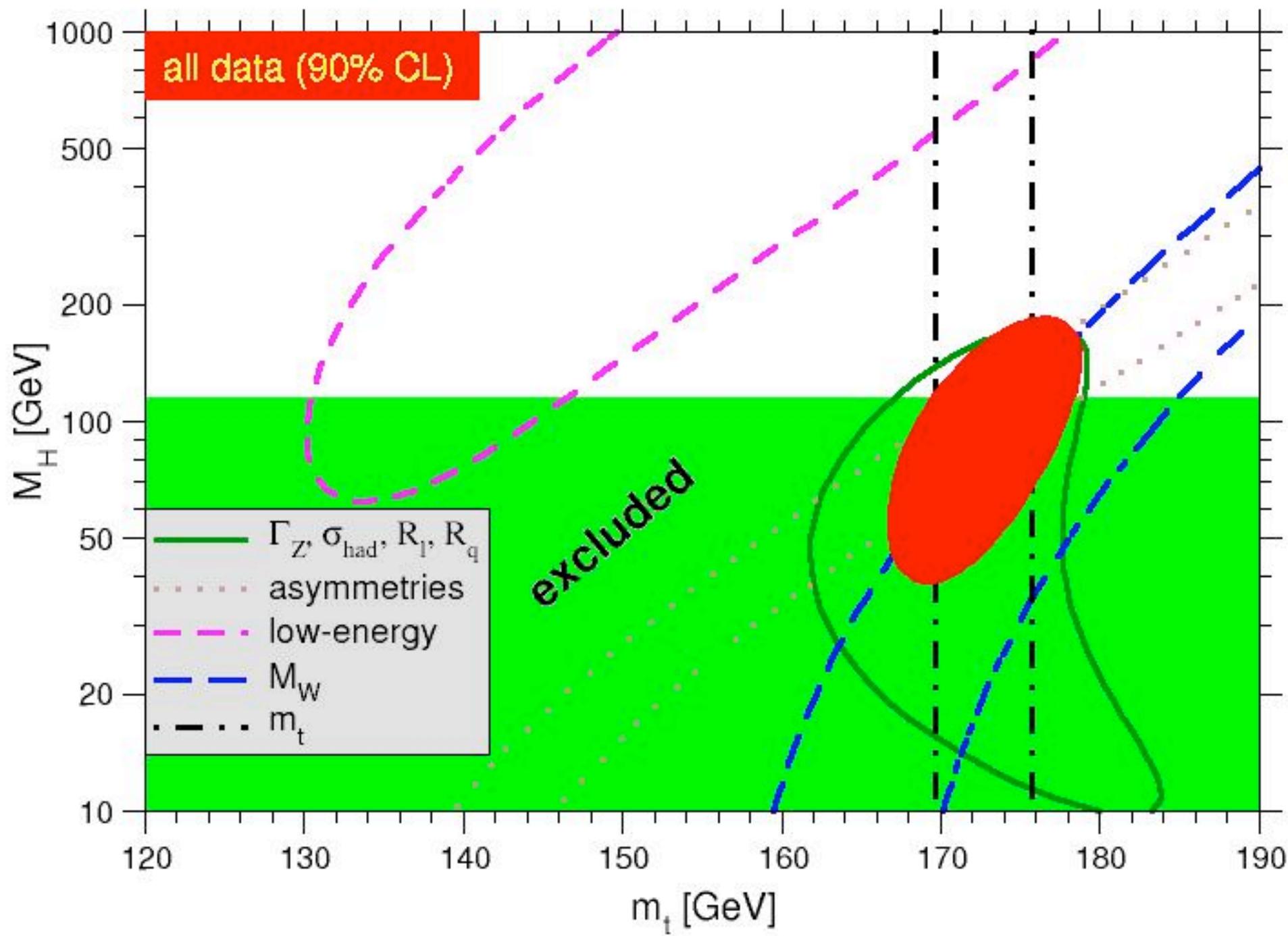
$$\sin^2 \hat{\theta}_W(M_Z) \equiv \hat{s}^2 = \frac{A^2}{M_W^2(1 - \Delta\hat{r}_W)}$$

$$\hat{s}^2 \hat{c}^2 = \frac{A^2}{M_Z^2(1 - \hat{\Delta}r_Z)}$$

$$A = \left[\frac{\pi \alpha}{\sqrt{2} G_F} \right]^{1/2} = 37.2805(2) \text{ GeV}$$

$\hat{\Delta}r_W, \hat{\Delta}r_Z$ collect radiative corrections. . .

September 2005



Global Fit

September 2005 + new top quark and
W boson masses as of October 2006

$$M_H = 84^{+32}_{-25} \text{ GeV}$$

$$m_t = 171.4 \pm 2.1 \text{ GeV}$$

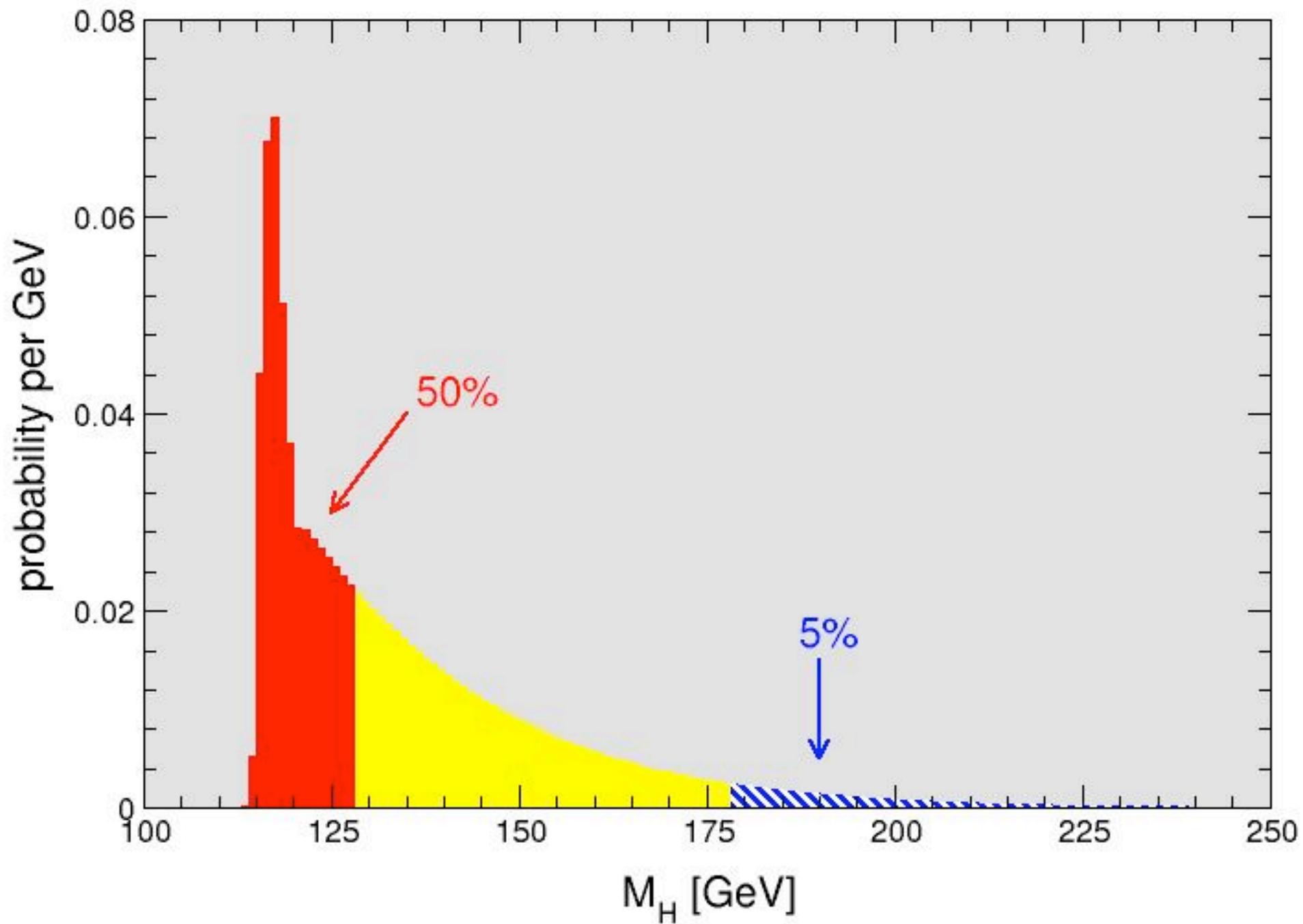
$$\alpha_s(M_Z) = 0.1216 \pm 0.0017$$

$$\chi^2/\text{d.o.f.} = 47.3/42 \text{ (27\%)}$$

indirect only:

$$m_t = 171.0^{+9.5}_{-7.1} \text{ GeV}$$

October 2006



Physics Beyond the SM

- **Supersymmetry** stabilizes Higgs potential,

$$V(\phi) = m_\phi^2 \phi^\dagger \phi + \frac{\lambda^2}{2} (\phi^\dagger \phi)^2,$$

by virtue of non-renormalization theorems.

- **Dynamical symmetry breaking** (e.g. technicolor)

avoids fundamental scalar.

- **Large extra dimensions** relate gauge hierarchy to geometry of higher dimensional space-time.

- **Little Higgs**: Higgs as pseudo-Goldstone boson → postpone quadratic divergences.

Weak Neutral Current

- The effective Lagrangian
- Parity violating DIS
- Polarized electron-proton scattering
- Polarized Møller scattering
- Parity violation in atoms
- Neutrino scattering
- The running weak mixing angle

effective lepton-hadron Lagrangian

$$\mathcal{L}_{\text{NC}}^{\ell h} = \frac{G_F}{\sqrt{2}} \sum_q [C_{1q} \bar{\ell} \gamma^\mu \gamma_5 \ell \bar{q} \gamma_\mu q + C_{2q} \bar{\ell} \gamma^\mu \ell \bar{q} \gamma_\mu \gamma_5 q + C_{3q} \bar{\ell} \gamma^\mu \gamma_5 \ell \bar{q} \gamma_\mu \gamma_5 q]$$

$$C_{1q} = -T_3^q + 2Q_q \sin^2 \theta_W,$$

$$C_{2u} = -C_{2d} = -\frac{1}{2} + 2 \sin^2 \theta_W,$$

$$C_{3u} = -C_{3d} = \frac{1}{2}.$$

PV-DIS

$$A_{RL} = \frac{3G_F Q^2}{10\sqrt{2}\pi\alpha} [(2C_{1u} - C_{1d}) + g(y)(2C_{2u} - C_{2d})]$$

- eD-DIS experiment by **Prescott et al. (SLAC)** crucial to establish SM (before W/Z discovery!)
- Situation from APV confused at the time.
- **CERN-NA-004:** $\mu^- \uparrow \mu^+ \downarrow$
- JLab @ 6 GeV (approved) and 12 GeV will improve on **SLAC** and **world average** by factors of **54** and **17**.
- Issues: **higher twist** and **CSV**; functions of **Q^2** and **x**.
- Limited by **polarization** and **Q^2** measurements (0.5%).

CEBAF at Jefferson Lab



Qweak in Hall C

Qweak

Similar $Q^2 = 0.03 \text{ GeV}^2$ as E-158 but $E = 1.165 \text{ GeV}$.

$$P = 0.85 \pm 0.01$$

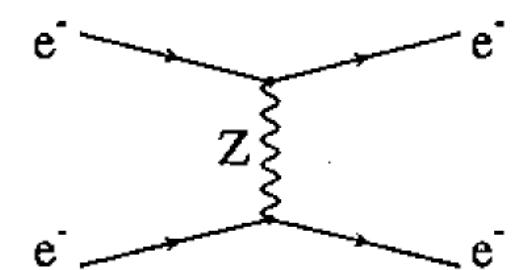
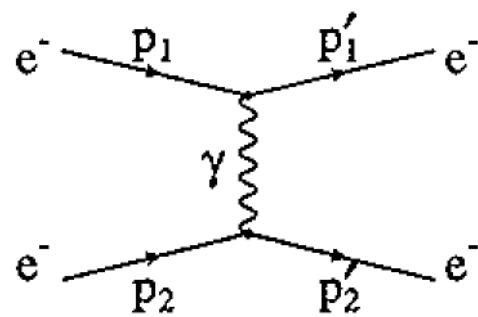
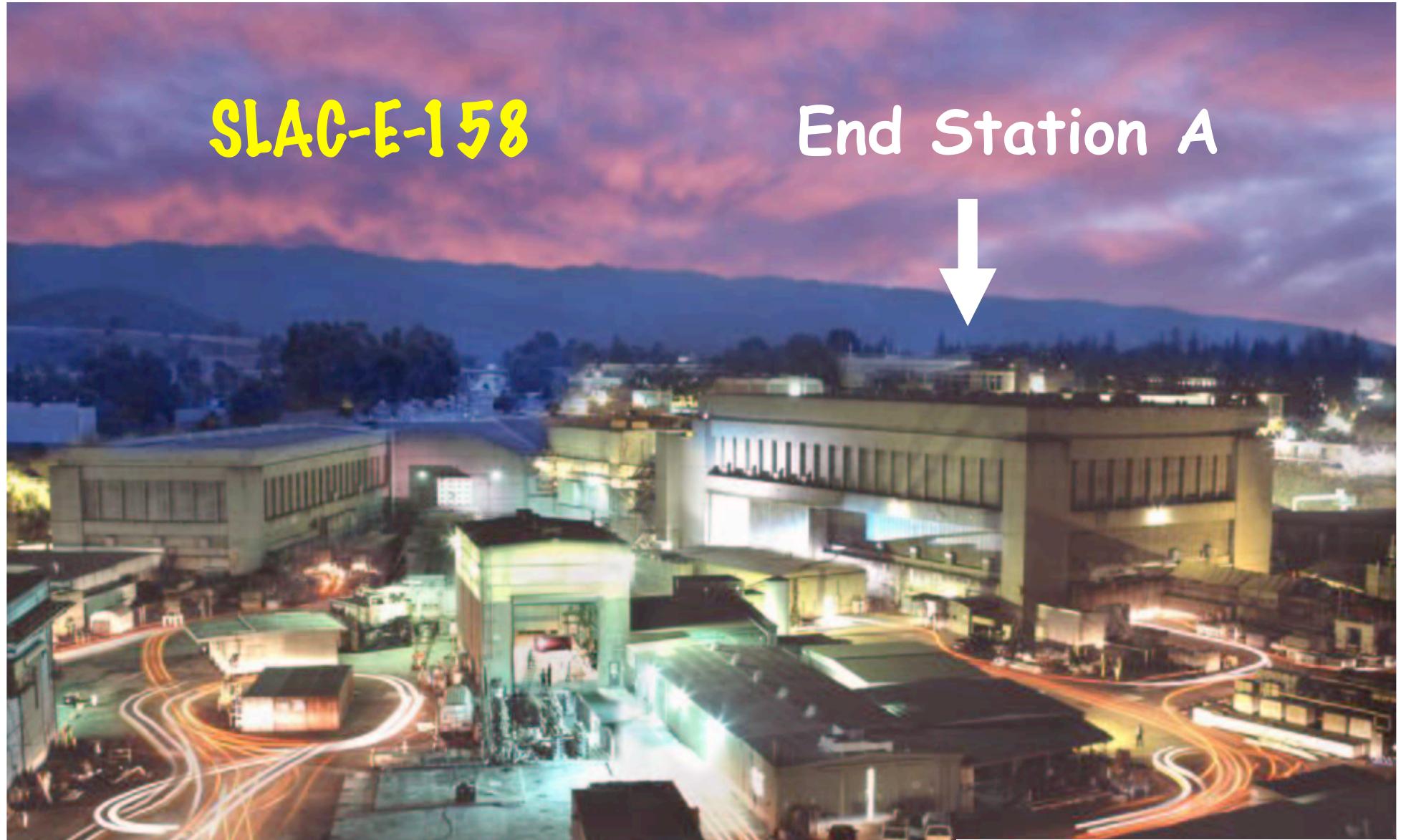
$$A_{PV} = (-2.68 \pm 0.05 \pm 0.04) \times 10^{-7}$$

$$\begin{aligned} A_{PV} &= 9 \times 10^{-5} \text{ GeV} (Q^2 Q_W^p + Q^4 B) \\ \Rightarrow \Delta Q_W^p &= \pm 0.003 \\ \Rightarrow \Delta \sin^2 \theta_W &= \pm 0.0007 \end{aligned}$$

don't miss plenary talk by Bob Michaels!

SLAC-E-158

End Station A



The Møller Asymmetry

$Q^2 = 0.026 \text{ GeV}^2$ ($E = 45$ and 48 GeV), $P = 0.89 \pm 0.04$

Very high rates: 660 M pulses, 500 G electrons per pulse

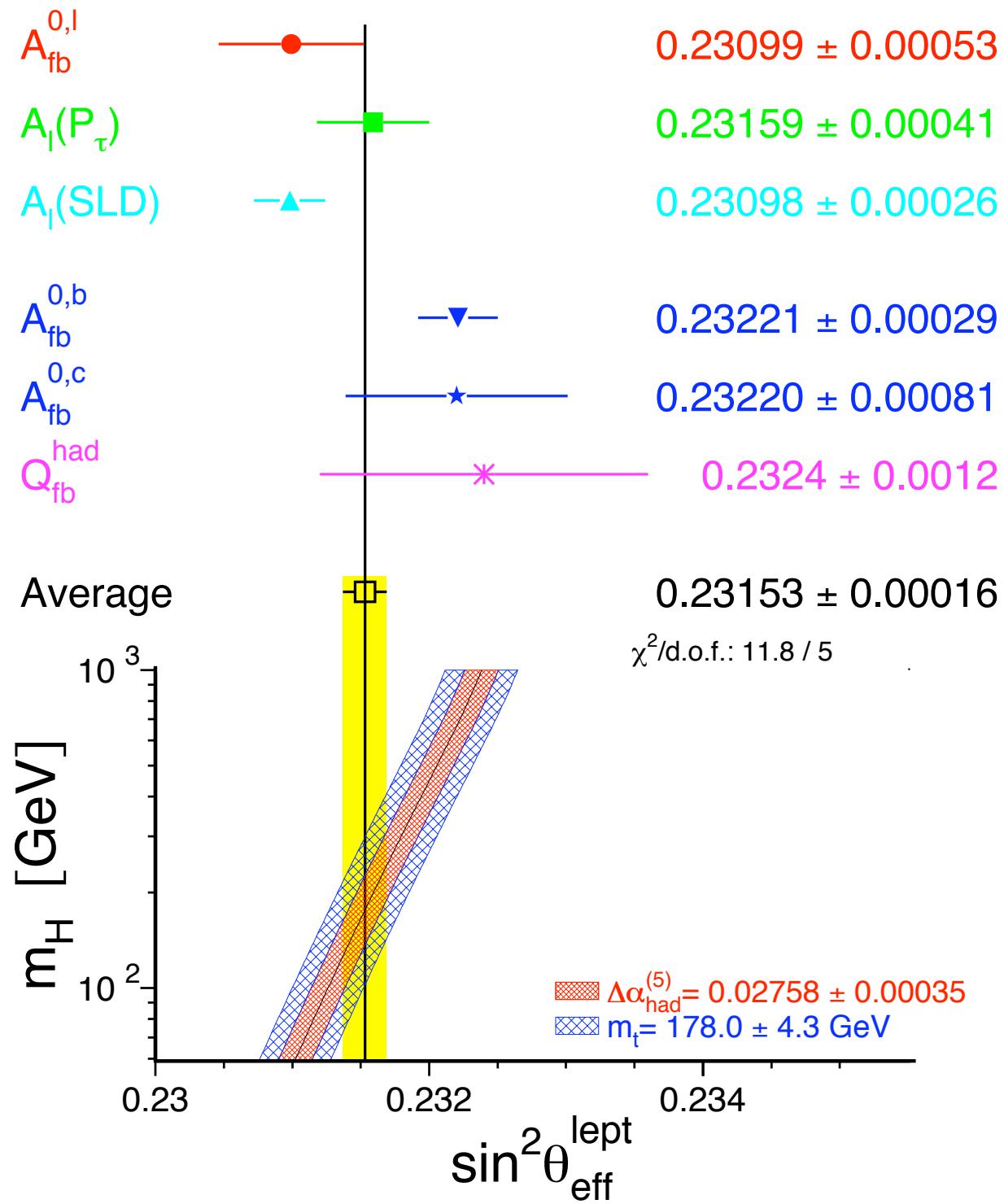
$$A_{PV} = (-1.31 \pm 0.14 \pm 0.10) \times 10^{-7}$$

$$A_{PV} = -\mathcal{A}(Q^2, y) Q_W^e \Rightarrow Q_W^e = -0.0403 \pm 0.0053$$

$$\Rightarrow \sin^2 \hat{\theta}_W(M_Z) = 0.2330 \pm 0.0014$$

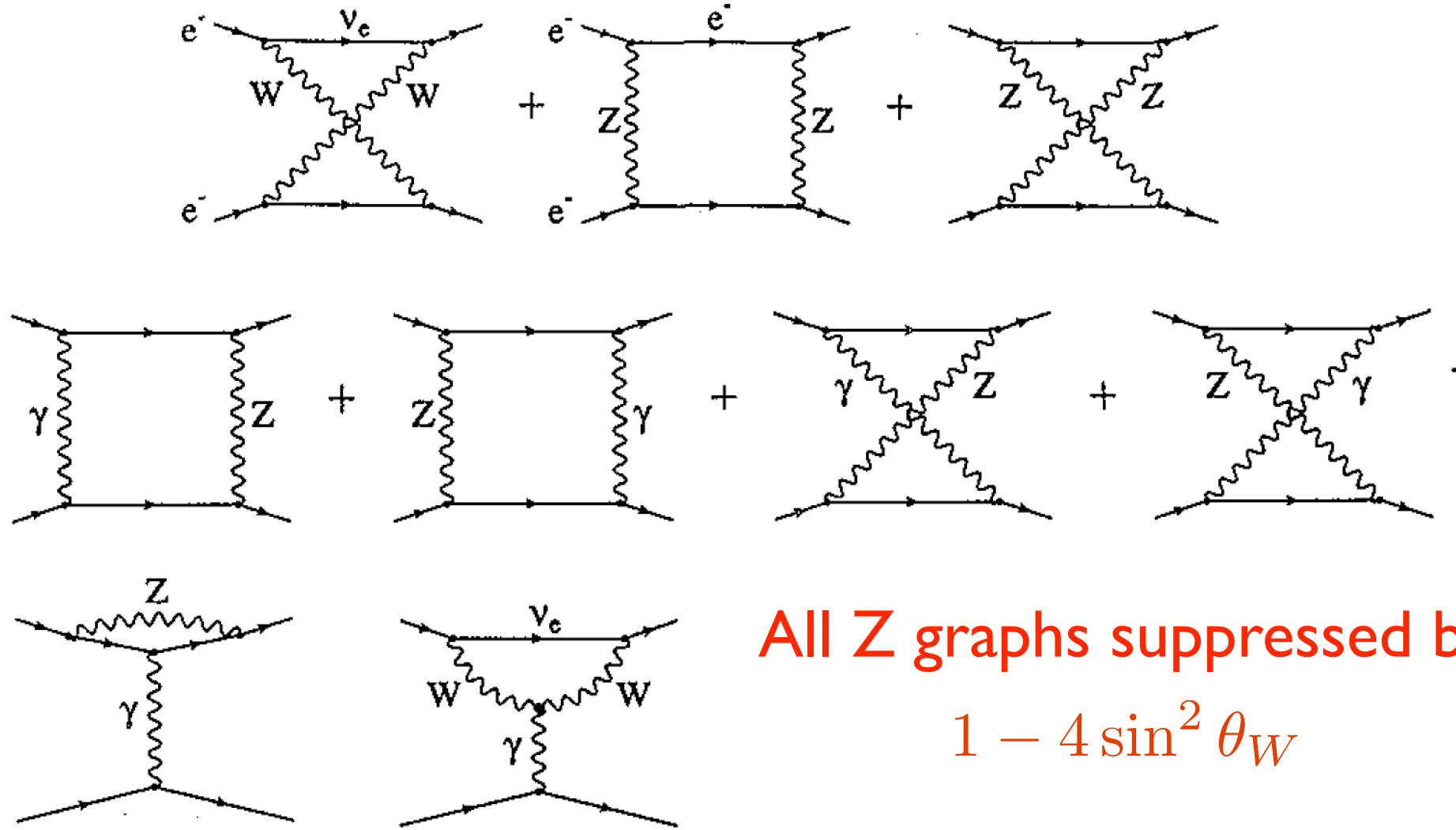
SLD: ± 0.00029 , best LEP: ± 0.00028

With a factor of 5 improvement would become
world's best measurement



Radiative Corrections to Q_W^e

Czarnecki & Marciano



Radiative Corrections to Q_W^p

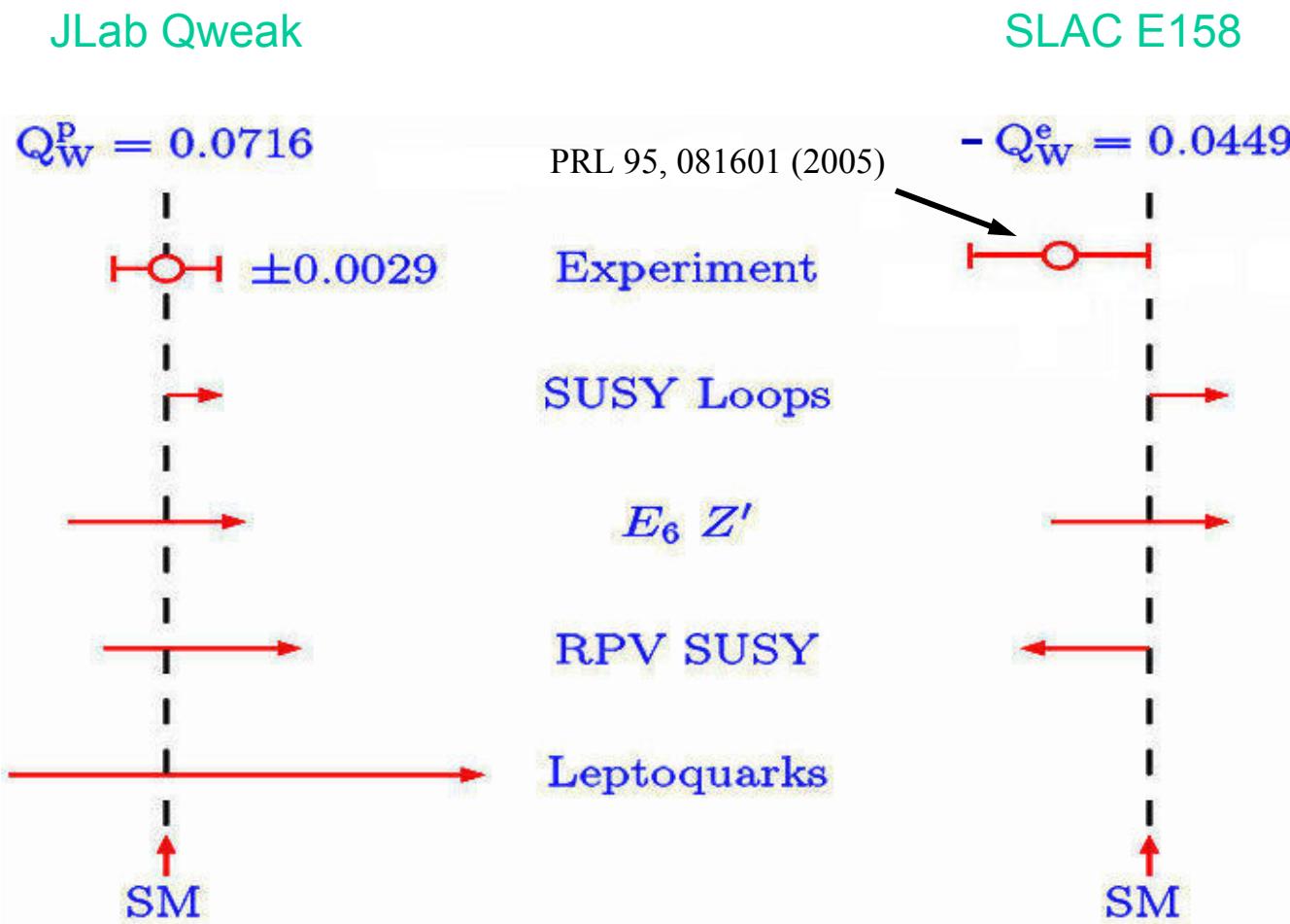
Marciano & Sirlin, Ramsey-Musolf & JE

$$Q_W^p = [\rho_{NC} + \Delta_e][1 - 4 \sin^2 \hat{\theta}_W(0) + \Delta'_e] \\ + \square_{WW} + \square_{ZZ} + \square_{\gamma Z}$$

- Similar structure as for Møller scattering.
- γZ box: long-distance QCD, suppressed by $1 - 4 \sin^2 \theta$.
- WW -box has factor 7 over Møller $\Rightarrow 26\%$ effect!
- \Rightarrow need 2-loop mixed electroweak-QCD corrections.

$$\square_{WW} = \frac{\hat{\alpha}}{4\pi \sin^2 \hat{\theta}_W} \left[2 + 5 \left(1 - \frac{\alpha_s(M_W^2)}{\pi} \right) \right]$$

Proton and Electron Measurements Are Needed



$$\left(\frac{\Lambda}{g}\right)_{\text{new}} = \frac{1}{\sqrt{\sqrt{2}G_F |\Delta Q_W^p|}} \approx 4.6 \text{ TeV}$$

Atomic Parity Violation

- Need to understand atomic structure below %-level.
- Most precise: $Q_W(\text{Cs}) = -72.62 \pm 0.46$
 $Q_W(\text{Tl}) = -116.4 \pm 3.64$

Wood et al., Bouchiat et al.

Edwards et al., Vetter et al.

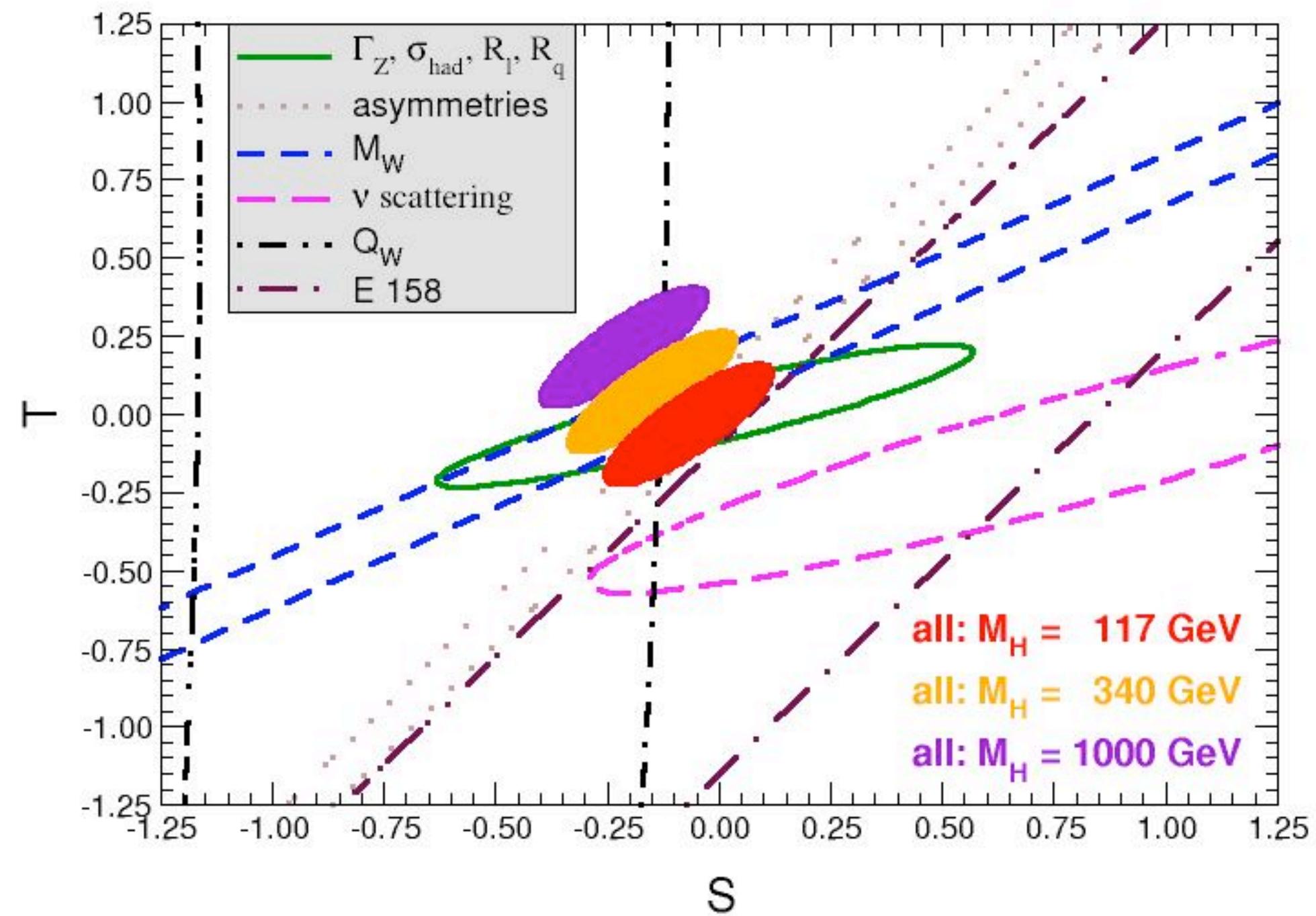
- Bi: $\pm 1\%$ experiment, Meekhof et al., but $\pm 15\%$ theory.
- Fr: $\pm 1\%$ theory but $\pm 10\%$ experiment (atom trap), Orozco et al.

talk by Victor Flambaum after this

APV (contd.)

- future directions: Ba⁺ (Cs-like) ion trap: $\pm 0.35\%$
Fortson et al.
- Yb isotope ratios: $\pm 0.1\%$ (mostly sensitive to Q_W^p).
DeMille, Kimball, Stalnaker et al.
- Finite nuclear size effects dominated by neutron distribution (0.15%) → problem for isotope chains.
- APV = nuclear spin independent + spin dependent terms: nuclear anapole moment dominates ($A > 20$).
- Improve experiment and theory on neutron density. Or use APV to study nuclear structure.

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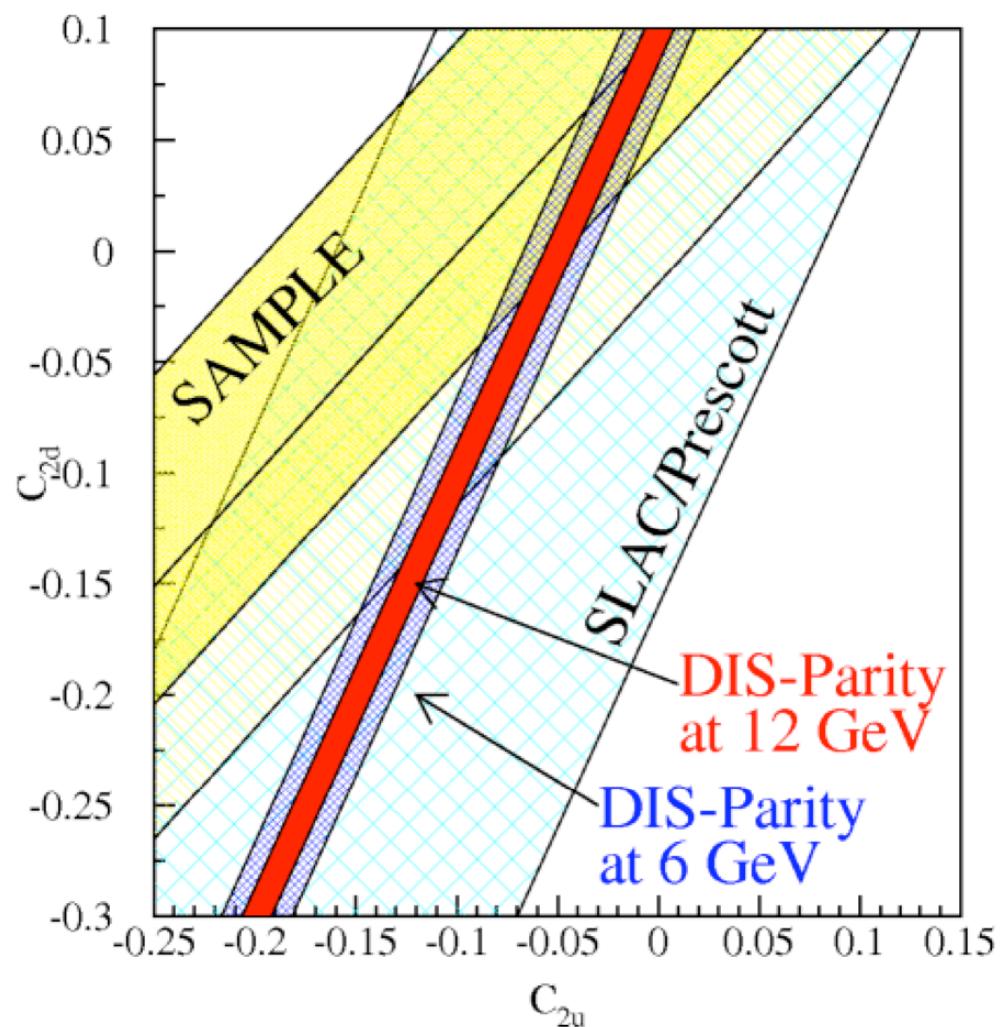
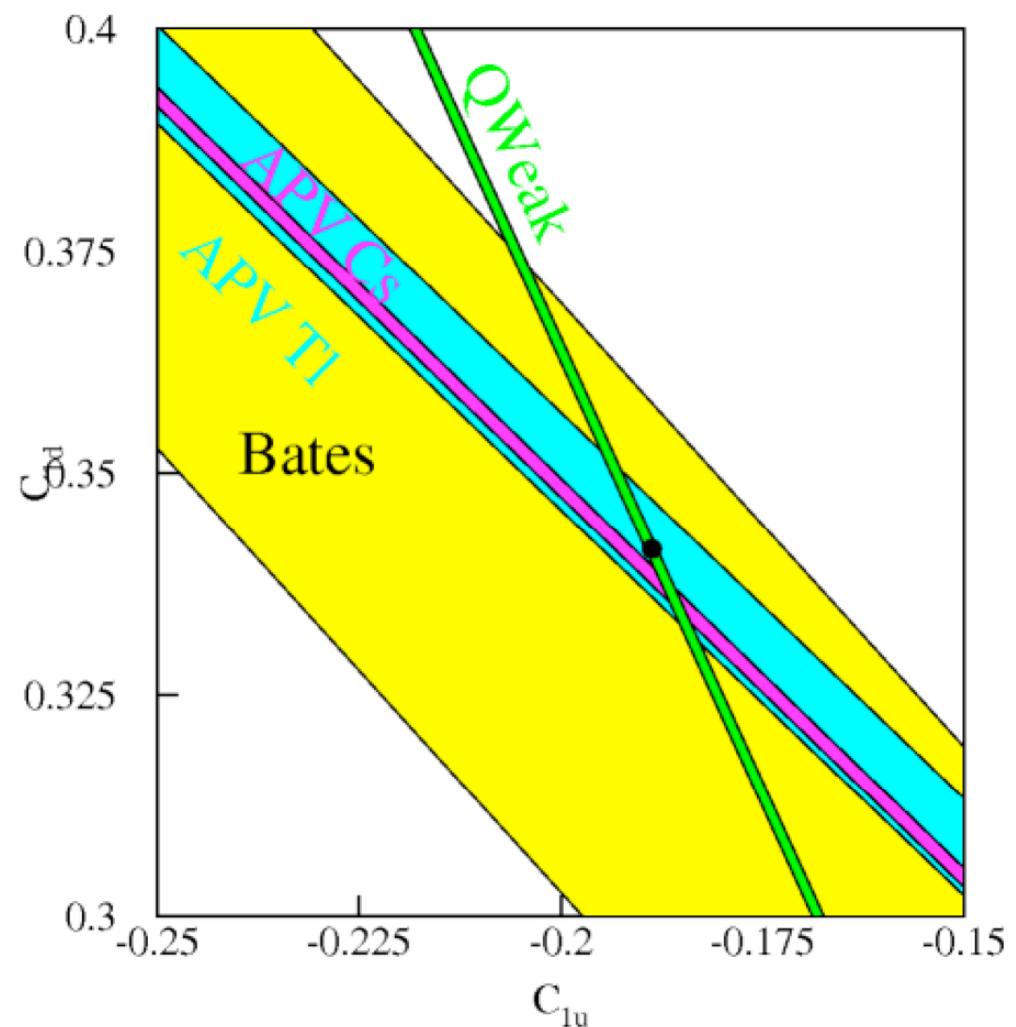


LEPTON-HADRON COUPLINGS

beam	Process	$\overline{Q^2}$ [GeV 2]	Combination	Result/Status	SM
SLAC	e^- -D DIS	1.39	$2C_{1u} - C_{1d}$	-0.90 ± 0.17	-0.7181
SLAC	e^- -D DIS	1.39	$2C_{2u} - C_{2d}$	$+0.62 \pm 0.81$	-0.0979
CERN	μ^\pm -C DIS	34	$0.66(2C_{2u} - C_{2d})$ $+2C_{3u} - C_{3d}$	$+1.80 \pm 0.83$	+1.4354
CERN	μ^\pm -C DIS	66	$0.81(2C_{2u} - C_{2d})$ $+2C_{3u} - C_{3d}$	$+1.53 \pm 0.45$	+1.4207
Mainz	e^- -Be QE	0.20	$2.68C_{1u} - 0.64C_{1d}$ $+2.16C_{2u} - 2.00C_{2d}$	-0.94 ± 0.21	-0.8532
Bates	e^- -C elastic	0.0225	$C_{1u} + C_{1d}$	$+0.138 \pm 0.034$	+0.1528
Bates	e^- -D QE	0.1	$C_{2u} - C_{2d}$	-0.042 ± 0.057	-0.0621
Bates	e^- -D QE	0.04	$C_{2u} - C_{2d}$	-0.12 ± 0.074	-0.0621
JLab	e^- - p elastic	0.03	$2C_{1u} + C_{1d}$	approved	-0.0356
JLab	e^- -D DIS	1.1 & 1.9	$2C_{2u} - C_{2d}$	approved	-0.0979
JLab	e^- -D DIS	3.3	$2C_{2u} - C_{2d}$	letter of intent	-0.0979
—	^{133}Cs APV	0	$-376C_{1u} - 422C_{1d}$	-72.69 ± 0.48	-73.17
—	^{205}Tl APV	0	$-572C_{1u} - 658C_{1d}$	-116.6 ± 3.7	-116.8

Fit to effective couplings

	value	error	SM	Correlation			
$C_{1u} + C_{1d}$	0.147	± 0.004	0.1529(1)	0.95	-0.75	-0.10	
$C_{1u} - C_{1d}$	-0.604	± 0.066	-0.5297(4)		-0.79	-0.10	
$C_{2u} + C_{2d}$	0.72	± 0.89	-0.0095			-0.11	
$C_{2u} - C_{2d}$	-0.071	± 0.044	-0.0621(6)				

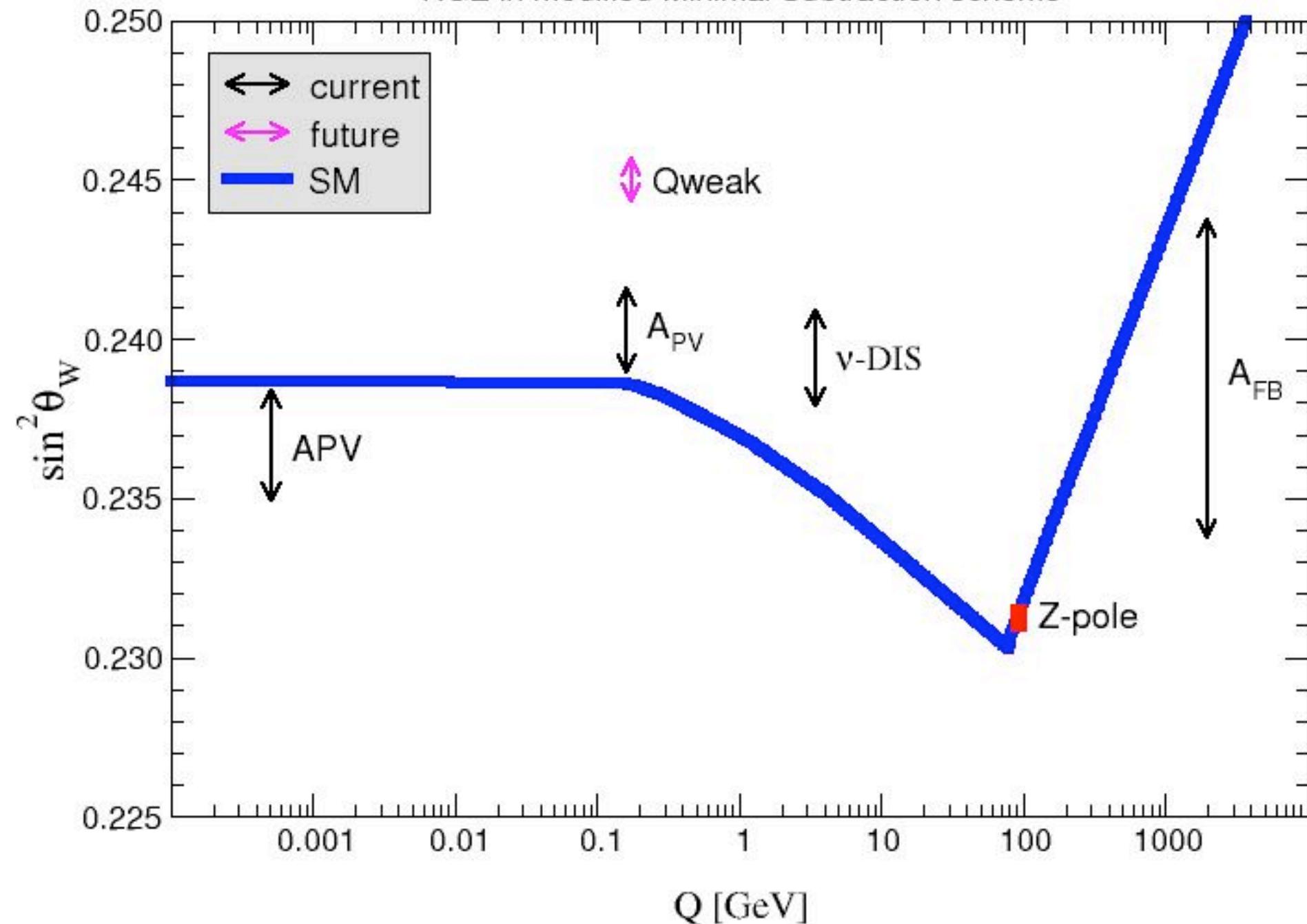


NuTeV

- 2.7σ (largest deviation)
- new QED radiative corrections (Diener, Dittmaier, Hollik) but not yet included by NuTeV collaboration
- Charge Symmetry Violation can remove or double the effect (MRST); model dependent
- s-quark asymmetry: 25% of effect (CTEQ), wrong sign (NuTeV) based on same data
- nuclear effects: different for NC and CC; $\sim 20\%$ of effect, both signs possible (Brodsky, Schmidt, Yang)

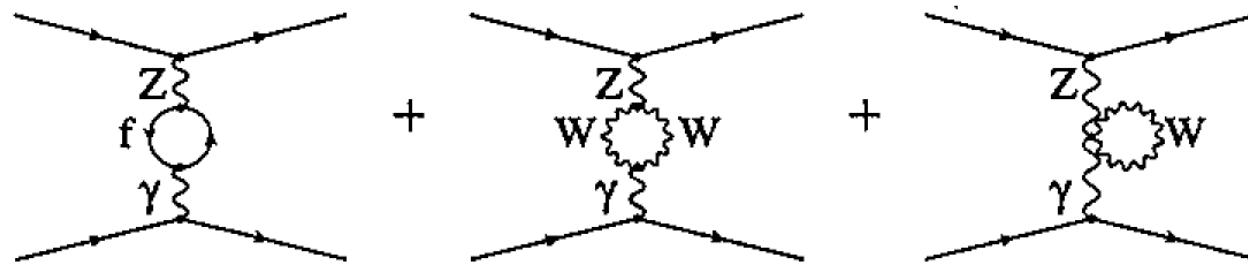
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RGE in modified Minimal Subtraction scheme



Radiative Corrections

Marciano & Sirlin; Ramsey-Musolf & JE



- Need $e^+e^- \rightarrow$ hadrons and/or hadronic tau decay **data** for quark (hadron) contribution.
- Assume (and correct for) **isospin symmetry**.
- Separate **strange quark** contribution \rightarrow study scaled heavy quark and SU(3) limits.
- Discuss **singlet** (QCD-annihilation) contribution (very small).
⇒ small theory error = ± 0.00007 .

μ -decay

$$\tau_\mu \Rightarrow G_F = 1.16637 \pm 0.00001 \text{ (exp.)} \rightarrow$$

2 new experiments at PSI (FAST and μ Lan); goal 1 ppm

Michel parameters

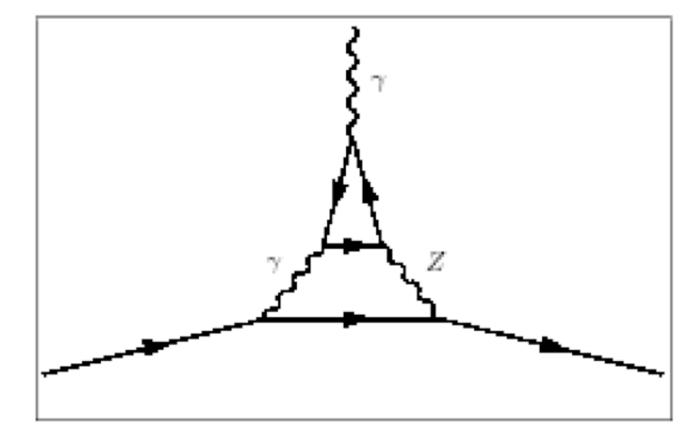
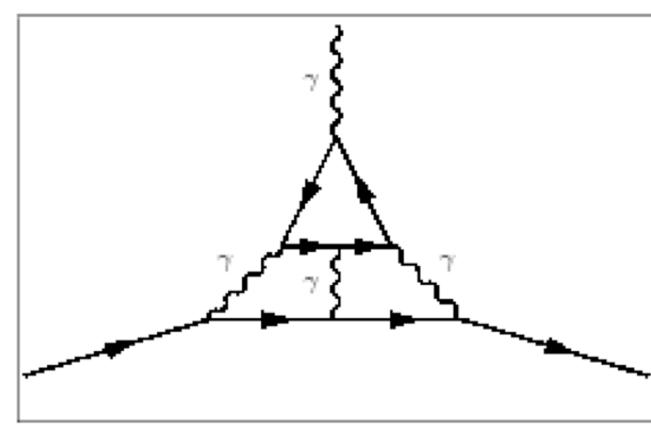
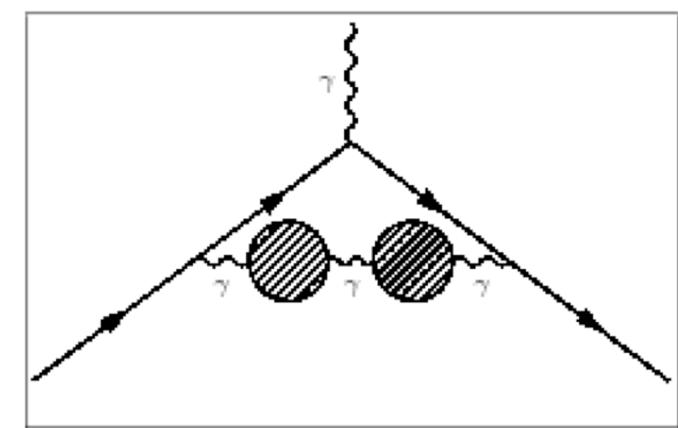
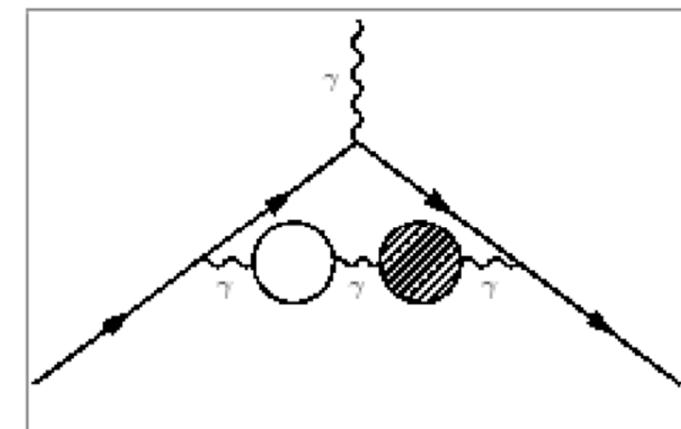
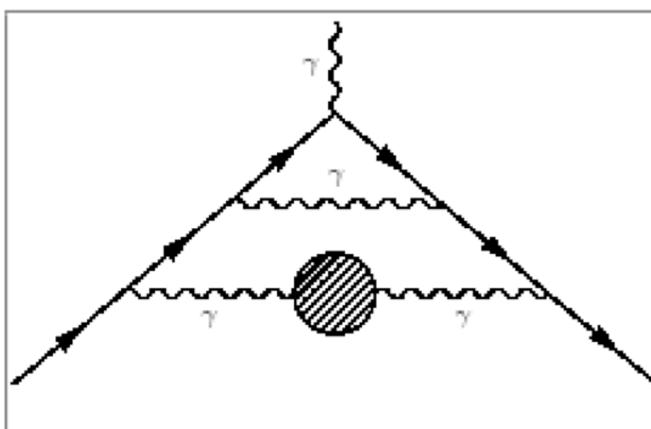
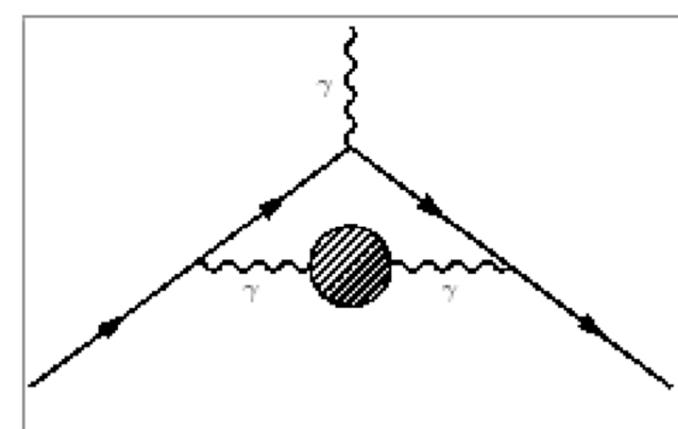
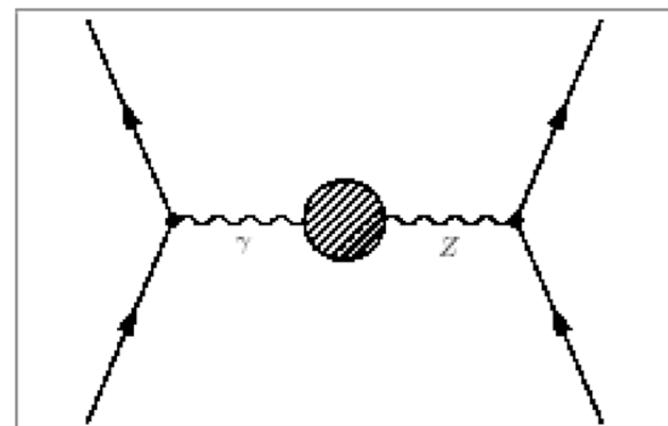
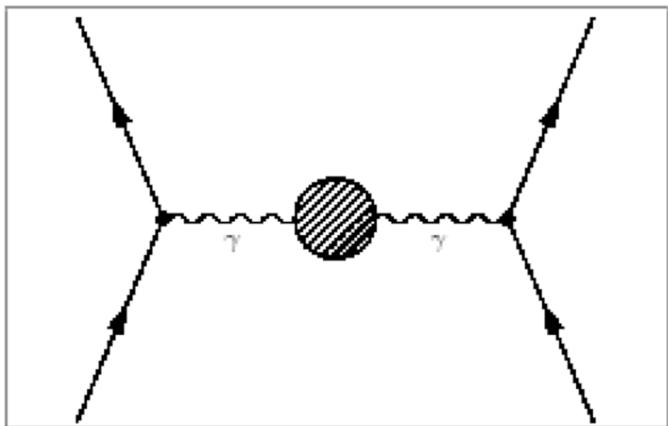
	value	error	SM	TWIST
ρ (spectral shape)	0.7518	± 0.0026	3/4	± 0.0001
δ (asymmetry shape)	0.7486	± 0.0040	3/4	± 0.00014
$P(\mu)\xi$ (asymmetry)	1.0027	± 0.0085	1	± 0.00013
η e-mass suppressed	-0.007	± 0.013	0	± 0.003

talk by Wulf Fetscher in Session 1,3 on Friday

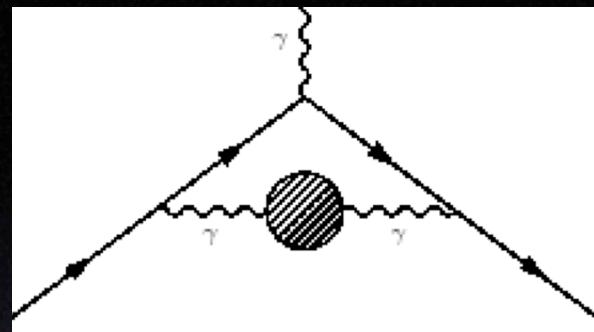
Muon g-2

- 2 to 3 σ deviation from SM
- for 2-loop vacuum polarization contribution
need optical theorem and same data as for
running α and running weak mixing angle
- inconsistencies between e+ e- annihilation data
- inconsistencies between τ decay and e+ e- data
- extra trouble: 3-loop light-by-light contribution

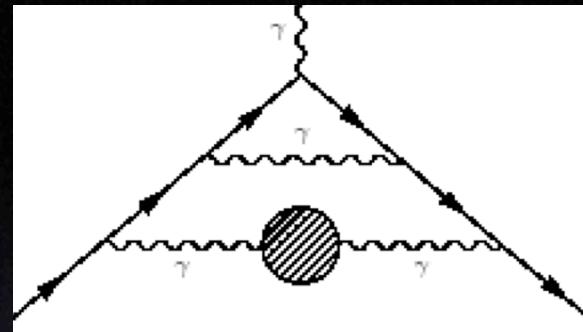
talk by Gerry Bunce in Session I,3 on Friday



vacuum polarization effects

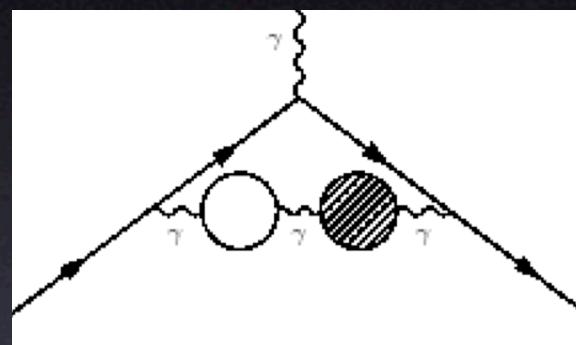


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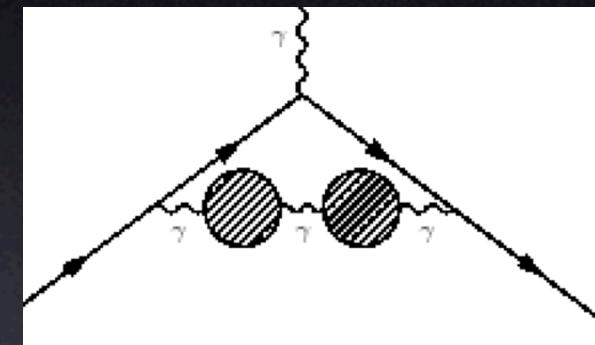


(2a)

(2c)

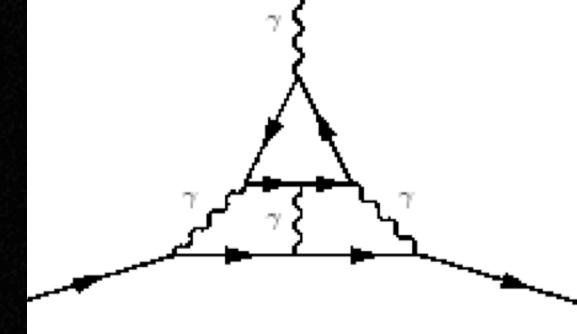


(2b)



kernel	free quarks	data	deviation
$K^{(1)}$	+65.1	+70.3	8%
$K^{(2a)}$	-2.11	-1.82	14%
$K^{(2b)}$	+1.07	+0.99	7%
$K^{(2c)}$	+0.027	+0.028	4%

Light-by-light contribution



- free quark estimate (using quark masses for running α)
- exact for infinitely heavy quarks (short distances OK)
- overestimate in chiral limit with m_μ/m_π fixed
(charged pointlike pions contribute negatively)
- VMD: $1.36 \pm 0.25 \times 10^{-9}$ (error: “rough guess”; $\mu \sim 0.6$ GeV) Melnikov & Vainshtein, PRD70, 113006 (2004)

free quarks $\left\{ \begin{array}{l} 1.37_{-0.27}^{+0.15} \times 10^{-9} \\ < 1.59 \times 10^{-9} \text{ (95% CL)} \end{array} \right.$ Toledo, JE

Electric Dipole Moments

- SM weak **CP** (CKM-phase) mixing and mass suppressed (many orders too small).
- SM strong **CP** (topological θ -term) limited by EDMs,

$$\mathcal{L}_\theta = \theta_{QCD} \frac{\alpha_s}{8\pi} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

- Baryon asymmetry \Rightarrow **CP** violation beyond the SM, but precise implication for EDMs unclear.

talk by Koichiro Asahi in Session I,3 on Friday

EDM experiments

System	Present Limit ($e\text{-cm}$)	Group	Future	SM (CKM)
e^-	1.6×10^{-27} (90% CL)	Berkeley Yale LANL	$\sim 10^{-29}$ $\sim 10^{-30}$	$< 10^{-38}$
μ	1.05×10^{-18} (90% CL)	CERN BNL	$\sim 10^{-24}$	$< 10^{-36}$
n	6.3×10^{-26} (90% CL)	ILL PSI LANL	1.5×10^{-26}	1.4×10^{-33}
			7×10^{-28}	\rightarrow
			2×10^{-28}	1.6×10^{-31}
^{199}Hg ^{225}Ra ^{129}Xe D	2.1×10^{-27} (95% CL)	Seattle Argonne Princeton BNL	5×10^{-28}	$< 10^{-33}$
			10^{-28}	
			10^{-31}	
			$\sim 10^{-27}$	$< 10^{-34}$

I am sticking my neck out:
the next generation of EDM searches is virtually
guaranteed to make a discovery.

PAUL LANGACKER

Conclusions

- A network of **high precision** polarized electron scattering experiments is set to study TeV scale.
- Next generation μ -decay experiments is looking for deviations from **V—A**.
- Searches for permanent **EDMs** highly motivated with spectacular experimental developments.

Low energy measurements will remain indispensable even with loads of LHC data!