

東京大学

Nov. 24-26, 2010

J-PARC における ストレンジネス核物理

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Outline - I

▶ 1st day

- Historical Overview of Strengeness Nuclear Physics
- Production of Hypernuclei
- Hypernuclear structure and YN interaction
- (π^+ , K^+) Spectroscopy of Λ hypernuclei

▶ 2nd day

- Hypernuclear gamma-ray spectroscopy
- Σ hypernuclei
- Weak decay of Hypernuclei

Outline -2

▶ 3rd day

- J-PARC Facility

- Kaonic Nuclei

- Hypernuclear Spectroscopy of $S = -2$ systems

▶ 物理学教室コロキウム 「ストレンジネスと原子核」



First day in UT

The image features a central white text block "First day in UT" set against a dark green rectangular background. This central element is flanked by two rows of four squares each. The top row consists of two dark green squares followed by two light green squares. The bottom row consists of two light green squares followed by two dark green squares. The squares are arranged in a grid-like pattern with white borders between them.

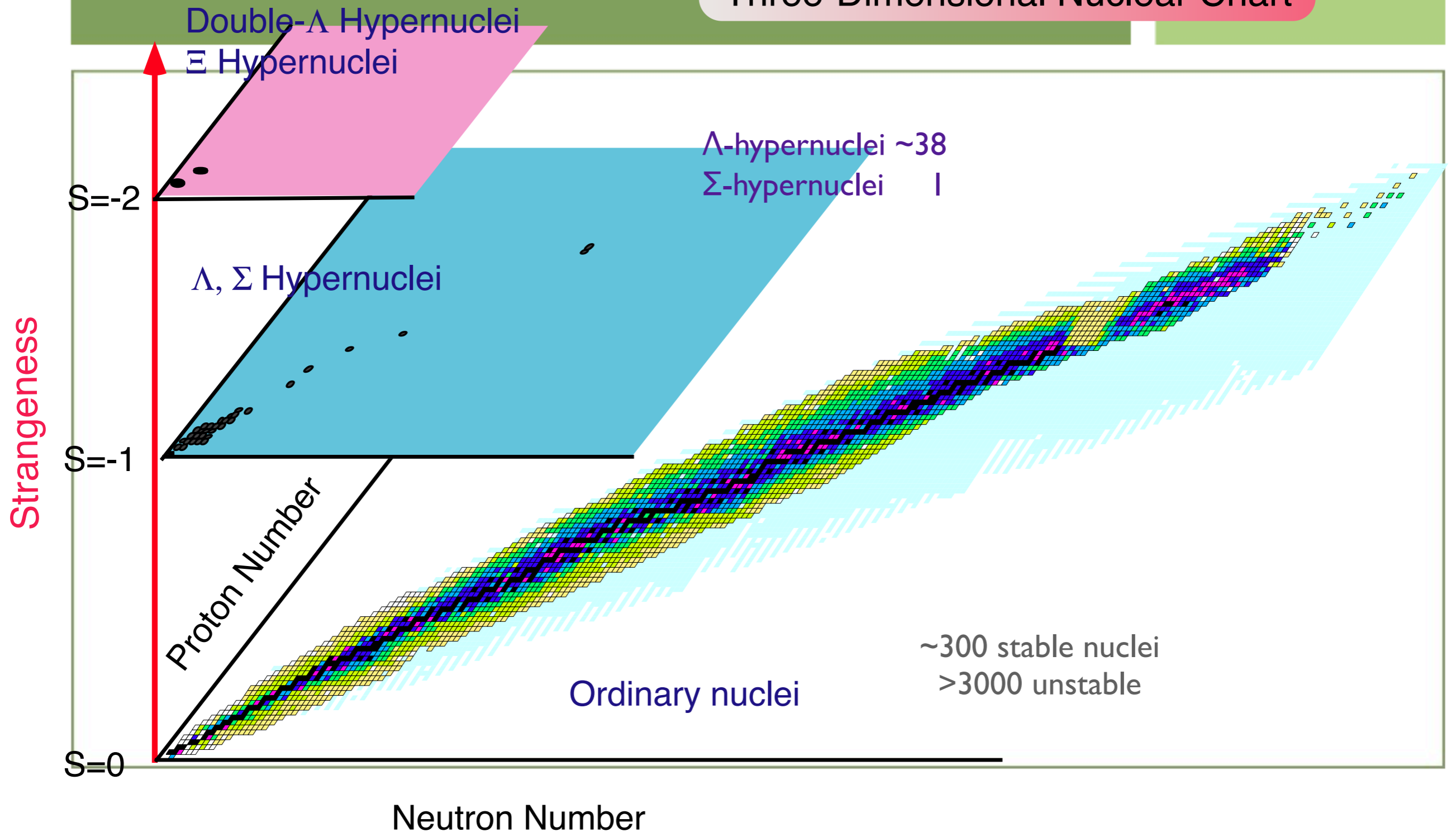
Hypernuclei

► A Nucleus with Hyperons

S		Lifetimes[s]	Main Decay channels	Mass [MeV/c ²]	Isospin
0	p: uud n: udd	Stable(?) 887	$p e^- \nu_e$ (100%)	938.3 939.6	1/2
-1	Λ : uds	2.63×10^{-10}	$p \pi^-$ (64%), $n \pi^0$ (36%)	1115.7	0
-1	Σ^+ : uus Σ^0 : uds Σ^- : dds	0.8×10^{-10} 7.4×10^{-20} 1.48×10^{-10}	$p \pi^0$ (52%), $n \pi^-$ (48%) $\Lambda \gamma$ (~100%) $n \pi^-$ (99.8%)	1189.4 1192.6 1197.4	1
-2	Ξ^0 : uss Ξ^- : dss	2.9×10^{-10} 1.64×10^{-10}	$\Lambda \pi^0$ (~100%) $\Lambda \pi^-$ (~100%)	1315 1321	1/2

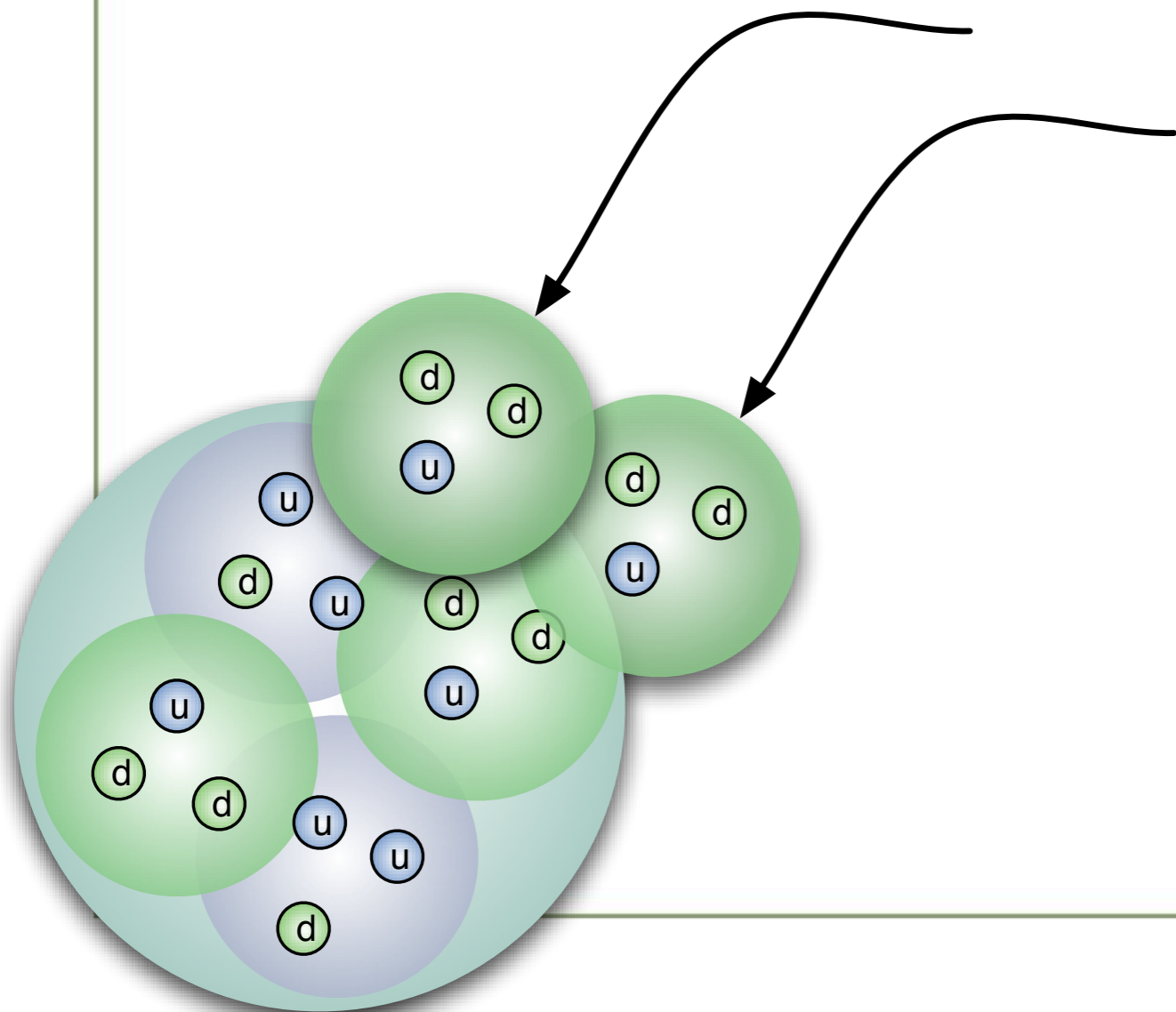
World of Strangeness Nuclear Physics

Three-Dimensional Nuclear Chart



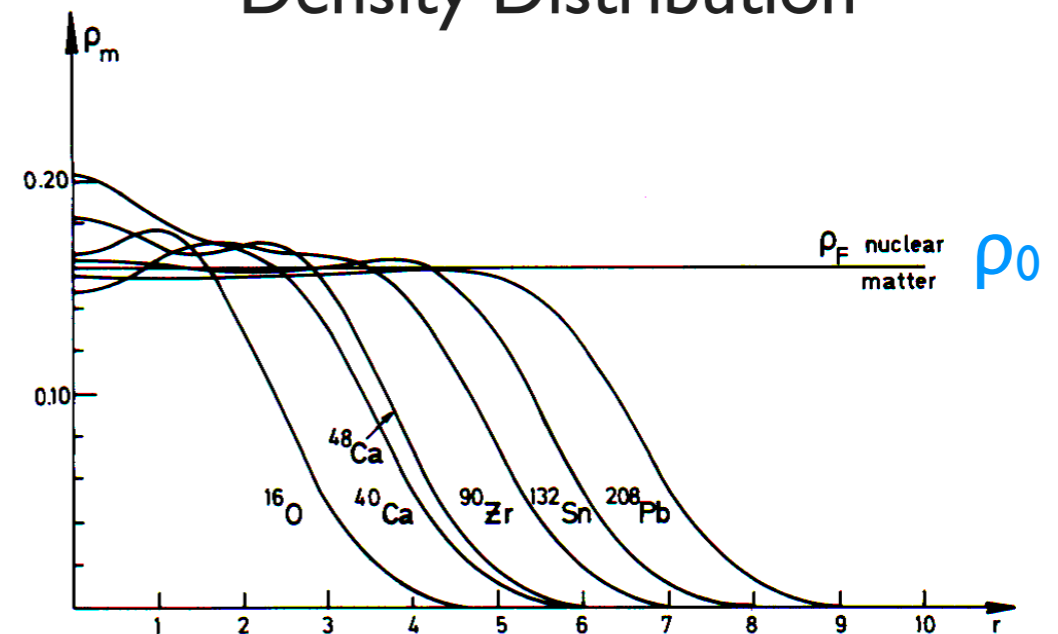
Normal Nuclei

- ▶ Many-Body systems composed of proton(uud)& neutron(udd)
 - ▶ Quark many-body systems with u & d quarks only
- Fermions



Saturation Density: $\rho_0 = 2.5 \times 10^{14} \text{ g/cm}^3$
 Binding Energy: 8 MeV/nucleon
 ← **Pauli Blocking, Repulsive core**

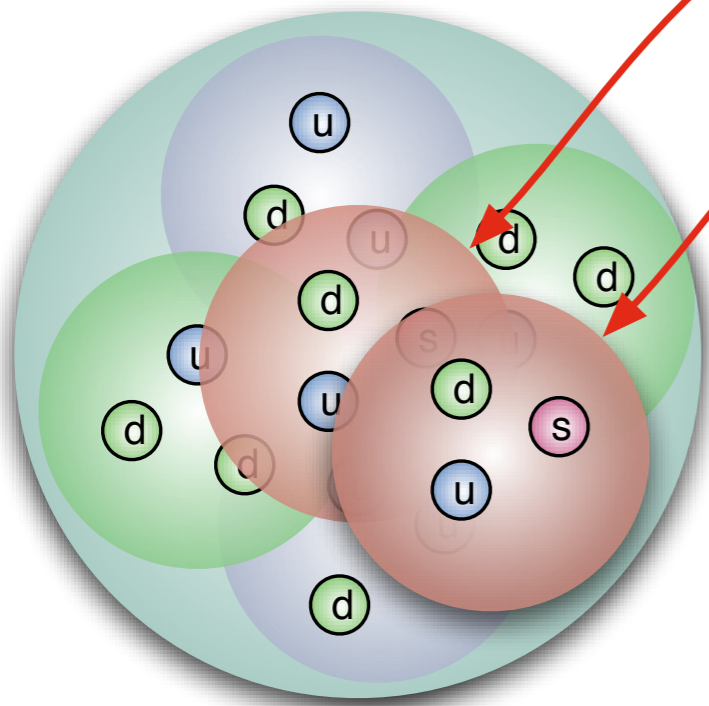
Density Distribution



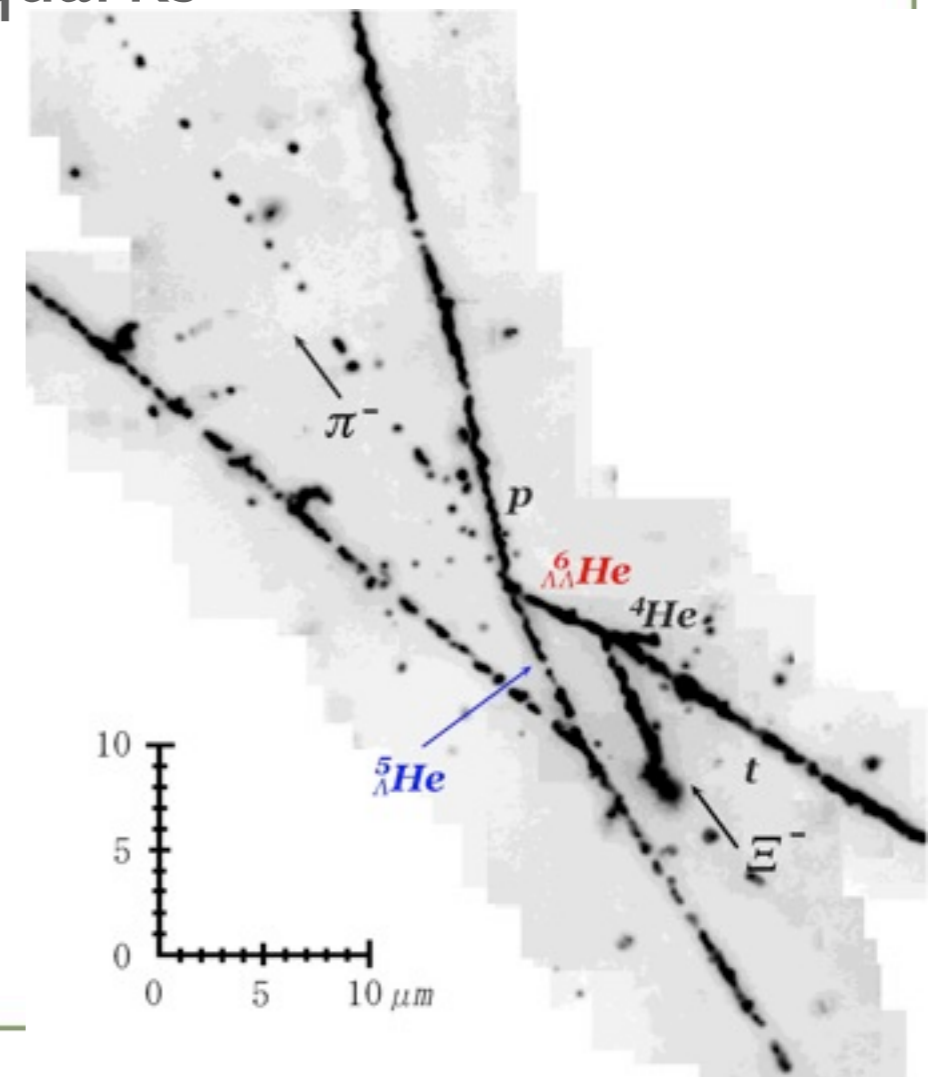
Hypernuclei

- ▶ Λ (uds)-Hypernuclei, Double- Λ Hypernuclei
- ▶ Quark many-body systems with u, d, & s quarks

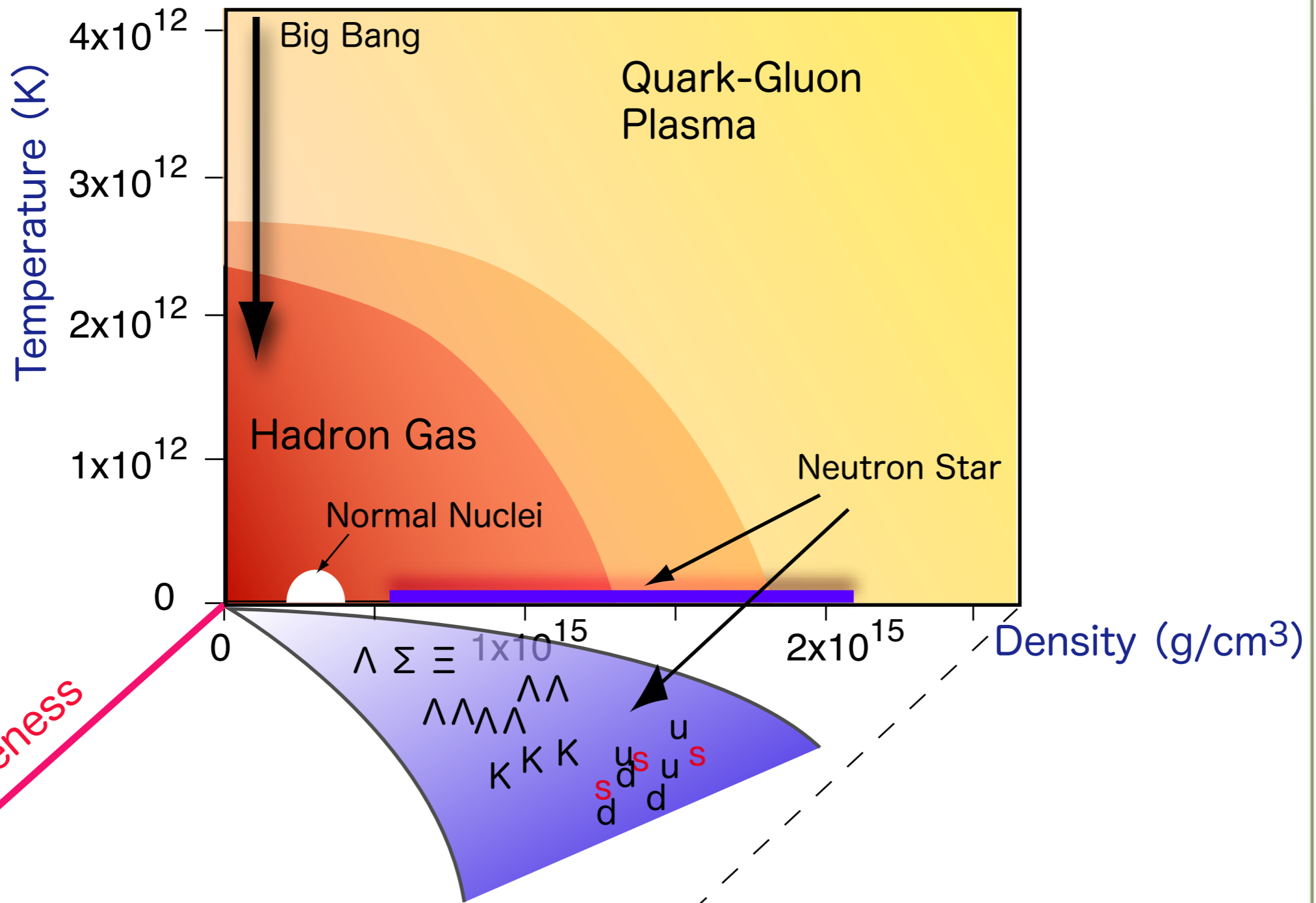
No Pauli Blocking
→ Higher Density



- ▶ Implant s quark(s) with u, d quarks



- ▶ Strangeness Degrees of Freedom
- ▶ Something beyond the “standard” Nuclear Physics



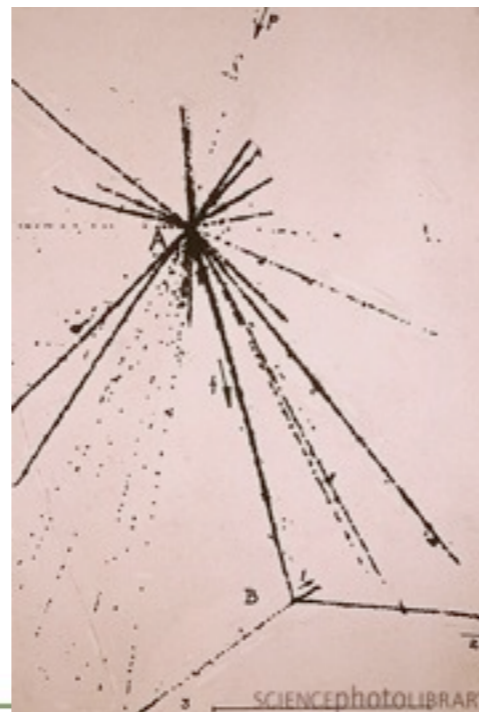
Brief history of Hypernuclear spectroscopy

► Discovery of Hyperfragments (1953) by M. Danysz and J. Pniewski

*ACTA PHYSICA POLONICA B 35 (2004)
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● $\Lambda \sim p, n$

● Discovery of V particles (1947) by G. Rochester and C. Butler



Early days - 1950s~1960s

- ▶ Stopped K^- reactions in Nuclear emulsion and He bubble chamber
 - High efficiency for Hyperfragment formation
 - Identification of Light Hyperfragments
 - ${}^3_{\Lambda}H \sim {}^{15}_{\Lambda}N$
 - Binding energies of ground states
 - Spin assignments for several ground states

Stopped K^- on ${}^4\text{He}$

- ▶ Λ emission $\sim 70\%$
- ▶ Σ emission $\sim 30\%$
- ▶ Non-pionic $\sim 17\%$

TABLE III. Branching ratios for K^- absorption at rest.

Reaction	Events/(stopping K^-) (%)
$K^- \text{He}^4 \rightarrow \Sigma^+ \pi^- \text{H}^3$	9.3 ± 2.3
$\rightarrow \Sigma^+ \pi^- dn$	1.9 ± 0.7
$\rightarrow \Sigma^+ \pi^- pnn$	1.6 ± 0.6
$\rightarrow \Sigma^+ \pi^0 nnn$	3.2 ± 1.0
$\rightarrow \Sigma^+ nnn$	1.0 ± 0.4
Total $\Sigma^+ = (17.0 \pm 2.7)\%$	
$K^- \text{He}^4 \rightarrow \Sigma^- \pi^+ \text{H}^3$	4.2 ± 1.2
$\rightarrow \Sigma^- \pi^+ dn$	1.6 ± 0.6
$\rightarrow \Sigma^- \pi^+ pnn$	1.4 ± 0.5
$\rightarrow \Sigma^- \pi^0 \text{He}^3$	1.0 ± 0.5
$\rightarrow \Sigma^- \pi^0 pd$	1.0 ± 0.5
$\rightarrow \Sigma^- \pi^0 ppn$	1.0 ± 0.4
$\rightarrow \Sigma^- pd$	1.6 ± 0.6
$\rightarrow \Sigma^- ppn$	2.0 ± 0.7
Total $\Sigma^- = (13.8 \pm 1.8)\%$	
$K^- \text{He}^4 \rightarrow \pi^- \Lambda \text{He}^3$	11.2 ± 2.7
$\rightarrow \pi^- \Lambda pd$	10.9 ± 2.6
$\rightarrow \pi^- \Lambda ppn$	9.5 ± 2.4
$\rightarrow \pi^- \Sigma^0 \text{He}^3$	0.9 ± 0.6
$\rightarrow \pi^- \Sigma^0 (pd, ppn)$	0.3 ± 0.3
$\rightarrow \pi^0 \Lambda (\Sigma^0) (pnn)$	22.5 ± 4.2
$\rightarrow \Lambda (\Sigma^0) (pnn)$	11.7 ± 2.4
$\rightarrow \pi^+ \Lambda (\Sigma^0) nnn$	2.1 ± 0.7
Total $\Lambda (\Sigma^0) = (69.2 \pm 6.6)\%$	
Total $= \Lambda + \Sigma = (100_{-7}^{+0})\%$	

Hypernuclear Production by stopped K^-

- ▶ $\text{o}(10^{-3})$ per stopped K^- ; ... not so bad

TABLE IX. Calculated capture rates per stopped K^- (in units of 10^{-3}) for production of $1s_\Lambda$ states (1^- transition) and $1p_\Lambda$ states (0^+ and 2^+ transitions) and selected experimental rates.

Transition	Input	$^{12}_\Lambda\text{B}$ [3]	$^{12}_\Lambda\text{C}$ [2]	$^{16}_\Lambda\text{O}$ [2]
1^-	$[K_\chi]$	0.203	0.425	0.219
	$[K_{\text{DD}}]$	0.060	0.125	0.055
	Experimental rates	0.28 ± 0.08	0.98 ± 0.12	0.43 ± 0.06
0^+	$[K_\chi]$	0.096	0.216	0.134
	$[K_{\text{DD}}]$	0.011	0.021	0.020
2^+	$[K_\chi]$	0.547	1.052	0.872
	$[K_{\text{DD}}]$	0.192	0.410	0.330
$0^+ + 2^+$	$[K_\chi]$	0.643	1.268	1.006
	$[K_{\text{DD}}]$	0.203	0.431	0.350
	Experimental rates	0.35 ± 0.09	2.3 ± 0.3	1.68 ± 0.16

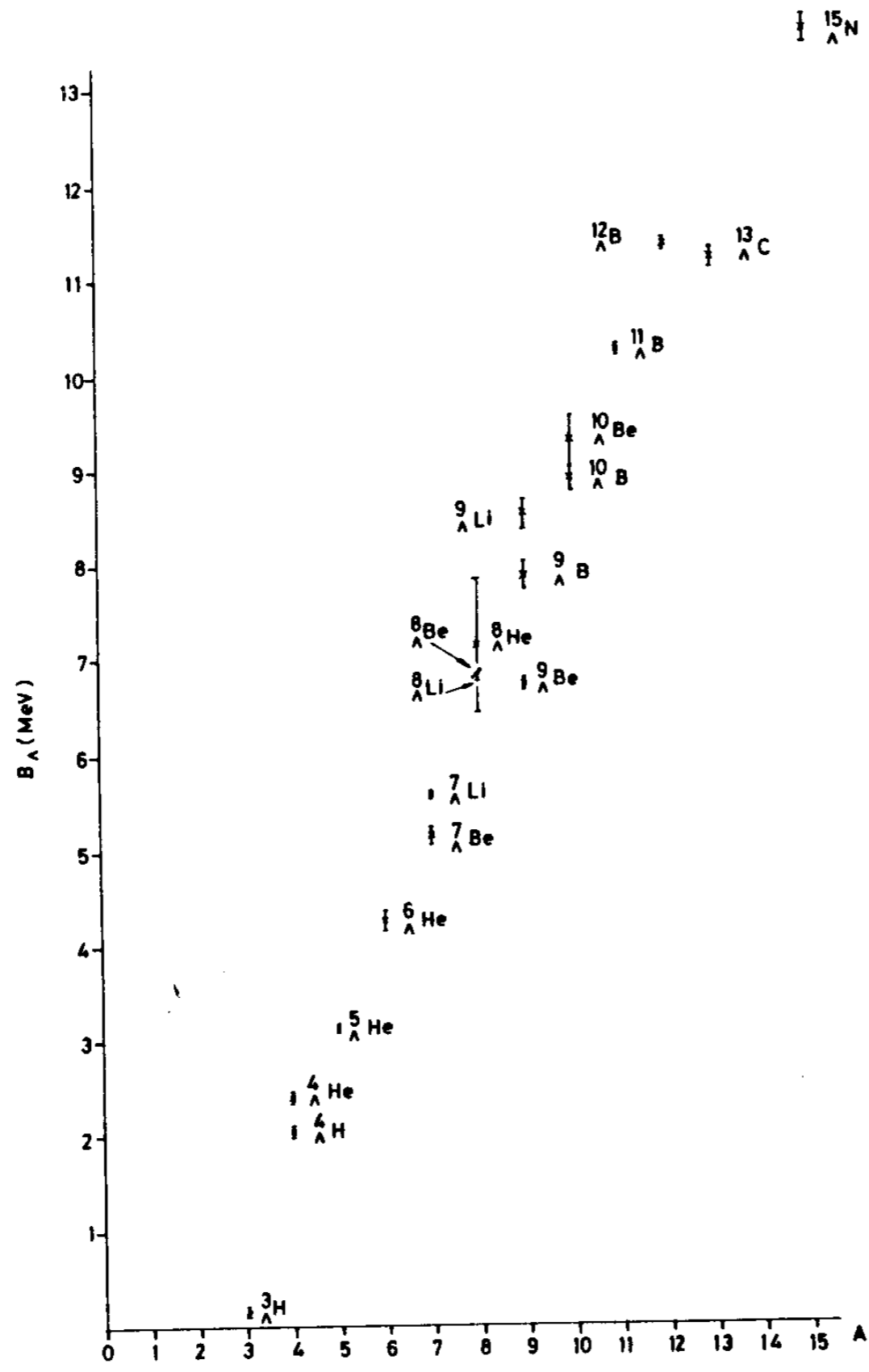
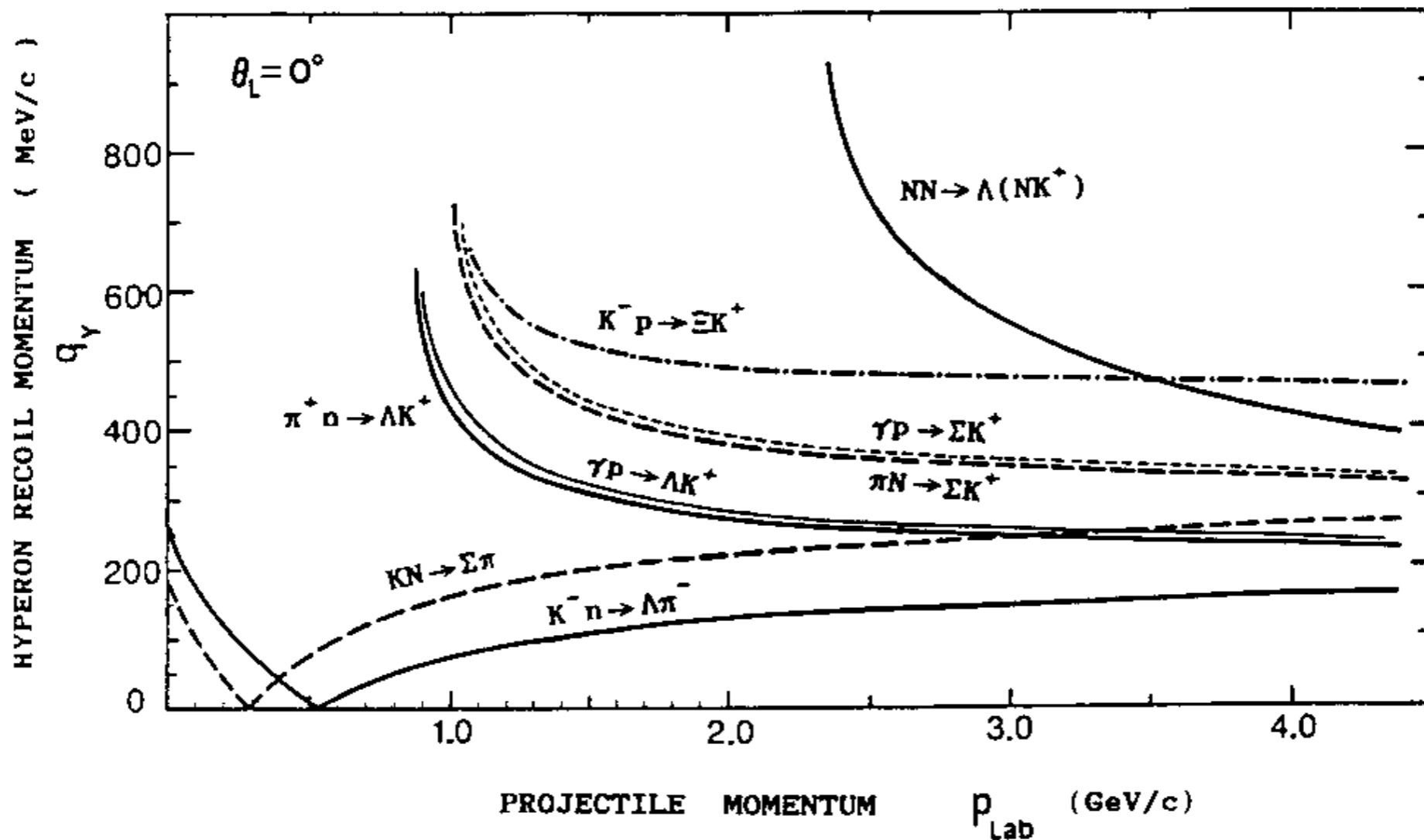


Fig. 10. Variation of the B_Λ values with the hypernuclear mass numbers.

In-flight (K^- , π^-) in 1970s

- ▶ Heidelberg-Saclay group
- ▶ “Magic momentum” - Recoilless condition
 - Population of Substitutional States: (p_n^{-1}, p_Λ)
 - Spectroscopic information on **Excited states**
 - Small Spin-Orbit splitting in Λ hypernuclei

Recoil Momentum of Hyperon



Data in the (K^-, π^-) reactions

► ${}^{16}_{\Lambda}\text{O}$

● $\delta_p = 0.8 \pm 0.7 \text{ MeV} \rightarrow V_{LS} = 4 \pm 2 \text{ MeV}$

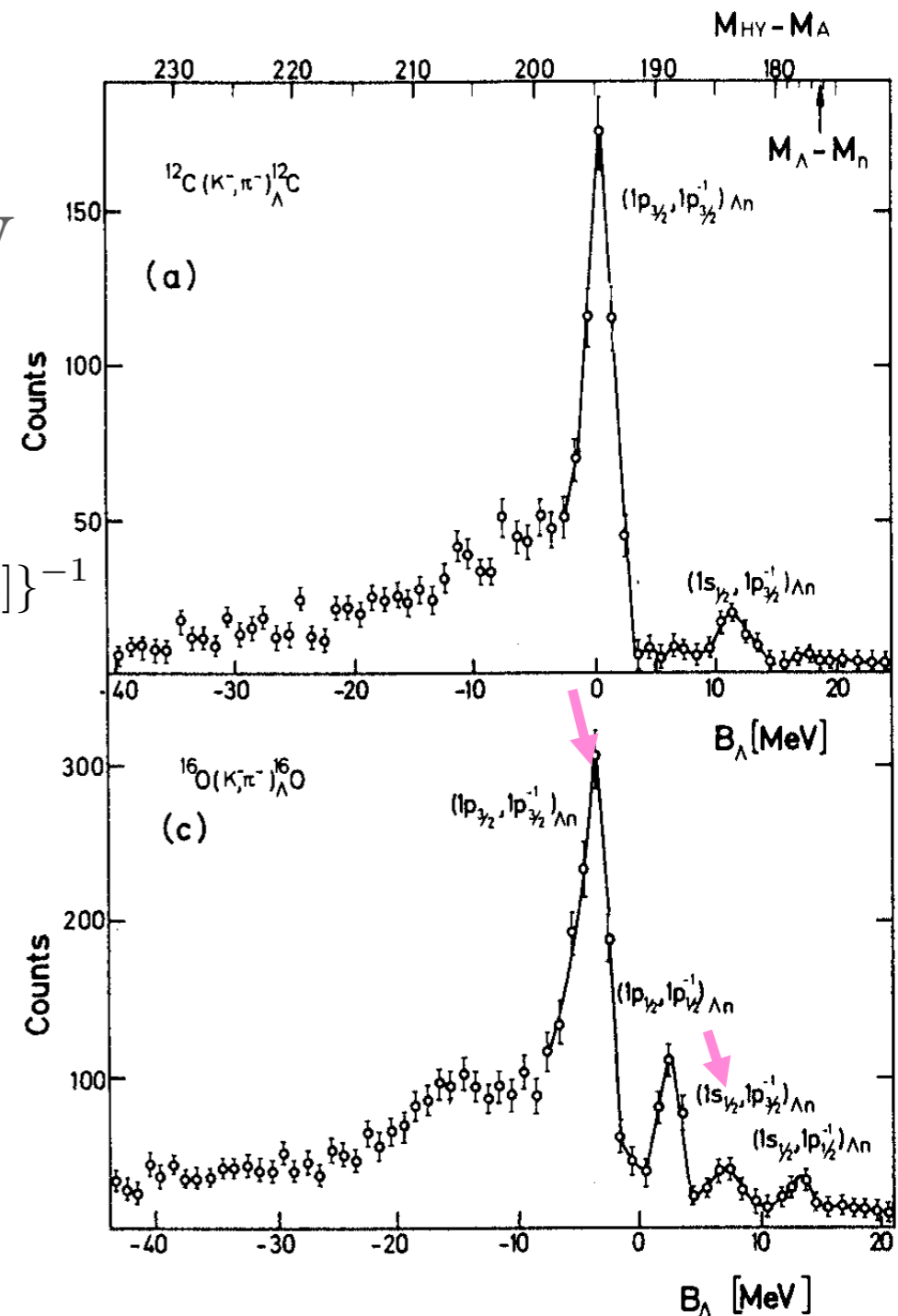
● $V_0 = 30 \text{ MeV}$

$$U_{\Lambda} = V_0^{\Lambda} f(r) + V_{LS}^{\Lambda} \left(\frac{\hbar}{m_{\pi} c} \right)^2 \frac{df(r)}{r dr} \vec{\ell} \cdot \vec{s}, f(r) = \{1 + \exp[(r - R)/a]\}^{-1}$$



For ordinary nuclei:

$V_0 \sim 50 \text{ MeV}, V_{LS} = 20 \text{ MeV}$




BNL-AGS & KEK-PS in 1980s ~

1990s

- ▶ Σ hypernuclei in (K^-, π^-)
 - narrow states \rightarrow not reconfirmed
 - one bound state ${}^4_{\Sigma}\text{He} \rightarrow$ confirmed
- ▶ Success of (π^+, K^+) Spectroscopy
- ▶ Success of Hypernuclear γ Spectroscopy
- ▶ H-particle search, Double- Λ hypernuclei

in the 21st century

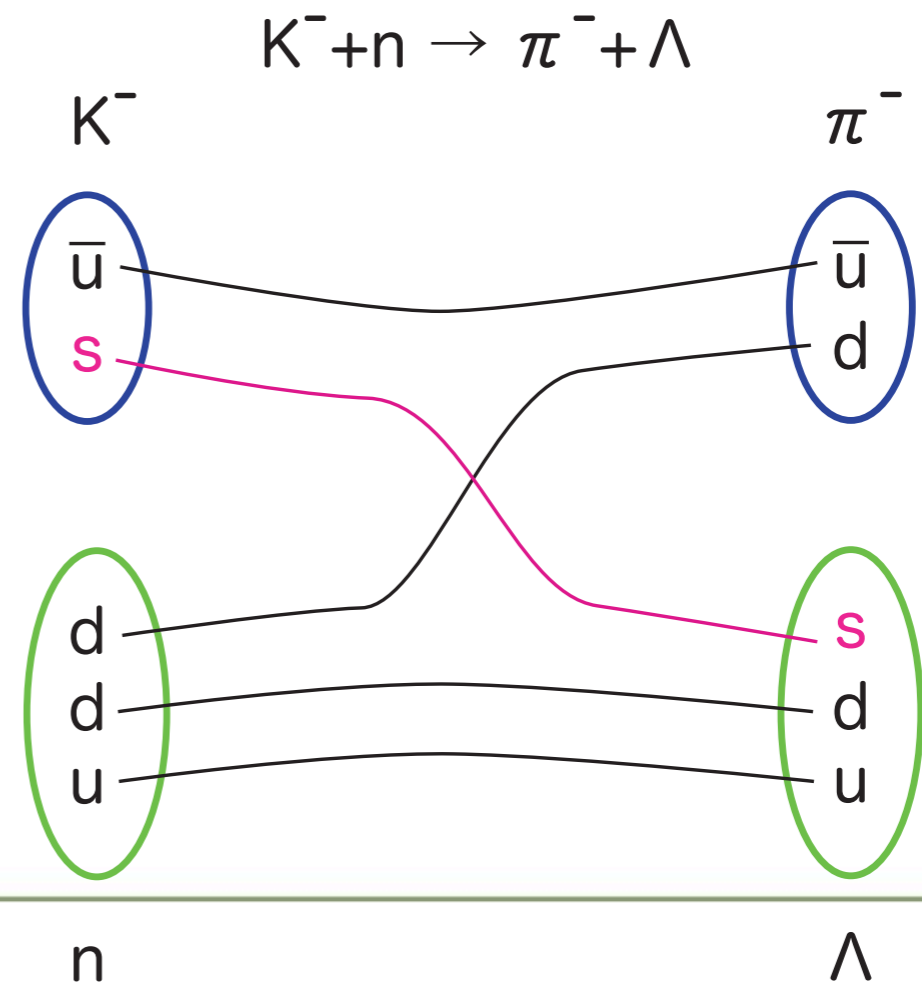
- ▶ $(e, e'K^+)$ at JLab
 - $\Delta E \sim 0.9 \text{ MeV}$  0.3 MeV
- ▶ $(K^-_{\text{stop}}, \pi^-)$ at DAFNE/FINUDA
 - $\Delta E \sim 0.7 \text{ MeV}$
- ▶ J-PARC, GSI, Mainz, ...

ハイパー核 の作り方

How to produce hypernuclei ?

► Strangeness exchange reactions: (K^- , π^-)

- Large cross section \sim mb/sr at 0 deg.
- K^- intensity limited

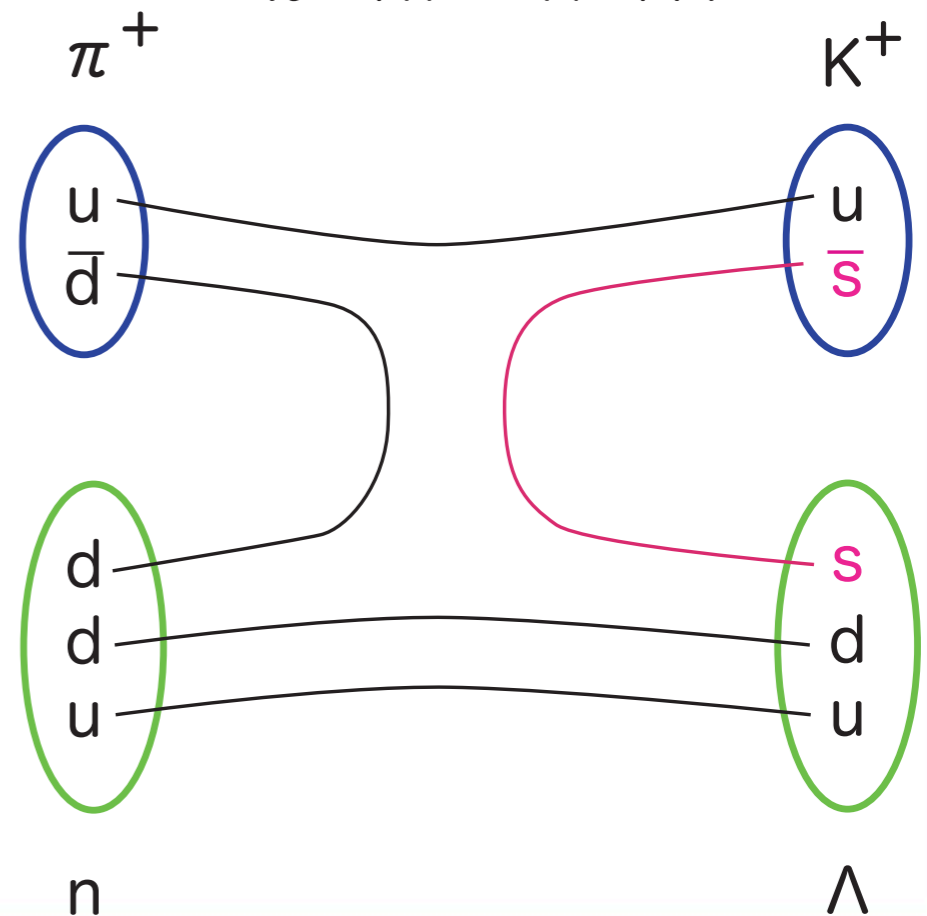


► Associated production: (π^+, K^+) , $(e, e'K^+)$

• Smaller cross sections: $\sim 10\mu\text{b}/\text{sr}$, $\sim 1\text{nb}/\text{sr}$

• High intensity beams: $>10^6 \pi^+$, $>10^{13} e^-$

$$\pi^+ + n \rightarrow K^+ + \Lambda$$

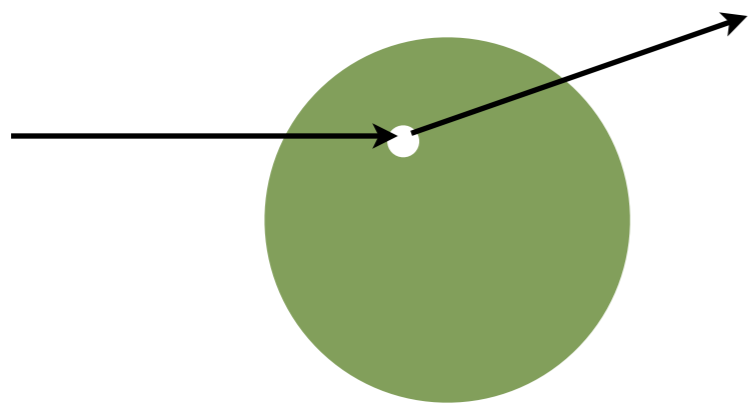


生成反応とその収量

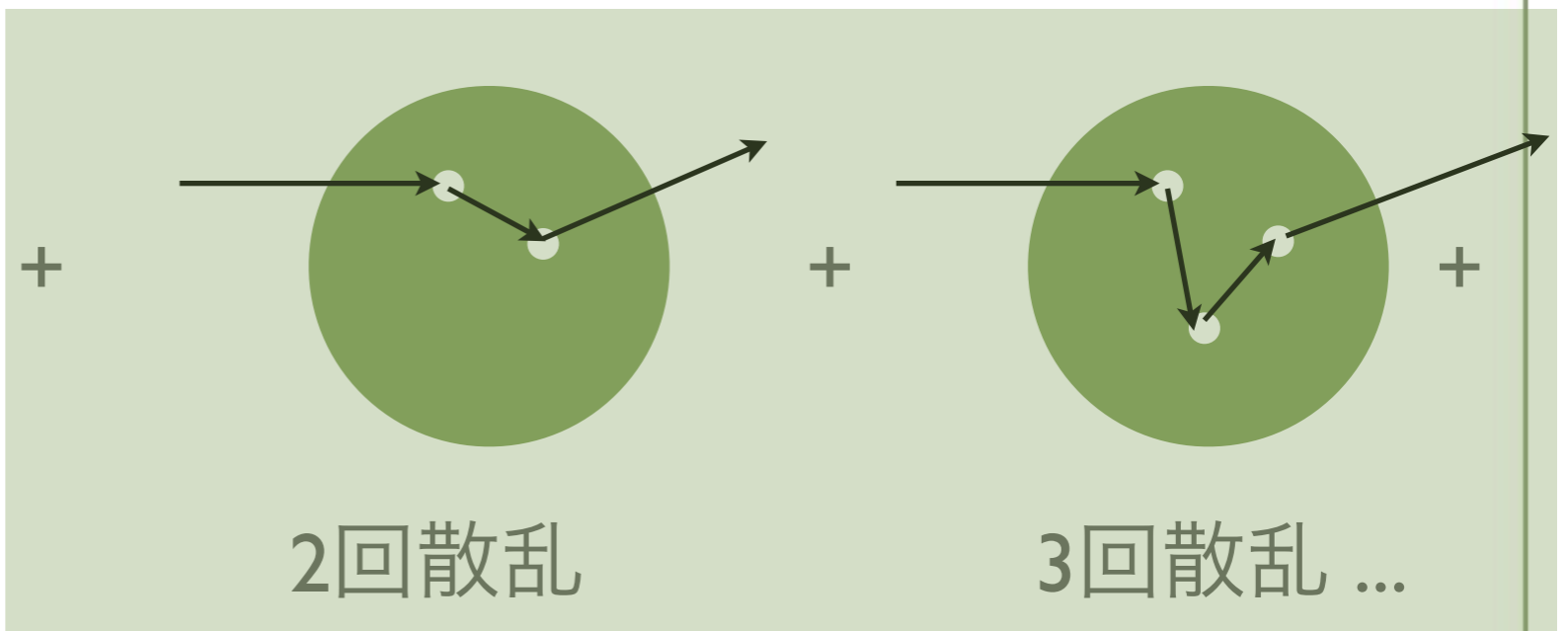
	(K ⁻ ,π ⁻)	(π ⁺ ,K ⁺)	(e,e'K ⁺)
p _{BEAM} (GeV/c)	~0.7	1.05	1.8
dσ/dΩ(μb/sr)	1000	10	10 ⁻³
I _{BEAM} (s ⁻¹)	10 ⁺⁵	10 ⁺⁶	>10 ⁺¹³
ΔΩ (msr)	20	100	20
n _x (g/cm ²)	3	3	0.1
ΔE (MeV)	3	2	0.2
Relative Yield	2	1	>3

反応機構

- ▶ DWIA (Distorted Wave Impulse Approximation)
 - ▶ Impulse Approx. : $p_{\text{inc}} \rightarrow \text{high}$, $\lambda = h/p \rightarrow \text{small} \ll 1 \text{ fm}$



1回散乱



2回散乱

3回散乱 ...

- ▶ 核内での遷移振幅 ~ 自由散乱の遷移振幅

- ▶ 1 + “2” → 3 + “4”

$$\left(\frac{d^2 \sigma_{fi}}{d\Omega_3 dE_3} \right)_{lab} = \frac{p_3 E_3}{(2\pi)^2 v_1} |T_{fi}|^2 \delta(\omega - E_1 + E_3)$$

$$T_{fi} = \langle \chi_3^{(-)} | \langle f | \sum_j t_j | i \rangle | \chi_1^{(+)} \rangle$$

- ▶ t_j : 素過程反応

- ▶ $\chi_3^{(-)}$, $\chi_1^{(+)}$: 平面波(PWIA)、or 歪曲波(DWIA)

Distorted Wave

- ▶ Eikonal Approximation: $E \gg U, pR \gg 1$

$$\chi^{(+)}(b, z) = e^{ipz} \phi(b, z)$$

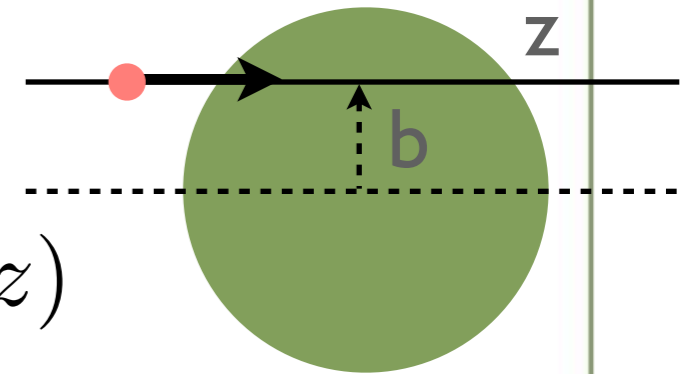
$$[-\nabla^2 + \mu^2 - \omega^2] \chi^{(+)}(b, z) = -2\omega U \chi^{(+)}(b, z)$$

$$\phi = \exp\left\{-iv^{-1} \int_{-\infty}^z U(b, z') dz'\right\}$$

$$2\omega U(b, z) = p\sigma^{tot} \rho(b, z)$$

$$\chi_3^{(-)*}(\mathbf{r}) \chi_1^{(+)}(\mathbf{r}) = \exp\left\{i\mathbf{q} \cdot \mathbf{r} - \frac{1}{2} \sigma_{eff} \int_{-\infty}^{\infty} \rho(b, z') dz'\right\}$$

$$\text{Mean free path} = 1/\rho\sigma = 1/(4 \text{ fm}^2)(0.15 \text{ fm}^{-3}) = 1.6 \text{ fm}, \quad \sigma = 40 \text{ mb}$$



→核表面での反応が支配的

Effective nucleon number

- ▶ 素過程($1+2 \rightarrow 3+4$)での微分断面積を使う

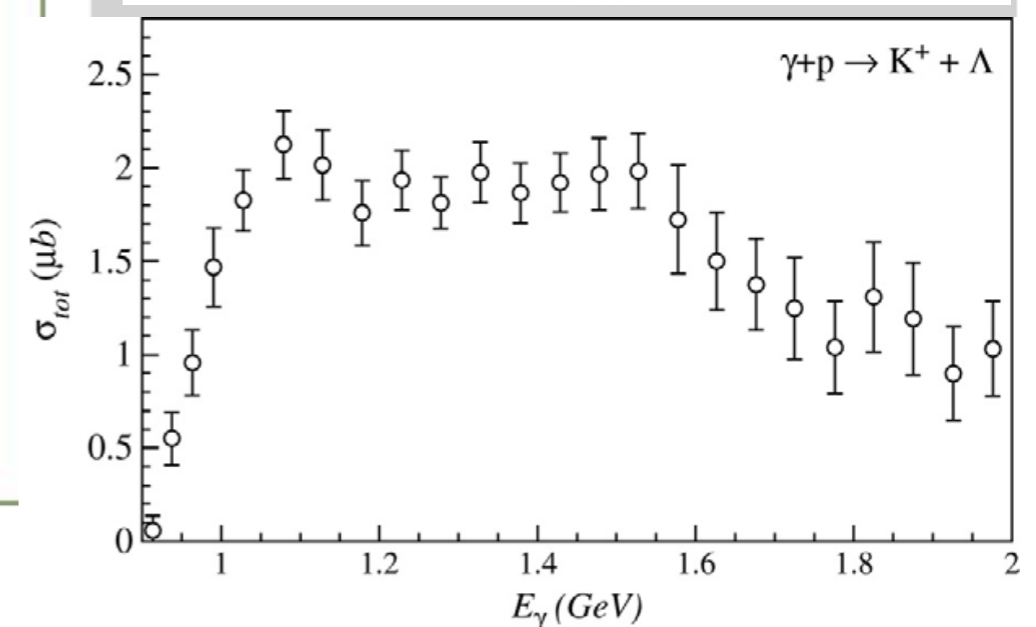
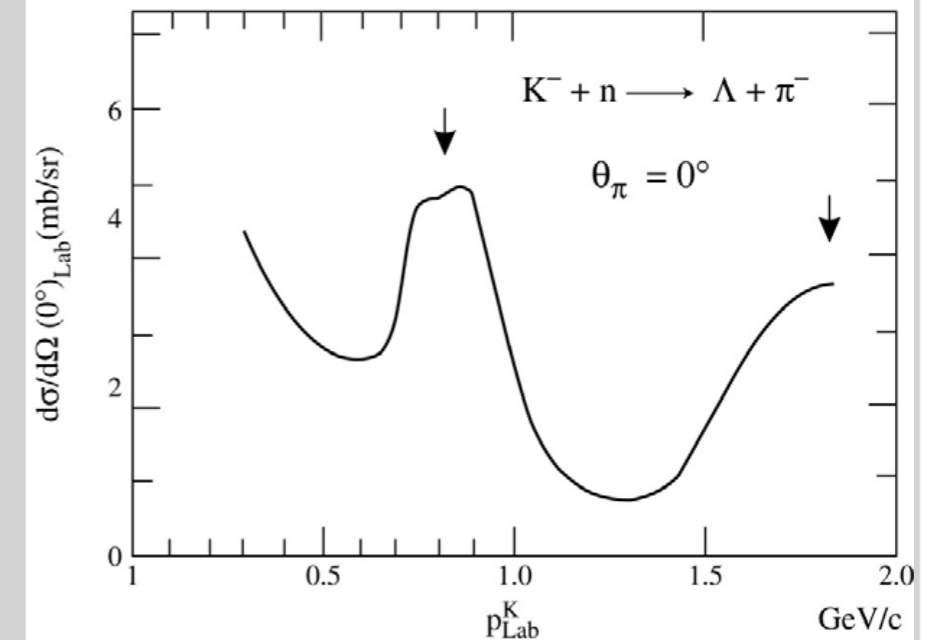
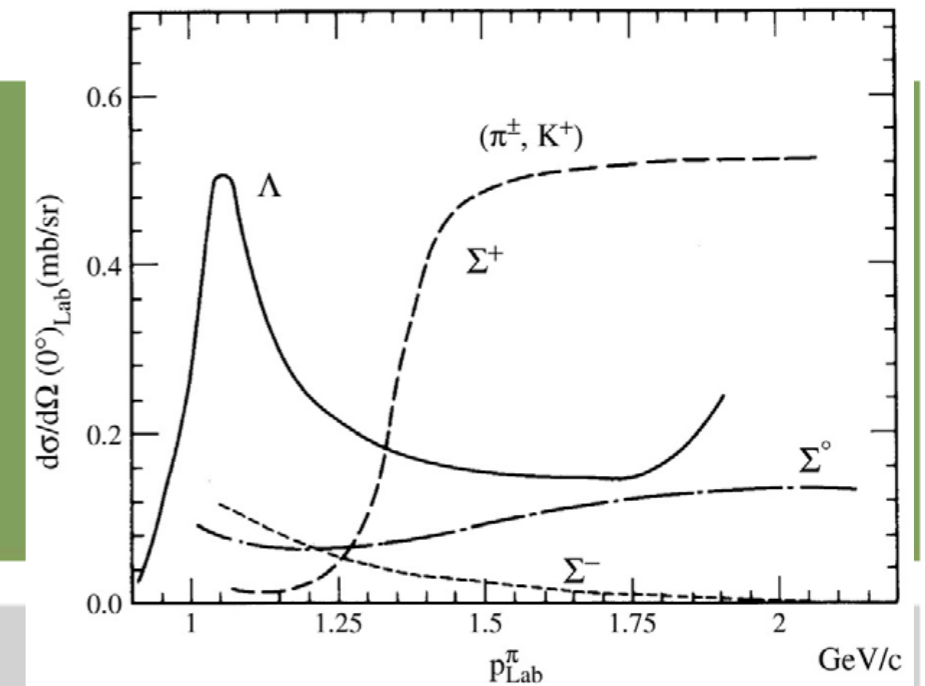
$$\left(\frac{d^2 \sigma_{fi}}{d\Omega_3 dE_3} \right)_{lab} = \beta \left(\frac{d\sigma}{d\Omega_3} \right)_{lab} N_{eff}(\theta_{lab}; i \rightarrow f) \delta(\omega + E_3 - E_1)$$

$$\beta = \left(1 + \frac{E_3^{(0)} p_3^{(0)} - p_1 \cos \theta_{lab}}{E_4^{(0)} p_3^{(0)}} \right) \frac{p_3 E_3}{p_3^{(0)} E_3^{(0)}}$$

2 体系((0))から多体系への運動学因子

入射エネルギー

- ▶ 1.05 GeV/c ; (π^+ , K^+) for Λ
- ▶ 0.7-0.8 GeV/c ; (K^- , π^-) for Λ
- ▶ 1.2 - 1.8 GeV ; for ($e, e'K^+$) for Λ



Hypernuclear Mass

- ▶ In-flight reactions: (π^+, K^+) , (K^-, π^-)



- ▶ $M_{HY}^2 = (E_\pi + M_A - E_K)^2 - (\mathbf{p}_\pi - \mathbf{p}_K)^2$; missing mass

- ▶ $M_{HY} - M_A = B_n - B_\Lambda + M_\Lambda - M_n$

- ▶ $-B_\Lambda = M_{HY} - (M_A + B_n - M_n + M_\Lambda)$

- ▶ Need incident momentum & out-going momentum → Two Spectrometers

▶ Stopped K^- reaction: (K^-_{stop}, π^-)



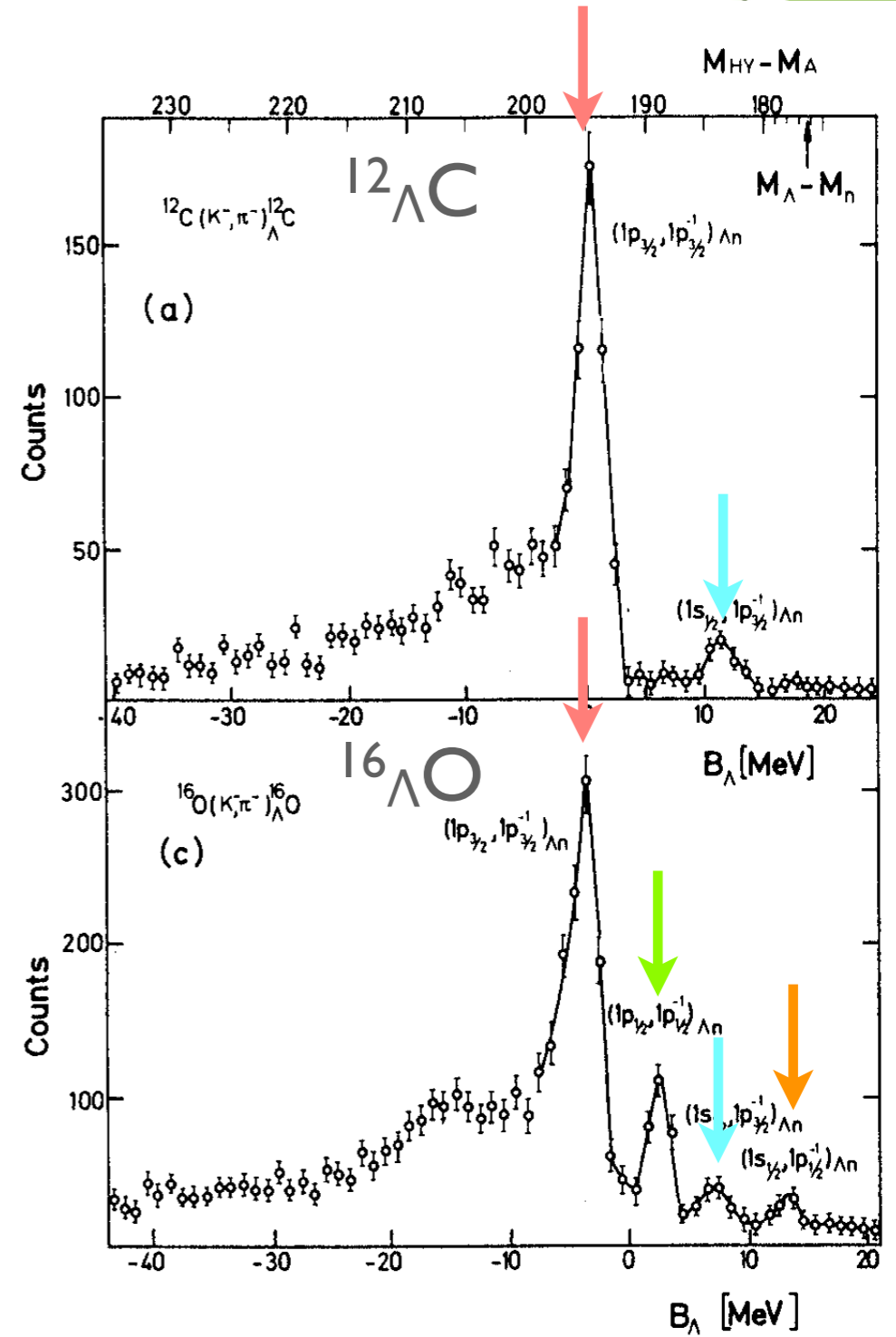
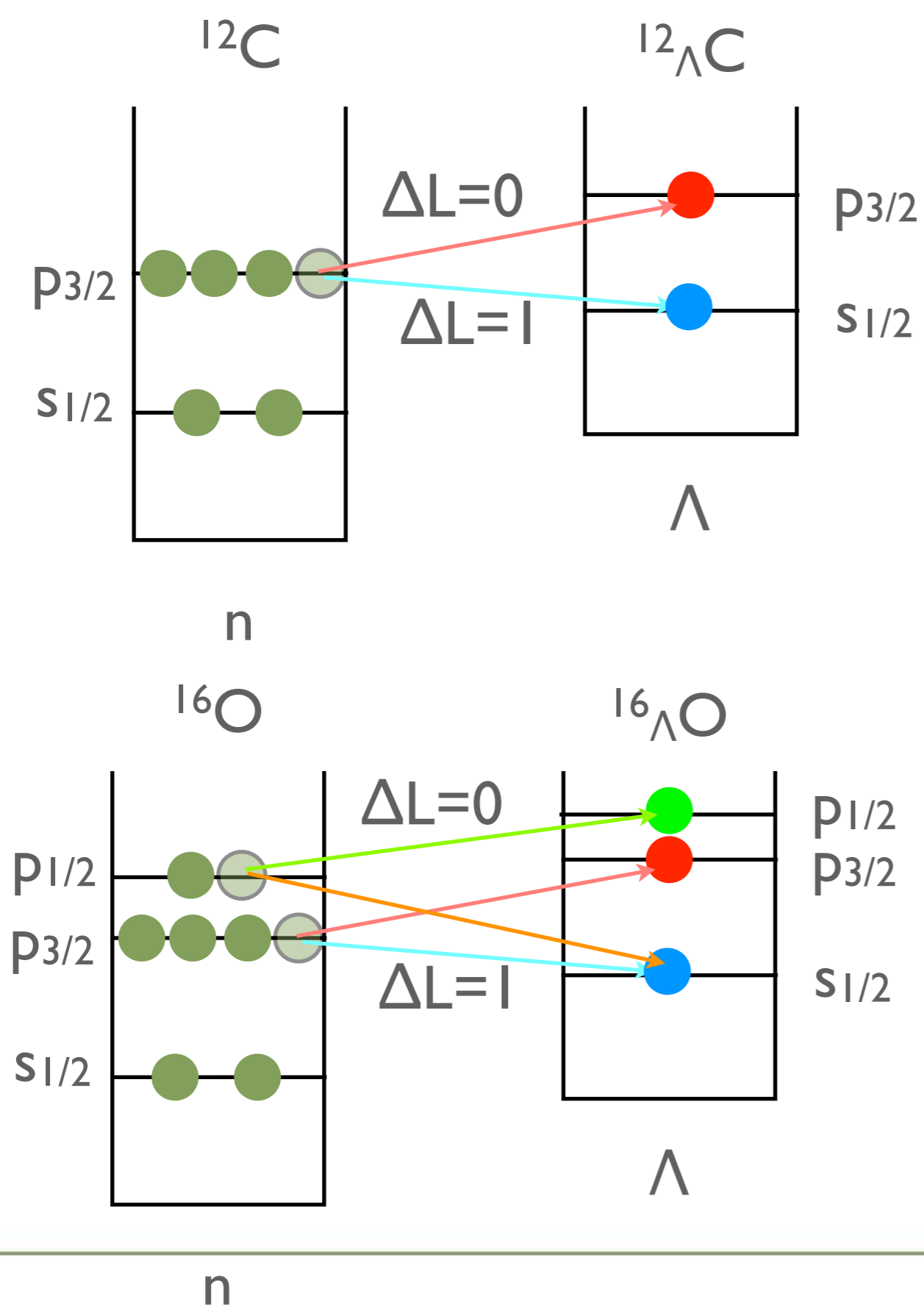
▶ $M_{HY}^2 = (M_K + M_A - E_{\pi})^2 - (p_{\pi})^2$; missing mass

▶ $M_{HY} - M_A = B_n - B_{\Lambda} + M_{\Lambda} - M_n$

▶ $-B_{\Lambda} = M_{HY} - (M_A + B_n - M_n + M_{\Lambda})$

▶ Need out-going π^- momentum only \rightarrow One Spectrometer

(K⁻,π⁻) in-flight



Spectroscopic Information

- ▶ Mass → Binding Energy
 - ▶ Missing Mass measurement in in-flight reactions
 - ▶ Weak decays of Hyperfragments
- ▶ Spin Assignment
 - ▶ Weak Decay
 - ▶ Gamma Decay

$^{208}\text{Pb}(e,e'p)$

- ▶ $zA_N(e,e'p) z-1A'_N$: nucleon hole state
- ▶ Deep Hole States \rightarrow Large Spreading Width $>$ a few MeV

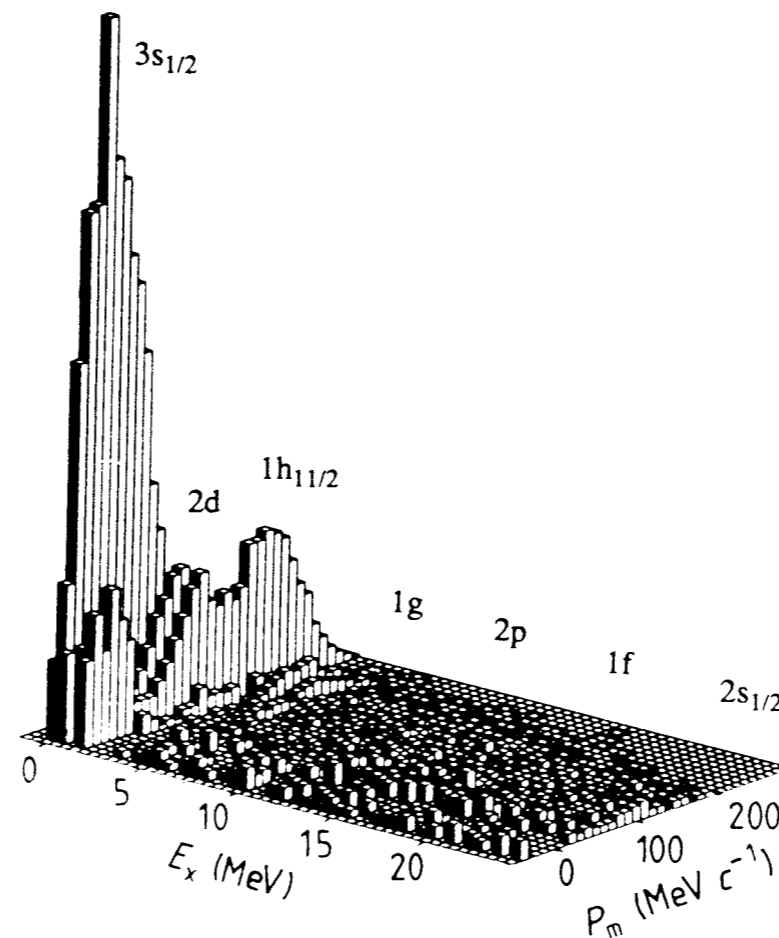
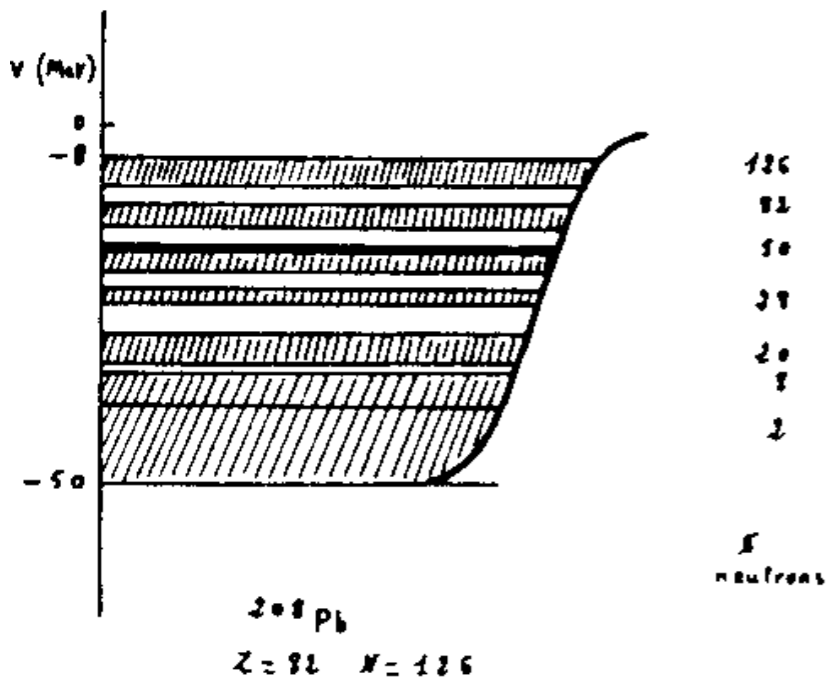


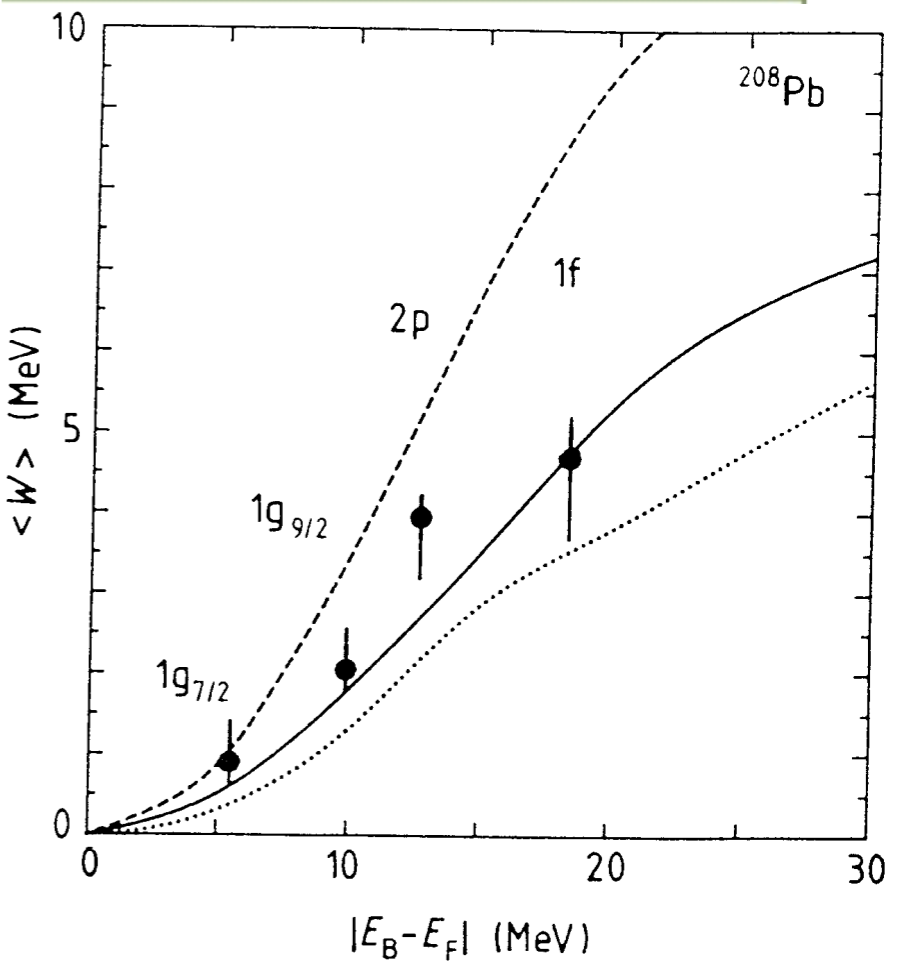
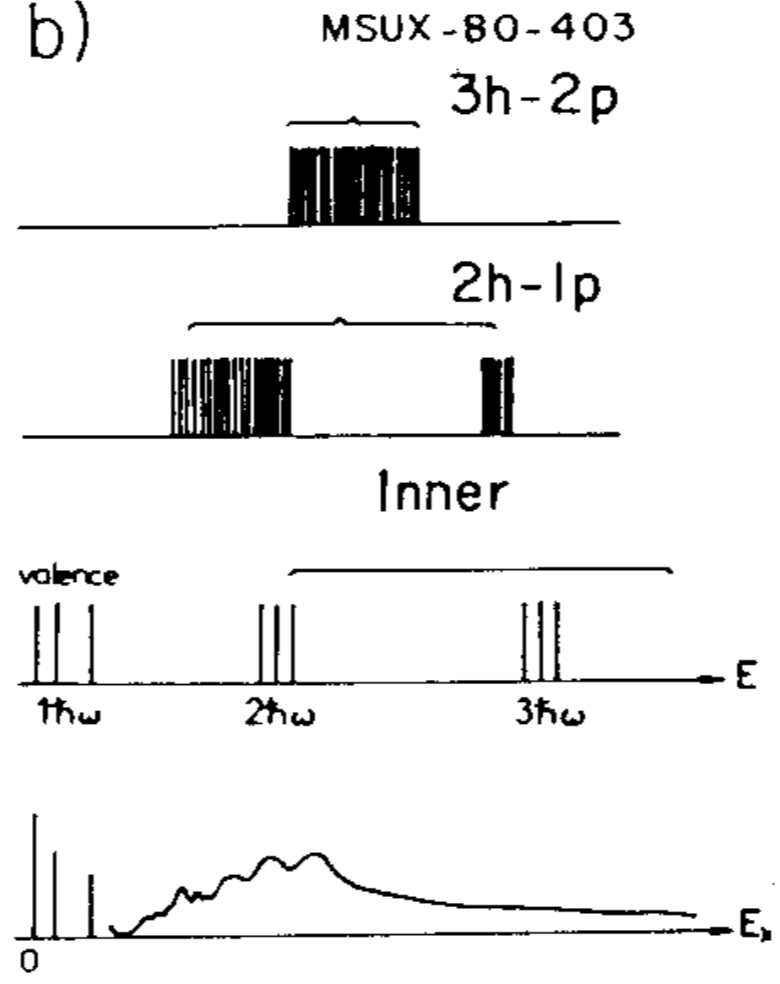
Figure 32. Experiment
 $^{208}\text{Pb}(e,e'p)^{207}\text{Tl}$.



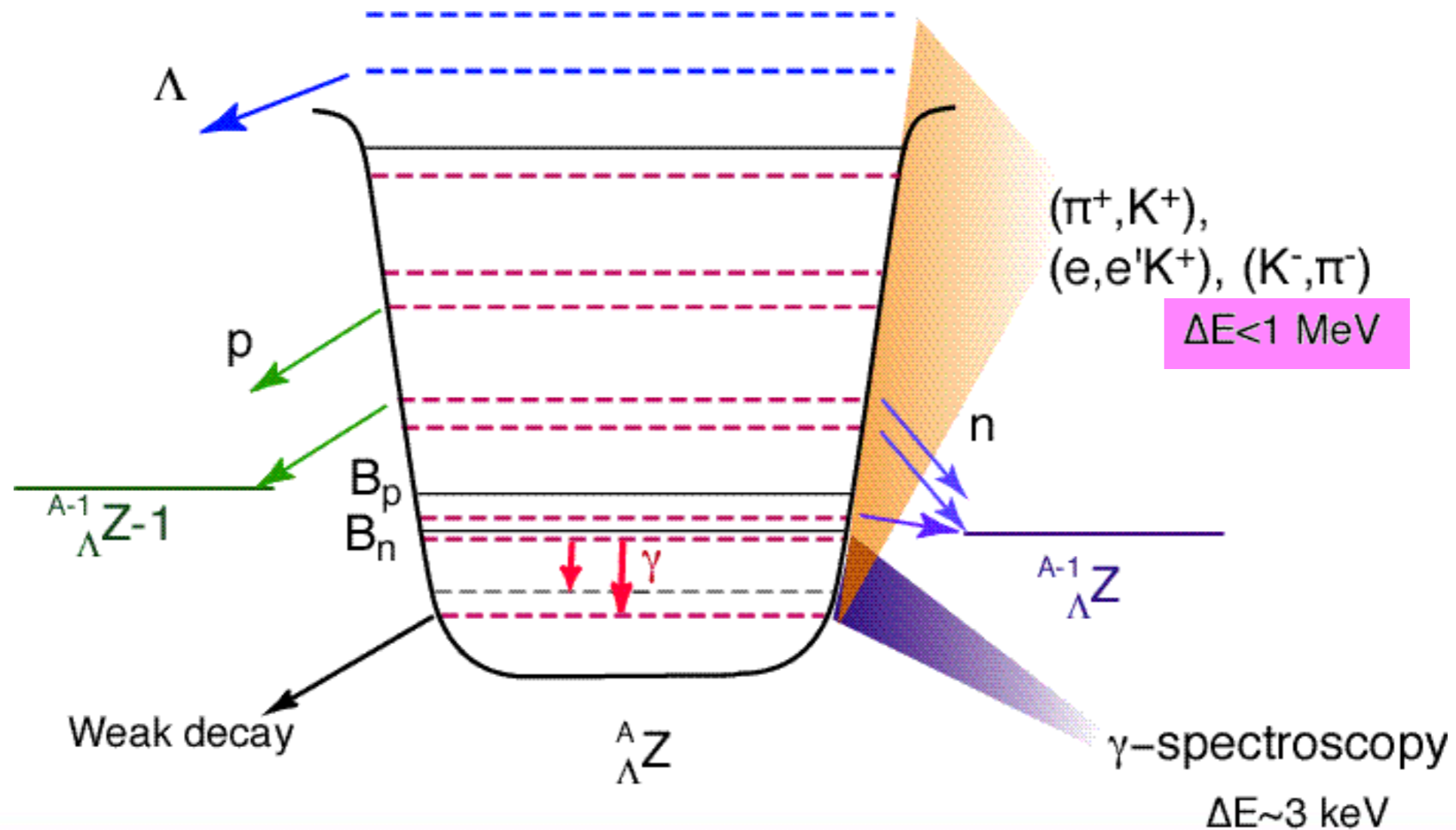
a)



b)



Excited levels of Λ -hypernuclei



Monochromatic Peak

► Mesonic decay of Hyperfragments

► ${}^4_{\Lambda}\text{H}$

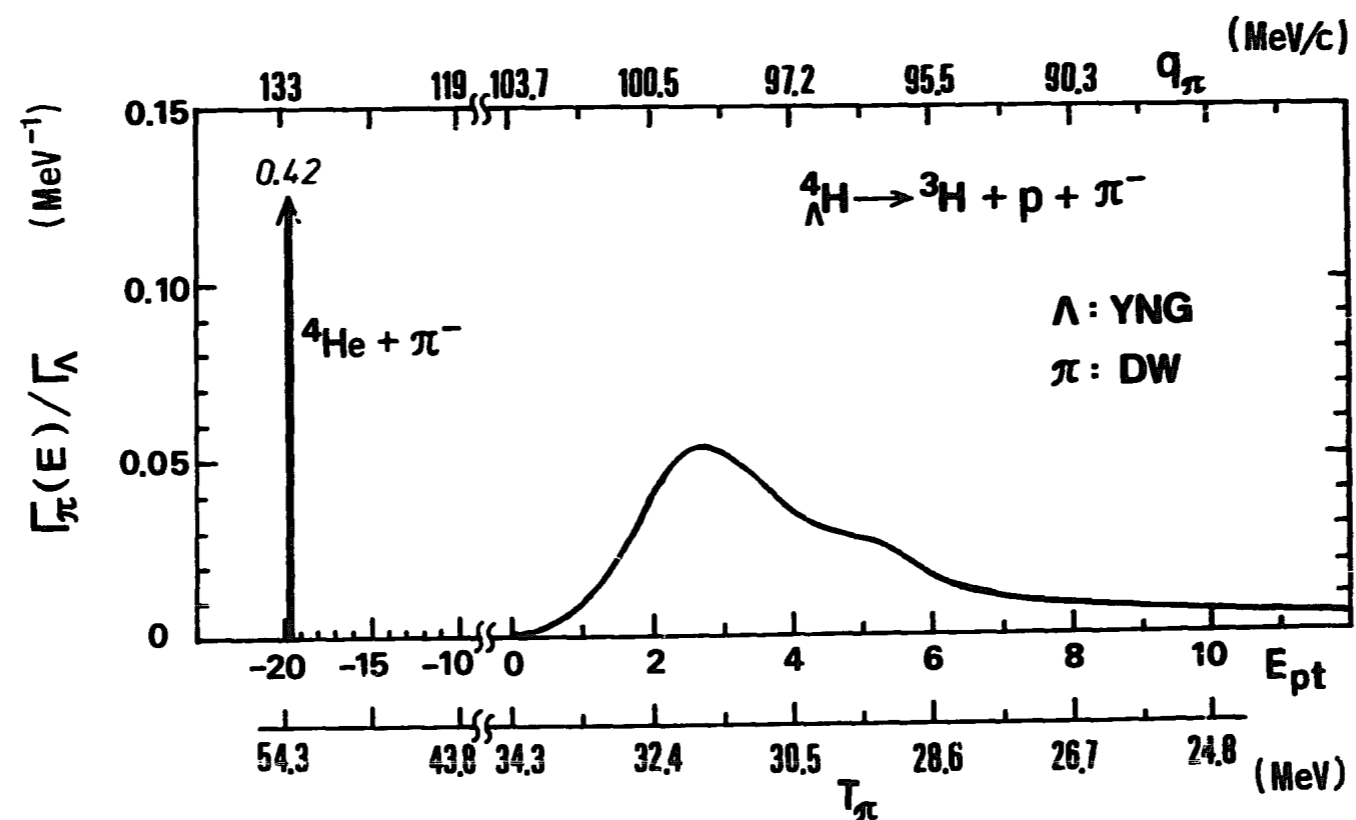


Fig. 9. The theoretical π^- decay spectrum $\Gamma_{\pi^-}({}^4_{\Lambda}\text{H})/\Gamma_{\Lambda}$ as a function of the proton- ${}^3\text{H}$ relative energy E_{pt} .

Quasi-monochromatic

- ${}^5_{\Lambda}\text{He} \rightarrow \pi^- + p + {}^4\text{He}$; $p_{\pi} = 99.9 \text{ MeV}/c$, $\Delta p \sim 1.4 \text{ MeV}/c$

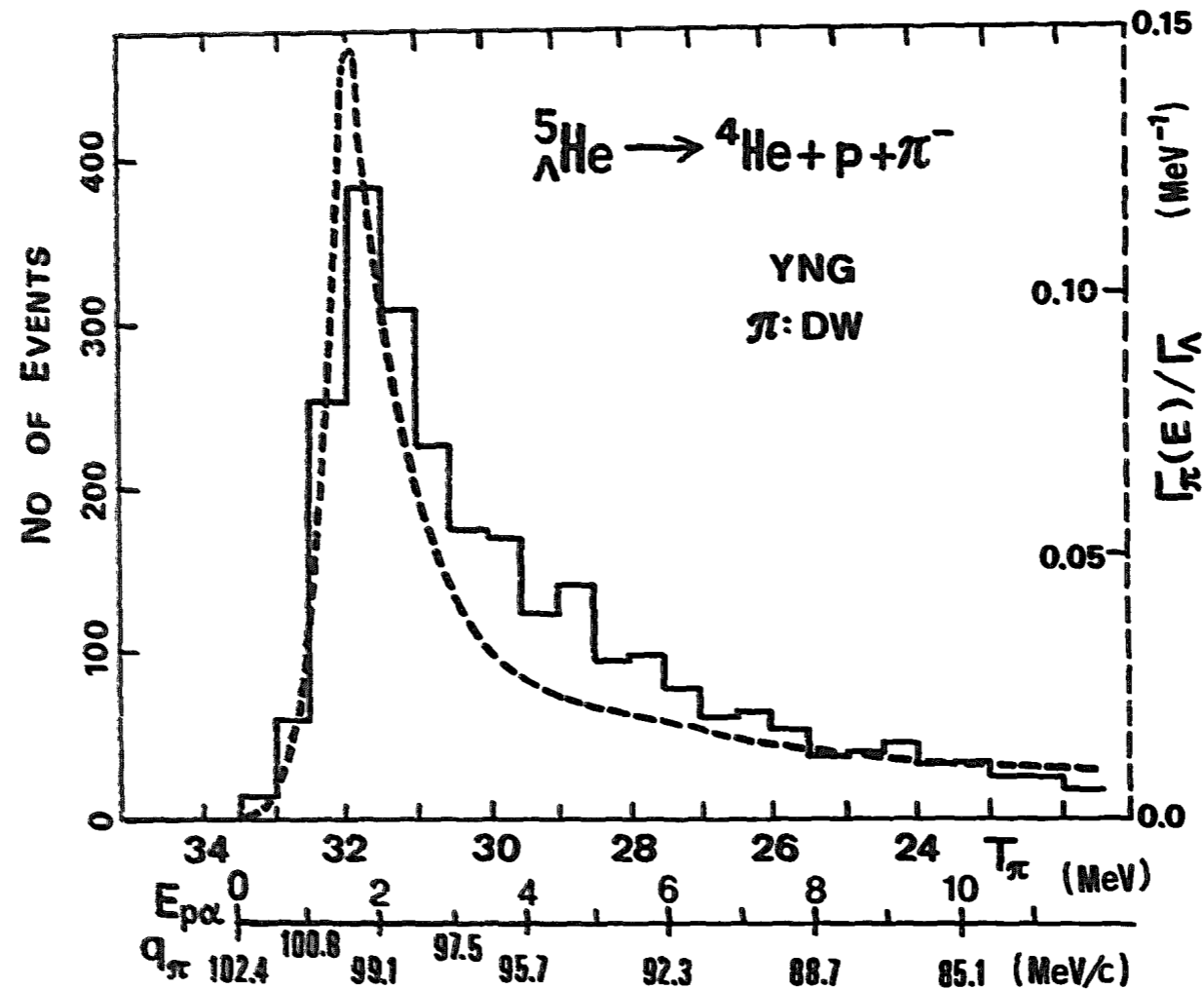


Fig. 4. The theoretical π^- decay spectrum $\Gamma_{\pi}({}^5_{\Lambda}\text{He})/\Gamma_1$ with YNG drawn as a function of the $p\alpha$ relative energy $E_{p\alpha}$ is compared with the observed π^- decay spectrum taken in the emulsion experiment^{18,33}). The calculated π^- decay rate is compared with the experimental values^{12,20}) in table 1 and fig. 5.

Mesonic Decay Rate

- ▶ $\Gamma_{\pi}/\Gamma_{\Lambda} \sim 0.4 - 0.6$ for light fragments

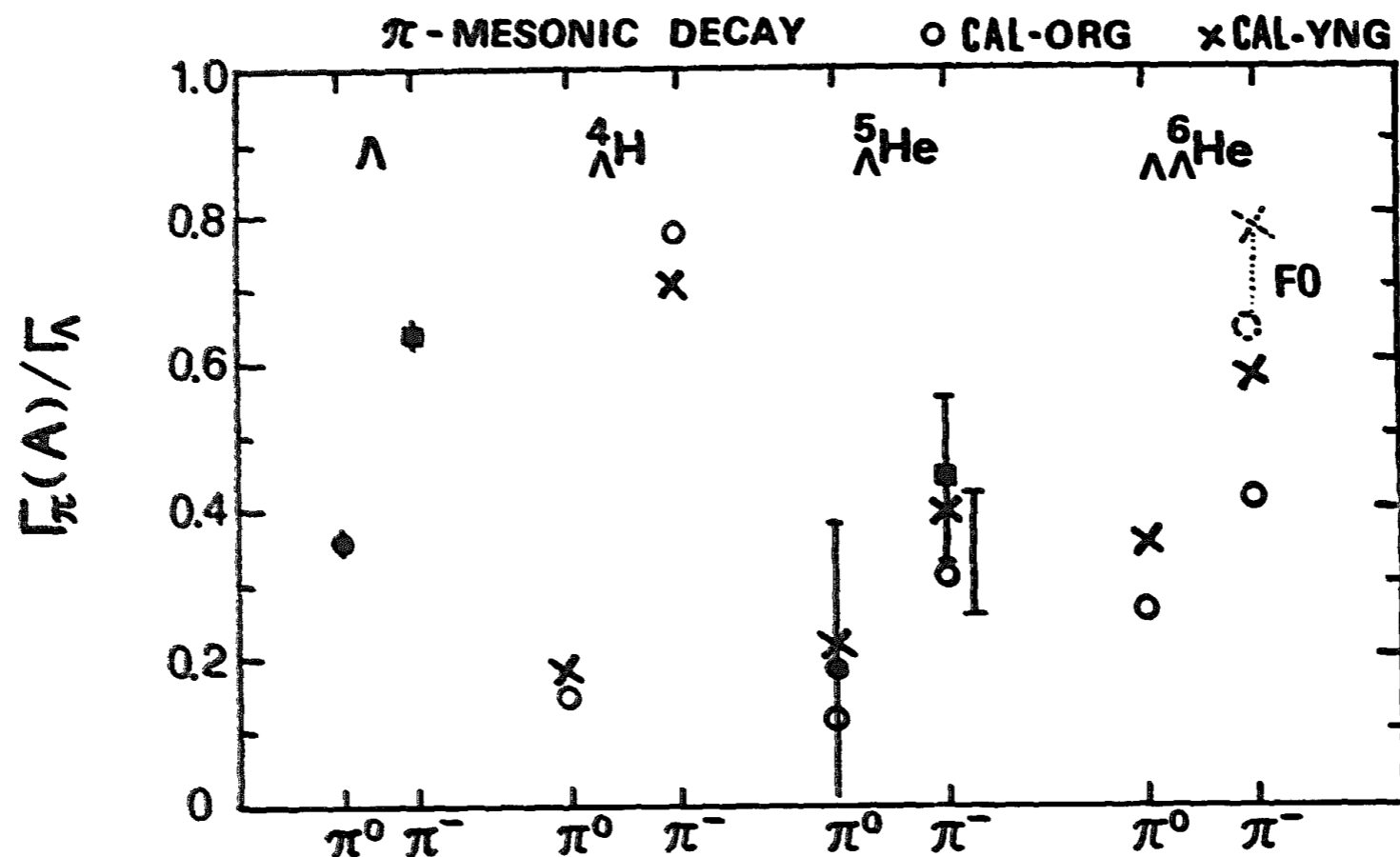
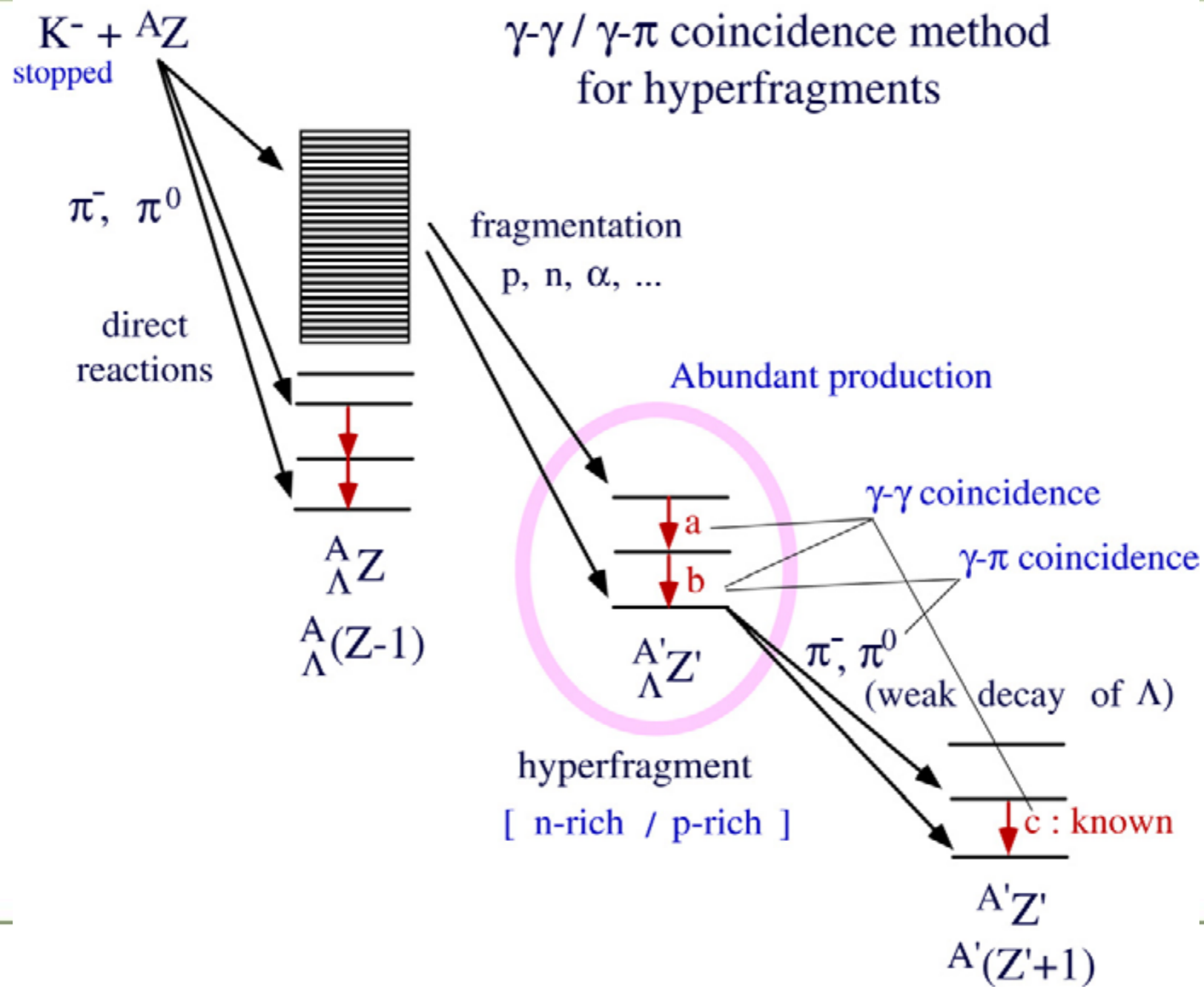


Fig. 5. Summary of the theoretical π -decay rates in units of Γ_{Λ} . The open circle and the cross correspond to ORG and YNG, respectively. The π^- decay rates of ${}^6_{\Lambda\Lambda}\text{He}$ in the case of the FO .1.1 interaction are also shown. The experimental values for ${}^5_{\Lambda}\text{He}$ are taken from refs. ^{12,20}).

γ -ray spectroscopy



▶ Charged-particle Spectroscopy

- ▶ magnetic spectrometer: $\Delta p/p > 10^{-4}$

- ▶ $\Delta E = 0.3 \sim 2 \text{ MeV}$

- ▶ Absolute Energy Level

- ▶ selectivity for produced states

▶ Gamma-ray Spectroscopy: Low detection efficiency

- ▶ NaI($\sim 100 \text{ keV}$), Ge($2\text{-}3 \text{ keV}$): **Excellent Resolution**

- ▶ Energy level separation

- ▶ Low-lying states below particle-emission threshold

Sticking probabilities

$$S_k(q; n_N l_N, n_Y l_Y) = \left| \langle \phi_{n_Y l_Y}^{HO}(r) | j_k(qr) | \phi_{n_N l_N}^{HO}(r) \rangle \right|^2$$

Production, Structure and Decay of Hypernuclei

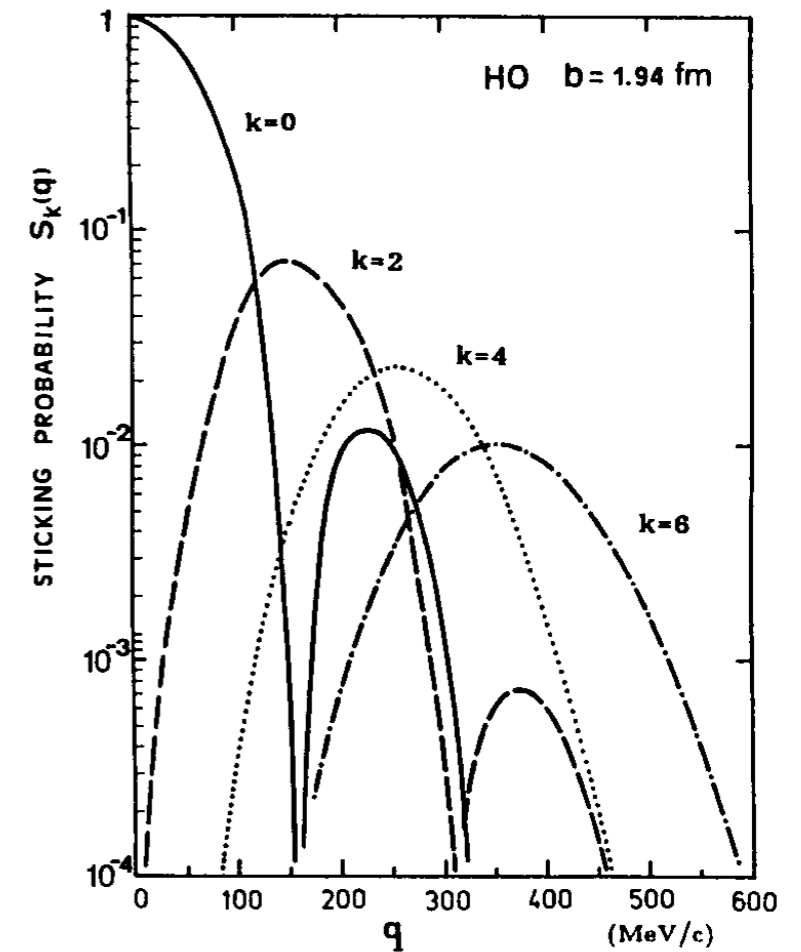
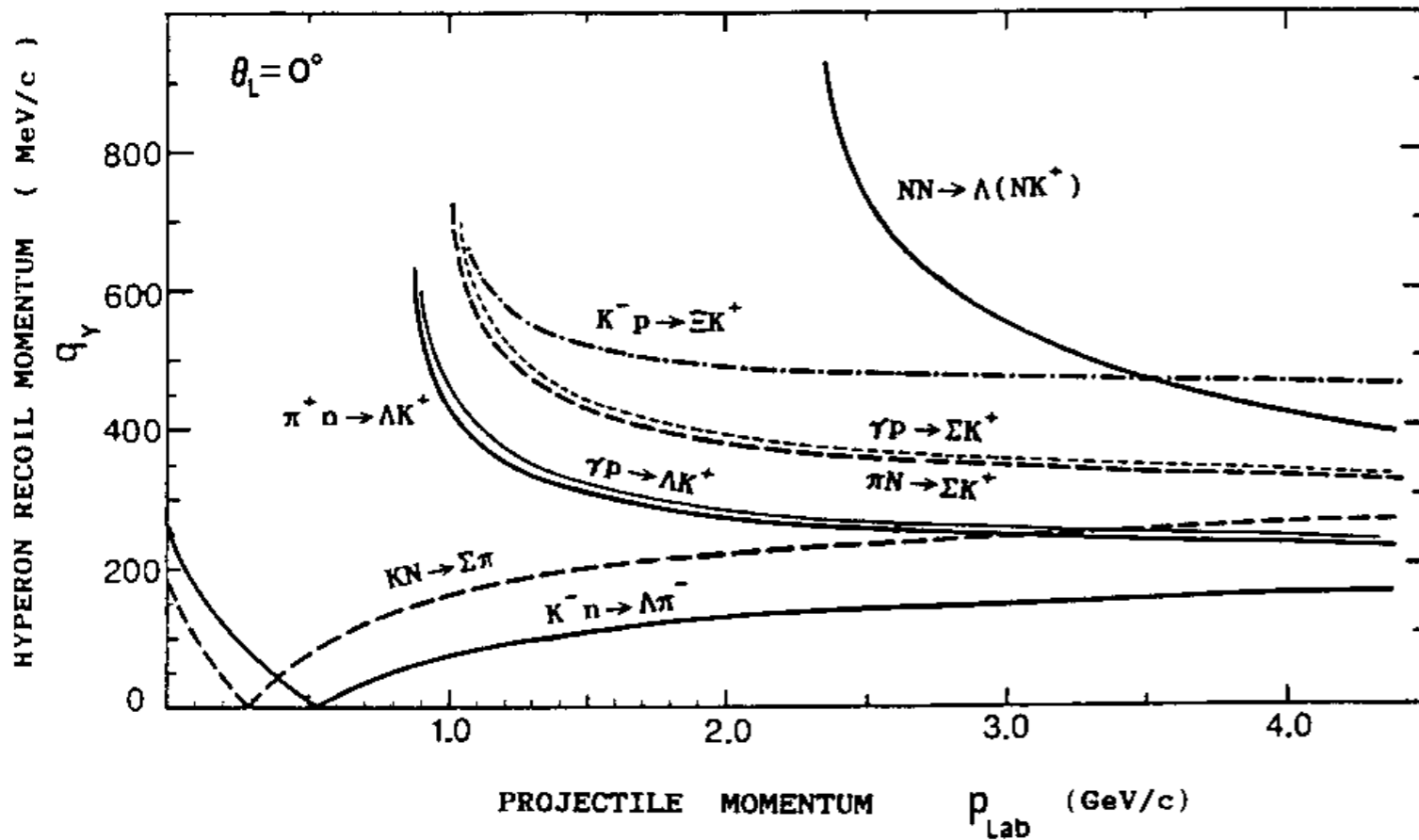


Fig. 2.4. The sticking probabilities $S_k(q; (0f)_N, (0f)_Y)$ of Eq. (2.2) as a function of q . The harmonic oscillator size parameter $b = 1.94$ fm is used.

► (K^-, π^-) : $q < 100$ MeV/c $\rightarrow \Delta \ell = 0$ dominant

Angular Distributions

- ▶ $\Delta l = 0$
 - ▶ $s_N \rightarrow s_\Lambda$
 - ▶ $p^{1/2}_N \rightarrow p^{1/2}_\Lambda$
- ▶ $\Delta l = 1$
 - ▶ $p^{3/2}_N \rightarrow s^{1/2}_\Lambda$
- ▶ $\Delta l = 2$
 - ▶ $p^{1/2}_N \rightarrow p^{3/2}_\Lambda$

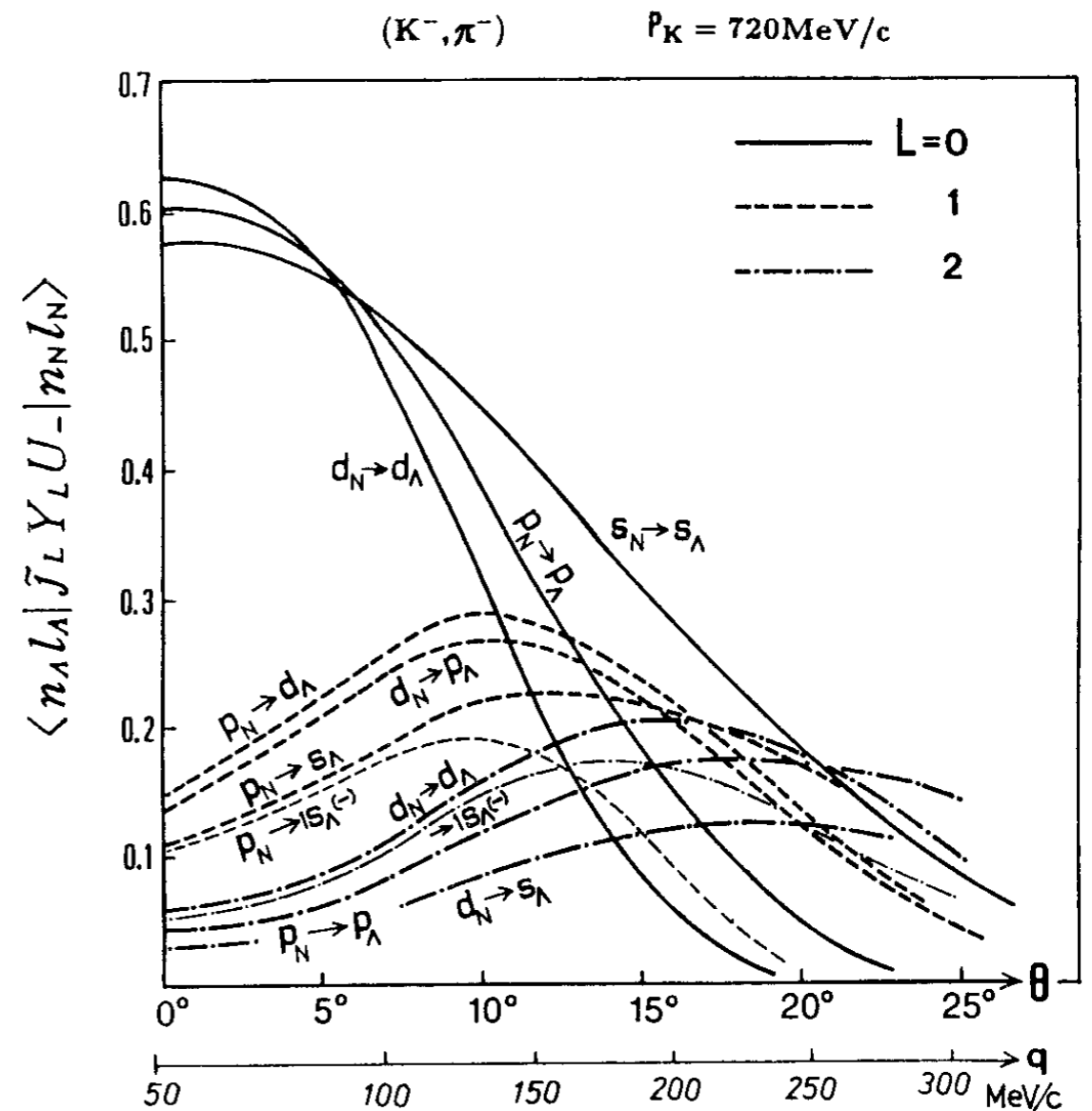
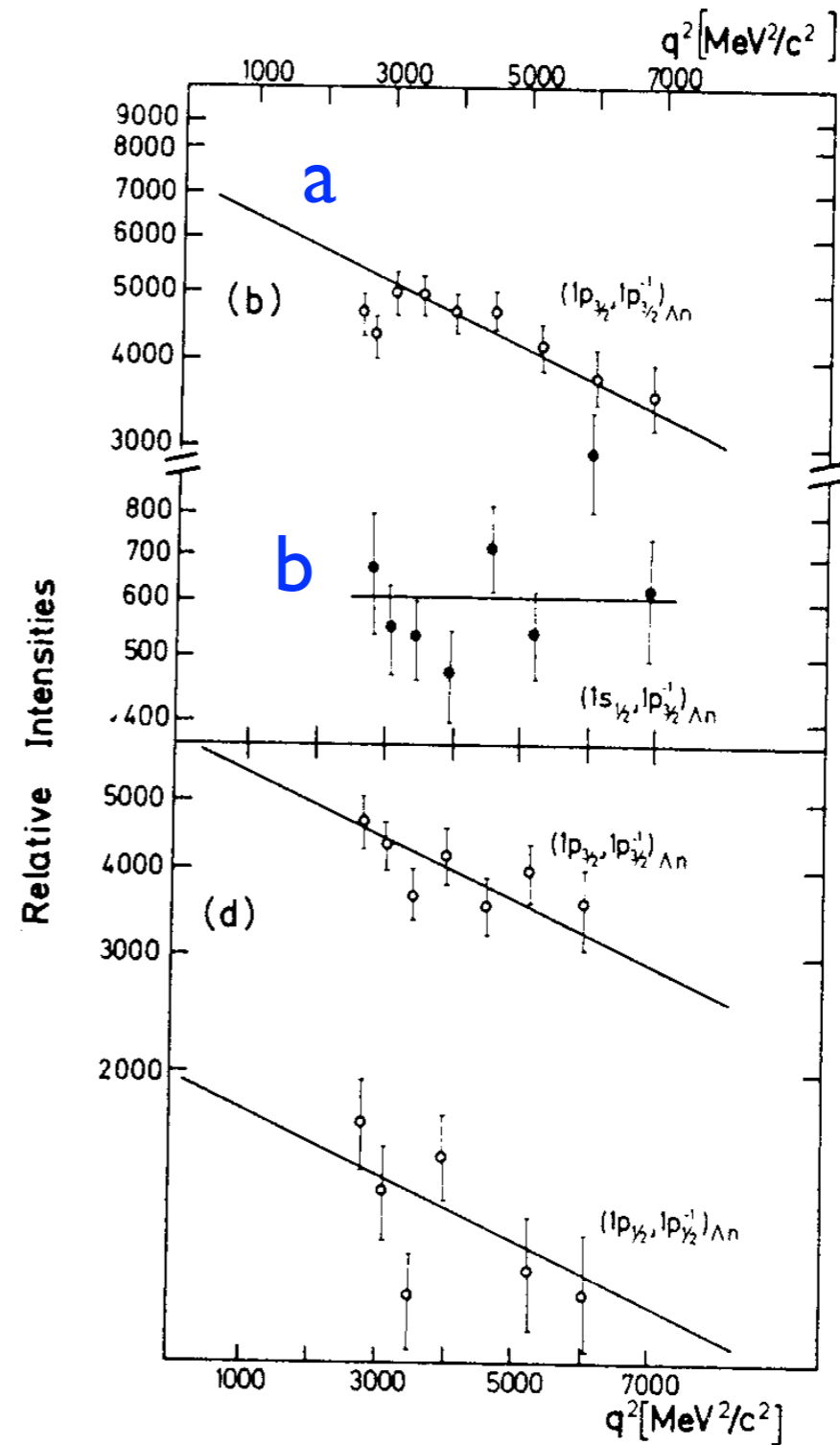
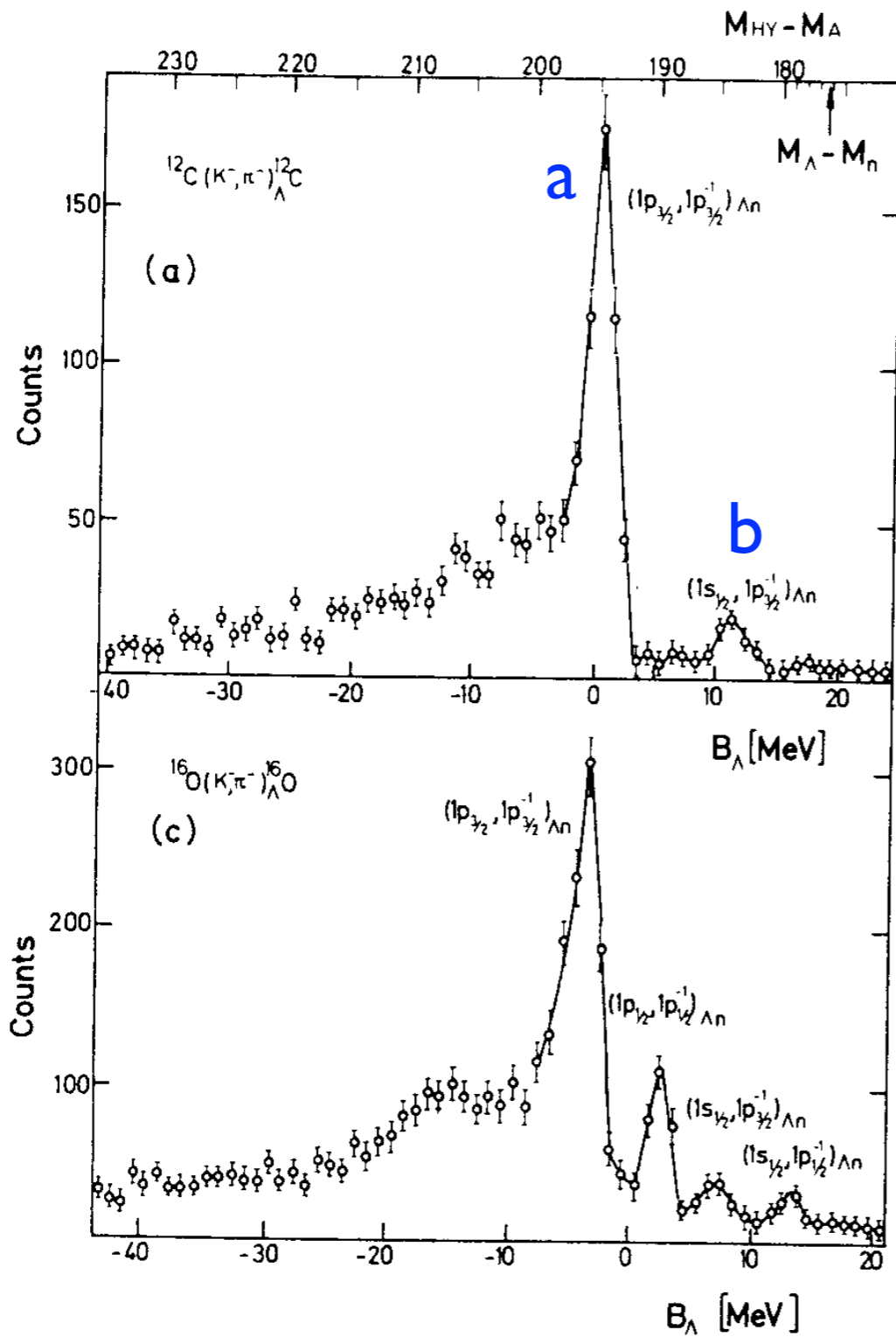


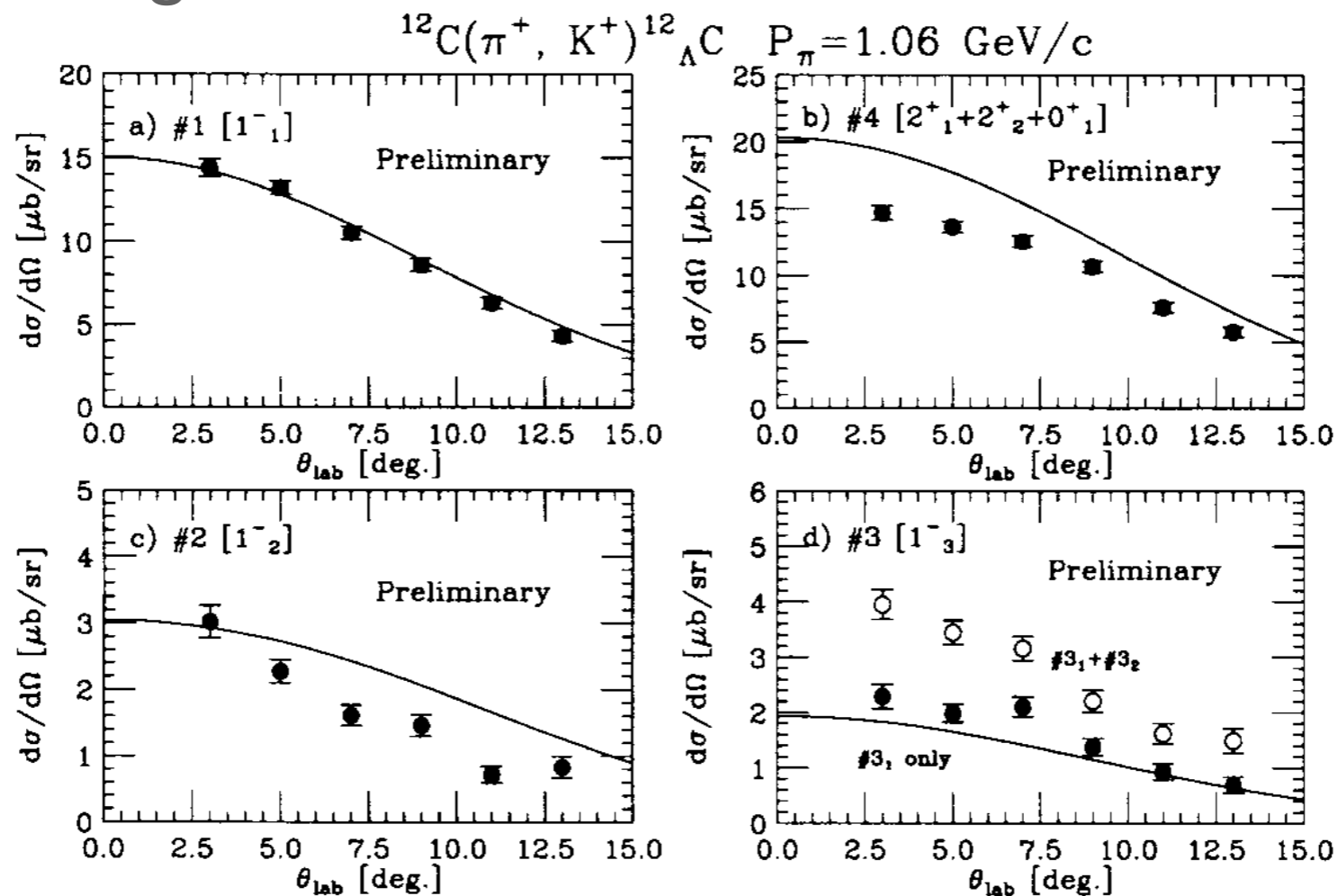
Fig. 4.1. θ -dependence of the single-particle transition matrix element $\langle n_\Lambda l_\Lambda | \tilde{J}_L Y_L U_- | n_N l_N \rangle$ calculated for the (K^-, π^-) reaction at $p_K = 720 \text{ MeV}/c$.²⁵⁵

(K^-, π^-) on ^{12}C & ^{16}O



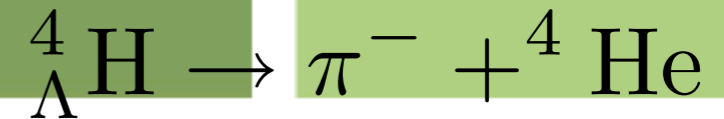
Angular distribution in (π^+, K^+)

- Small change of q
- $^{12}\Lambda C$: good agreement with a DWIA cal.



T. Takahashi et al., Nucl. Phys. A670 (2000) 265c.
 Cal. by K. Itonaga et al., Phys. Rev. C49 (1994) 1045.

Spin of ${}^4_{\Lambda}\text{H}$ (I)



- ▶ ${}^4_{\Lambda}\text{H} = {}^3\text{H}(1/2) + \Lambda(1/2)$
 - ▶ Initial State: $J=0$ or 1
 - ▶ Final State: $\pi(0^{-}), {}^4\text{He}(0^{+})$
 - ▶ s-wave ($J=0$) or p-wave ($J=1$)
 - ▶ isotropic or $\cos^2\Theta$

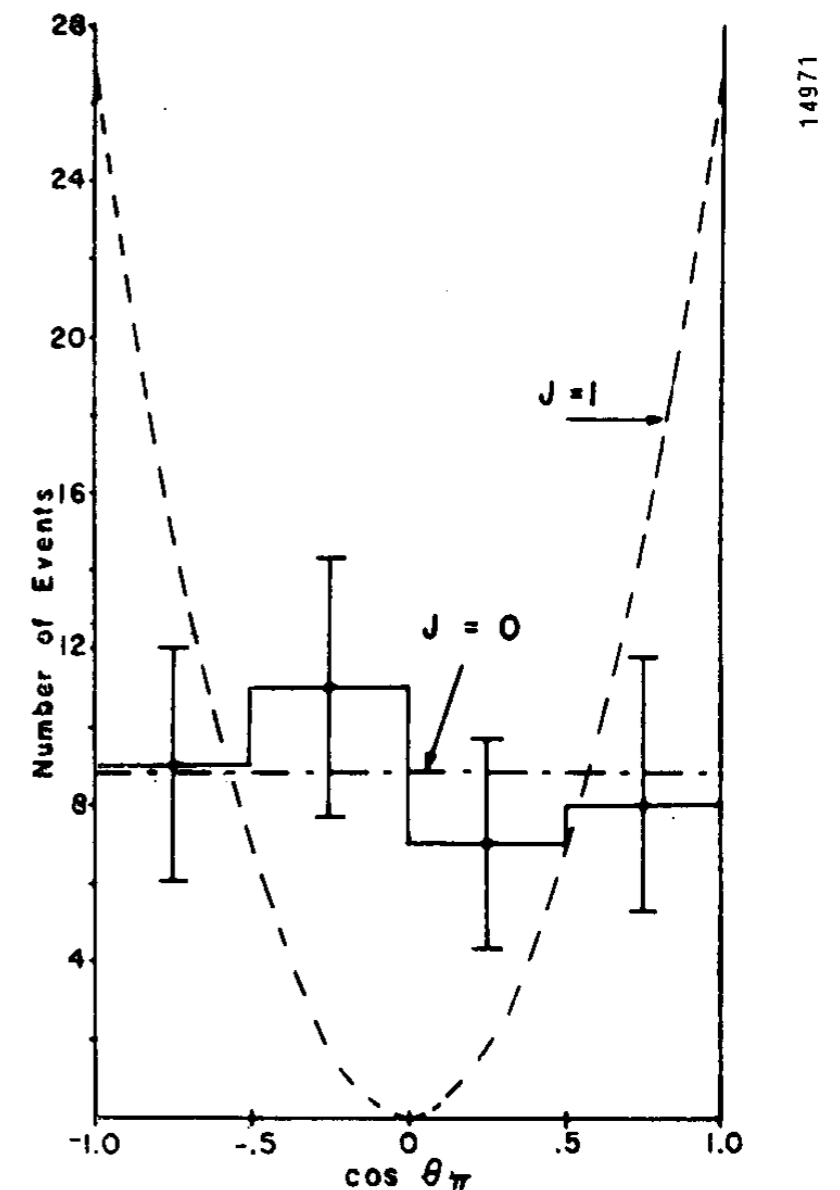


Fig. 1 The angular distribution of the π^{-} from the decay ${}^4_{\Lambda}\text{H} \rightarrow \pi^{-} + {}^4\text{He}$, for hyperfragments produced in the capture reaction $K^{-} + {}^4\text{He} \rightarrow {}^4_{\Lambda}\text{H} + \pi^{0}$.

Spin of ${}^4_{\Lambda}\text{H}$ (2)

► $R_4 = ({}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^4\text{He}) / (\text{all } \pi^- \text{ decays of } {}^4_{\Lambda}\text{H})$

► v.s. $p^2/(s^2+p^2)$

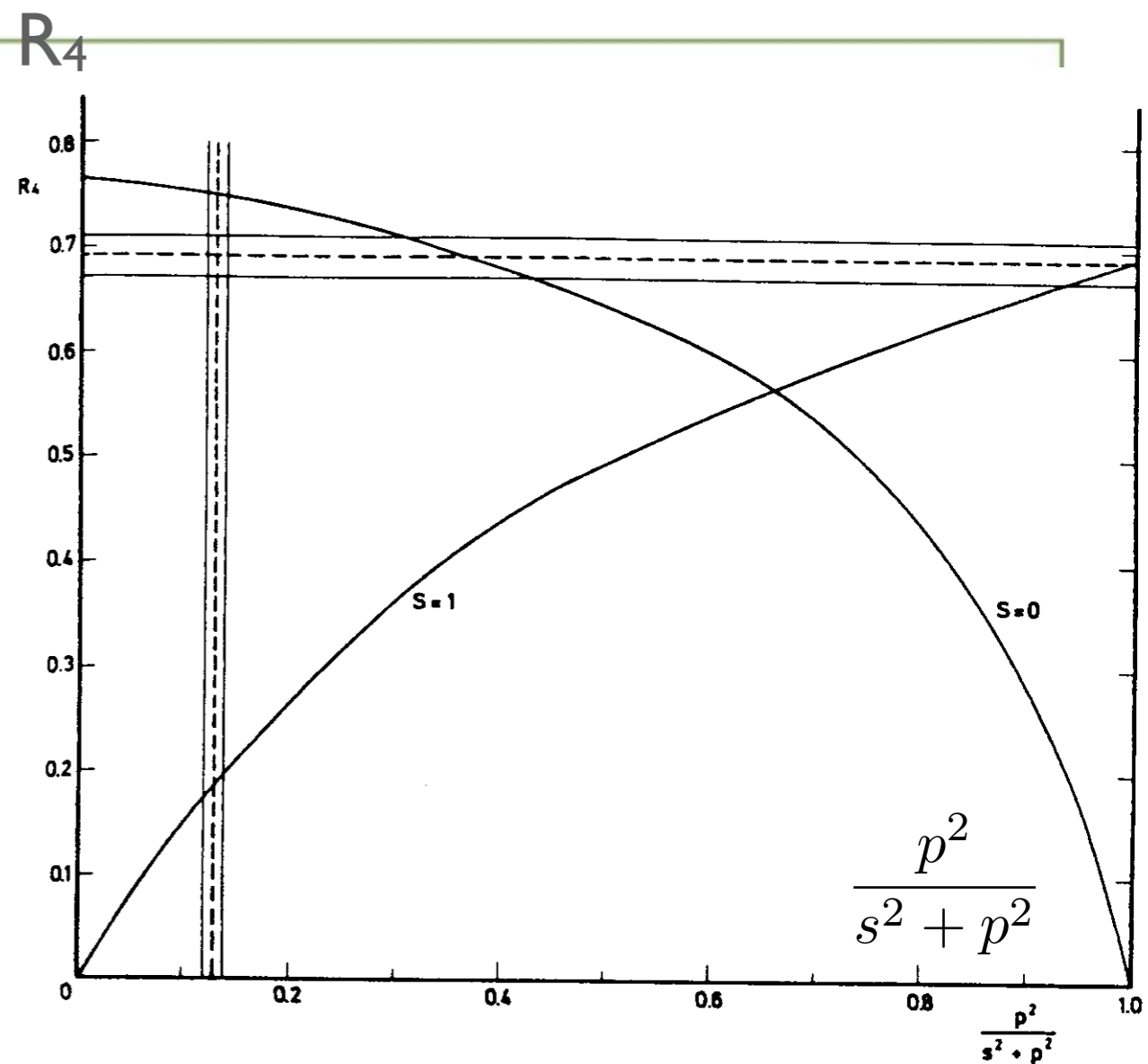
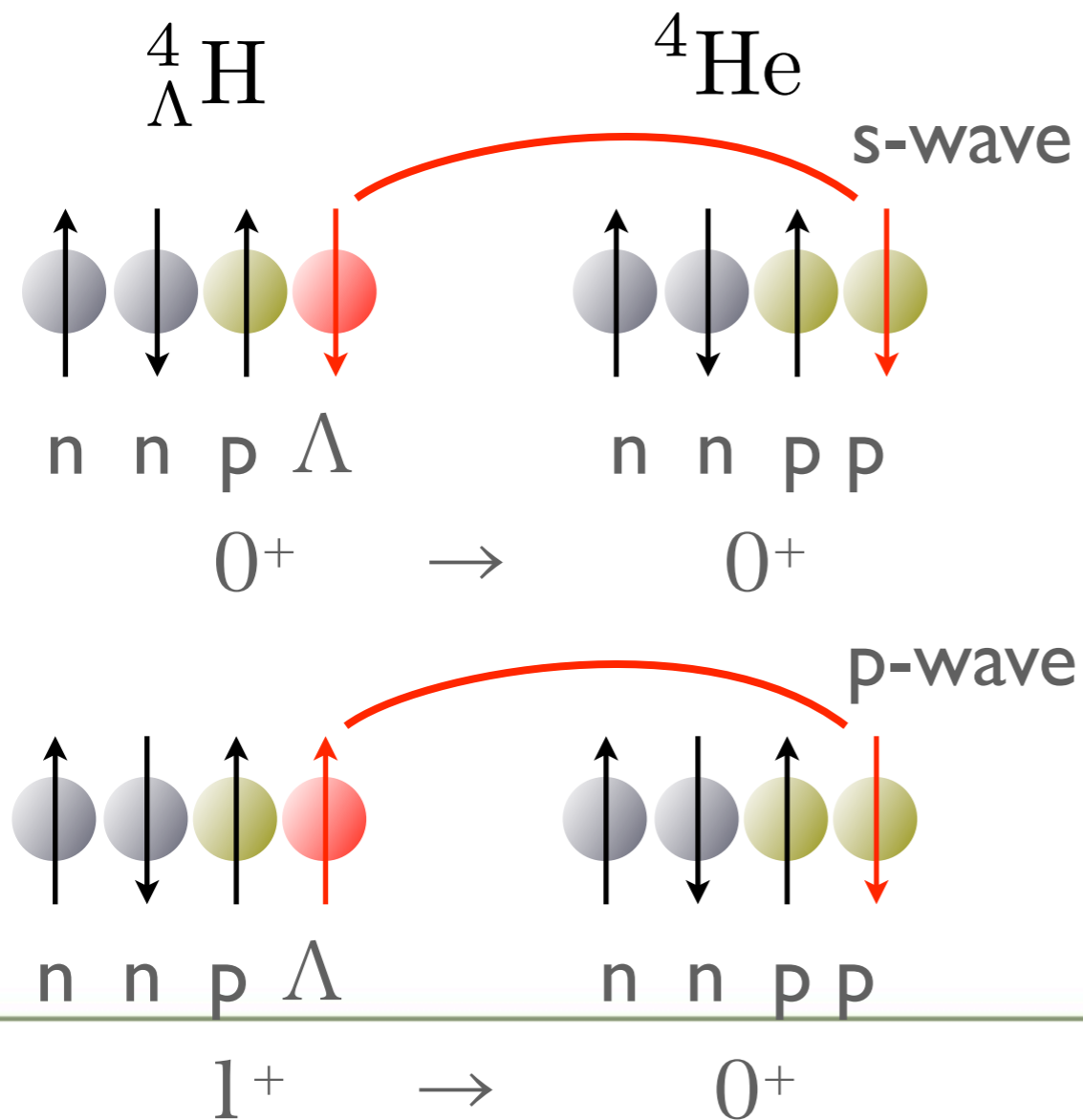


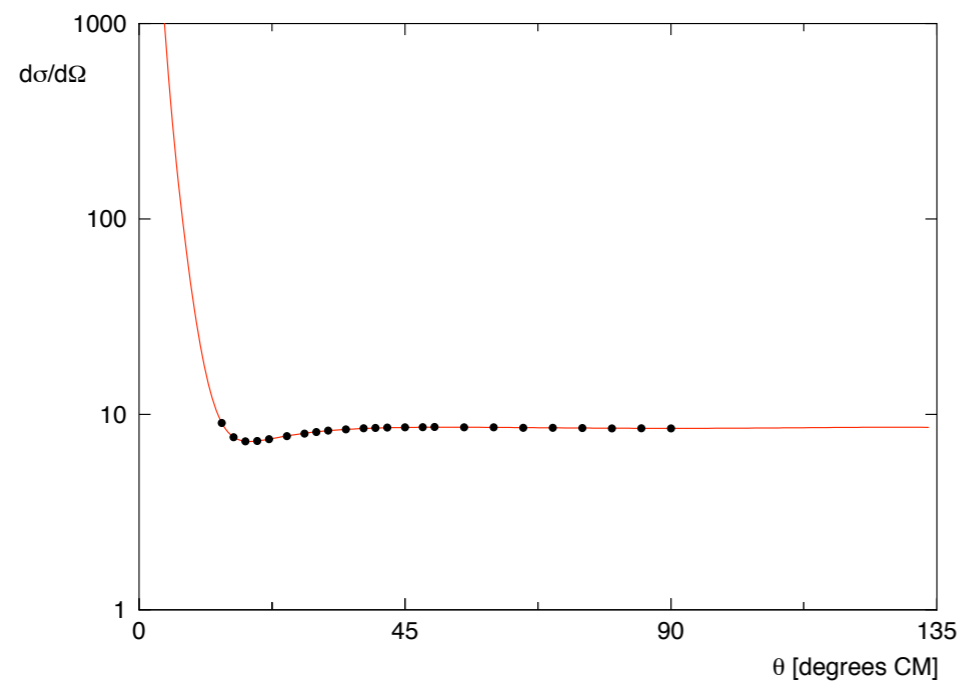
Fig. 3. The ratio $R_4 = ({}^4_{\Lambda}\text{H} \rightarrow \pi^- + {}^4\text{He}) / (\text{all } \pi^- \text{ mesonic decays of } {}^4_{\Lambda}\text{H})$ as a function of $p^2/(p^2+s^2)$. The curves illustrate the results of the calculations made by Dalitz and Liu [4] for $J({}^4_{\Lambda}\text{H}) = 0$ and 1.

Motivations of Hypernuclear Spectroscopy

- ▶ Extract YN and YY interactions
 - difficulties in YN and YY scattering measurements
- ▶ Hyperon as an impurity
 - structure change, new symmetry, etc.
- ▶ Hyperon in nuclei
 - effective mass, magnetic moment, etc.

Realistic Nuclear Force

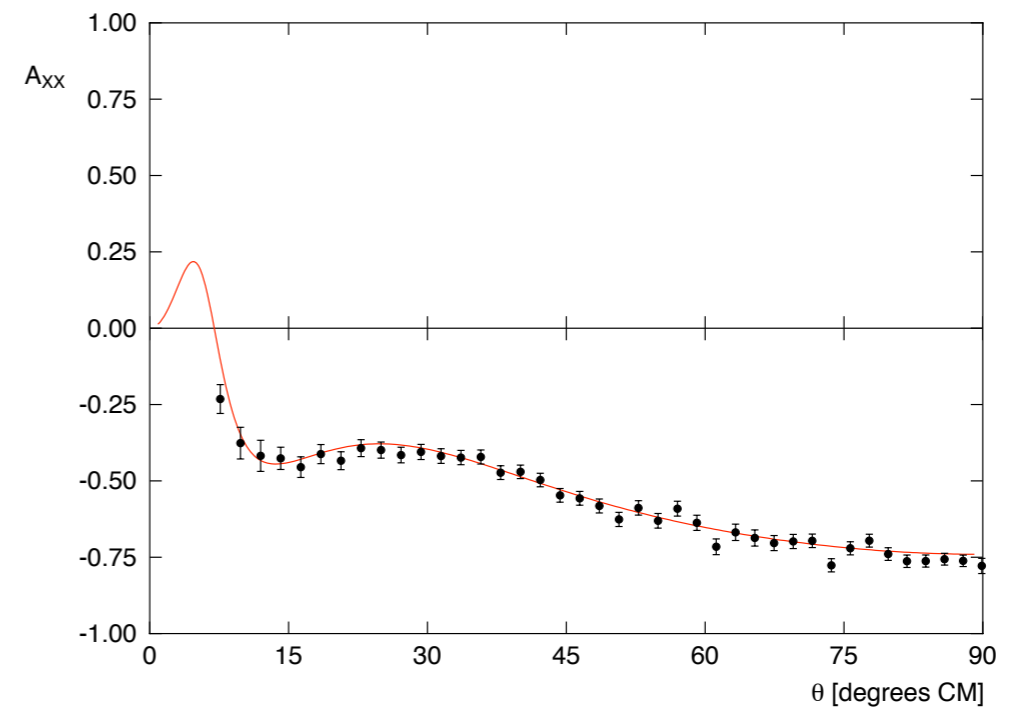
- ▶ Based on a lot of pp & pn scattering data:
 - ▶ ~5900 $d\sigma/d\Omega$, >2000 Pol., + 1700 data



pp observable $d\sigma/d\Omega$ at $T_{\text{lab}} = 50.06$ MeV

— PWA93

• Berdoz et al., SIN(1986)



pp observable A_{xx} at $T_{\text{lab}} = 350.0$ MeV

— PWA93

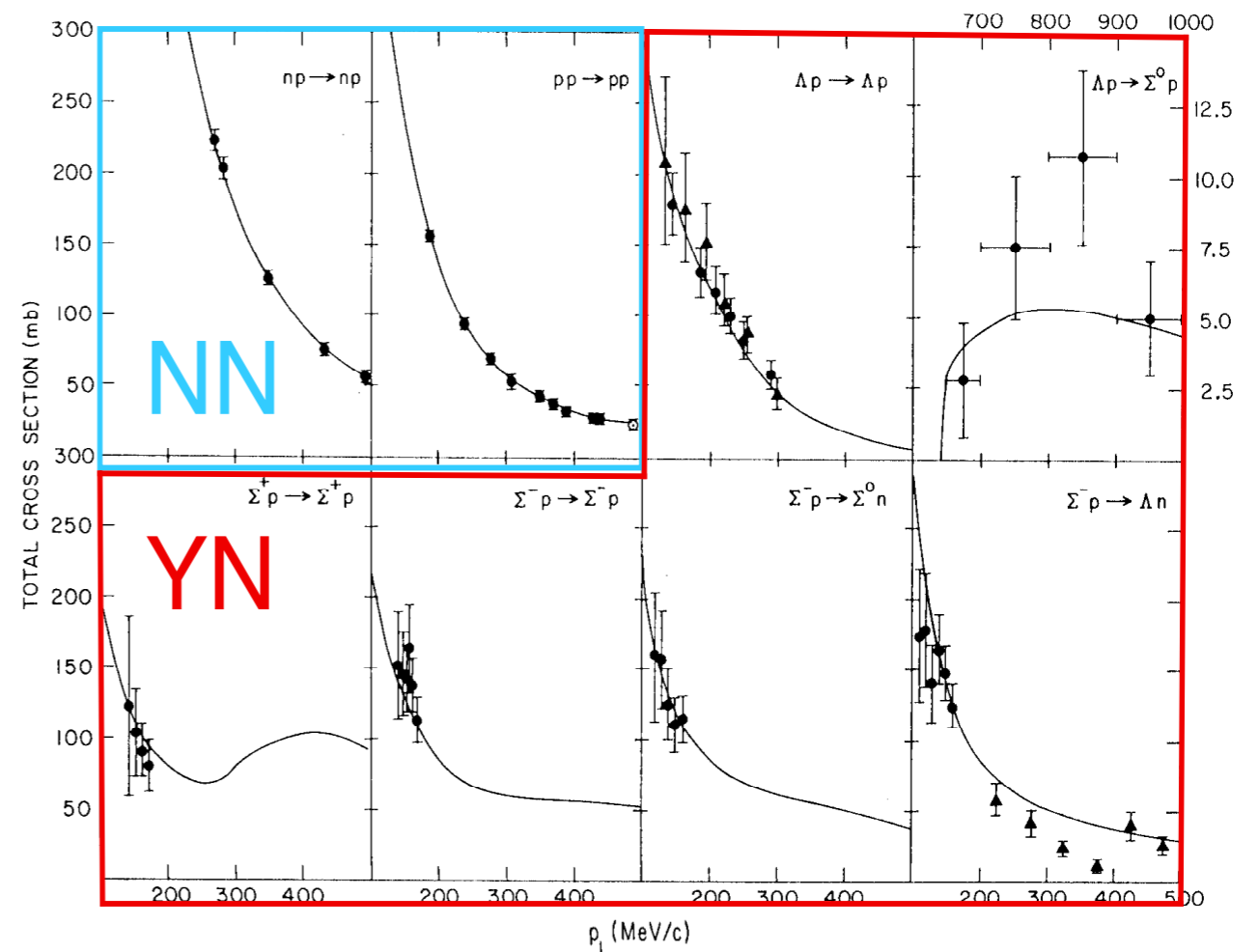
• von Przewoski et al., IUCF(1998)

Hyperon-Nucleon Scattering

$\Sigma^\pm p, \Lambda p$: only 38 data points

- $\Xi^- p$ elastic scattering and $\Xi^- p \rightarrow \Lambda \Lambda$ reaction
- Asymmetry in Λp and $\Sigma^+ p$ elastic scattering

$\Lambda^+ p, \Sigma^+ p, \Sigma^- p$ and $\Xi^- p$ scattering

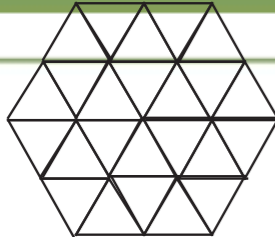


from Dover & Feshbach Ann.Phys.198(90)321

Need high quality data with high statistics

Baryon-Baryon Interaction

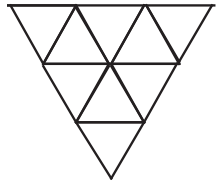
Baryon-Baryon Systems in SU(3)

27_s 


- S=0 NN(T=1)
- S=-1 ΣN(T=3/2)ΣN-ΛN(T=1/2)
- S=-2 ΣΣ(T=2)ΞN-ΣΛ-ΣΣ(T=1)ΞN-ΣΣ-ΛΛ(T=0)
- S=-3 ΞΣ(T=3/2)ΞΣ-ΞΛ(T=1/2)
- S=-4 ΞΞ(T=1)

10_a 


- S=0 NN(T=0)
- S=-1 ΣN-ΛN(T=1/2)
- S=-2 ΞN-ΣΛ(T=1)
- S=-3 ΞΣ(T=3/2)

10_a 

- S=-1 ΣN(T=3/2)
- S=-2 ΞN-ΣΛ-ΣΣ(T=1)
- S=-3 ΞΣ-ΞΛ(T=1/2)
- S=-4 ΞΞ(T=0)

8_s 

- S=-1 ΣN-ΛN(T=1/2)
- S=-2 ΞN-ΣΛ(T=1)ΞN-ΣΣ-ΛΛ(T=0)
- S=-3 ΞΣ-ΞΛ(T=1/2)

8_a 

- S=-1 ΣN-ΛN(T=1/2)
- S=-2 ΞN-ΣΛ-ΣΣ(T=1)ΞN(T=0)
- S=-3 ΞΣ-ΞΛ(T=1/2)

1_s • S=-2 ΞN-ΣΣ-ΛΛ(T=0)

► Understanding of the flavor SU(3) baryon-baryon interaction

● Y-N, Y-Y < N-N ?

Repulsive or Attractive ?

● Repulsive cores in Y-N/Y-Y ?
What's the origin ?

● Spin-dependent forces in Y-N/Y-Y.

● Dibaryons

H Dibaryon ?

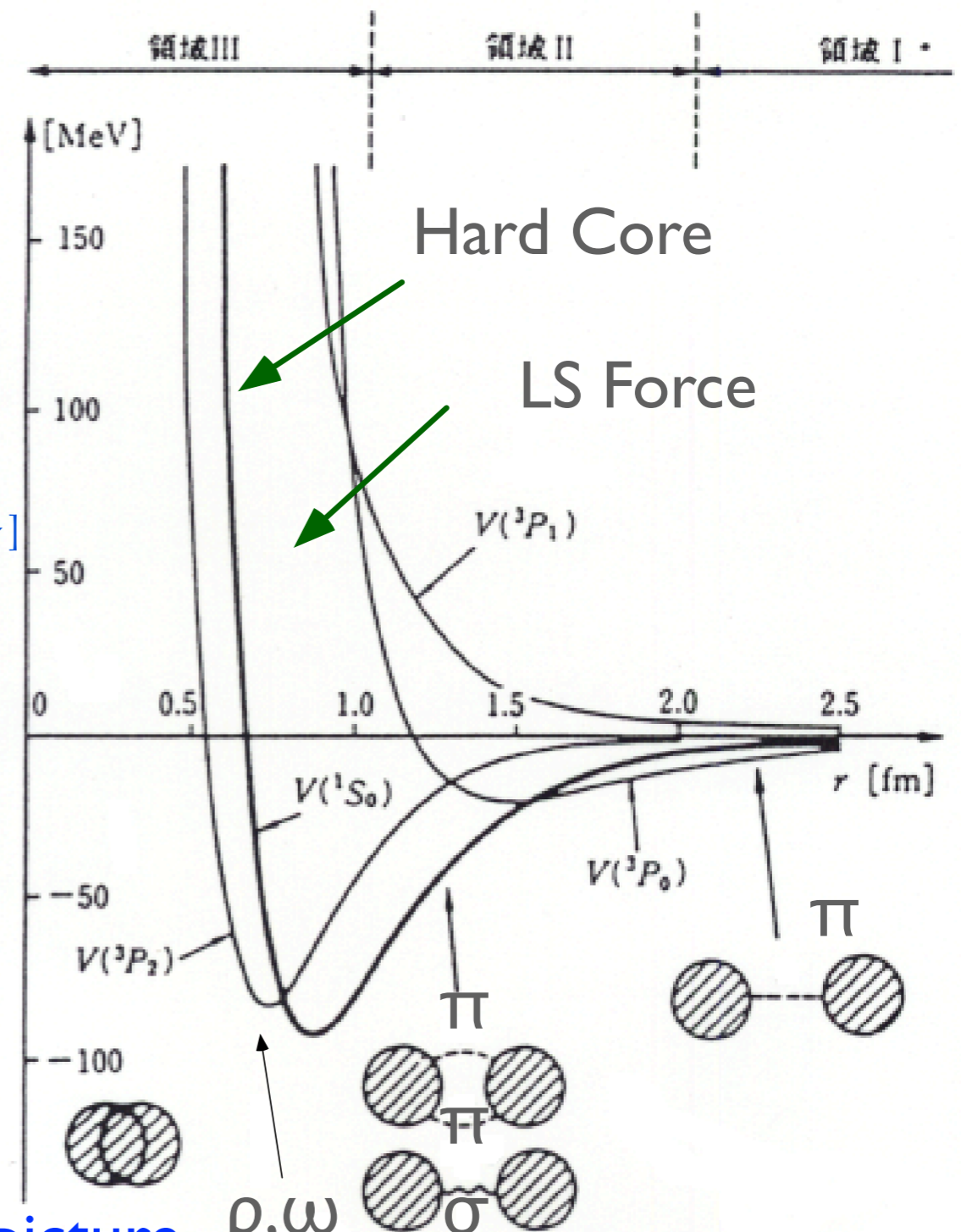
Do we understand the Nuclear Force ?

Short-range forces (=repulsive core, LS force) determine the “basic properties of nucleus” (=saturation, magic number).

from textbook by Tamagaki

Quark Cluster Model

- NN repulsive core → color magnetic int.
 Δ -N mass difference
 ↓
 H dibaryon ($SU_f(3) \times SU_f(3)$ singlet) $[u \uparrow u \downarrow d \uparrow d \downarrow s \uparrow s \downarrow]$
 = Attractive core in $\Lambda\Lambda$ - ΞN channel
- ΣN ($I=3/2, S=1$) strongly repulsive core
 ← quark Pauli blocking
- LS force → quark gluon exchange
 → Λ : very small
 Σ : as large as N



quark-gluon picture

meson exchange picture

Theory Interest in Flavor Nuclear Physics

- Recent Model building:

1. Nijmegen models: OBE and ESC Soft-core (SC)

[Rijken, Phys.Rev. C73, 044007 \(2006\)](#)

[Rijken & Yamamoto, Phys.Rev. C73, 044008 \(2006\)](#)

[Rijken & Yamamoto, arXiv:nucl-th/060874 \(2006\)](#)

2. Chiral-Unitary Approach model

[Sasaki, Oset, and Vacas, Phys.Rev. C74, 064002 \(2006\)](#)

3. Jülich Meson-exchange models

[Haidenbauer, Meissner, Phys.Rev. C72, 044005 \(2005\)](#)

4. Jülich Effective Field Theory models

[Polinder, Haidenbauer, Meissner, Nucl.Phys. A 779, 244 \(2006\)](#)

5. Quark-Cluster-models: QGE + RGM

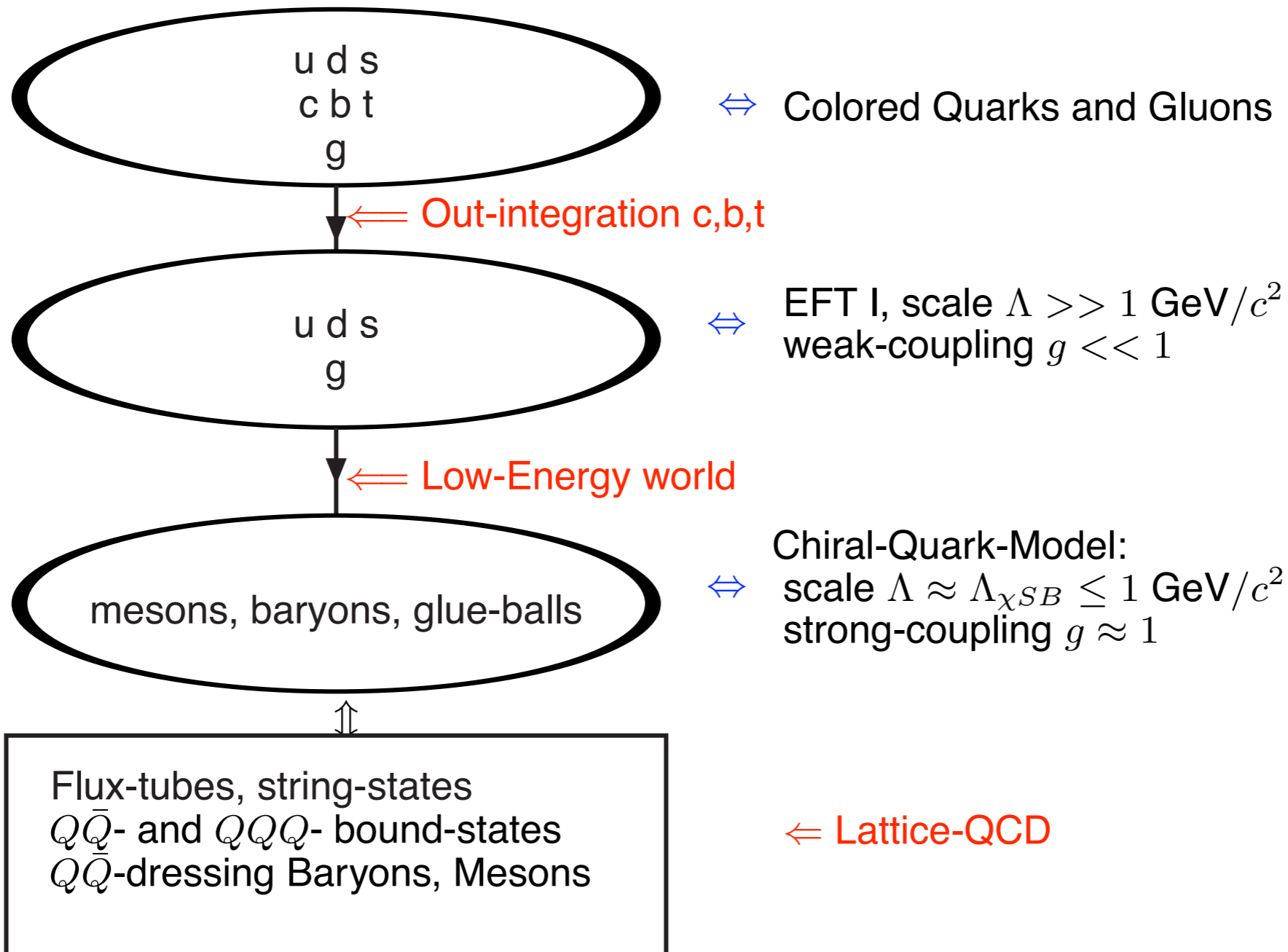
[Fujiwara et al, Progress in Part. & Nucl.Phys. 58, 439 \(2007\)](#)

[Valcarce et al, Rep.Progr.Phys. 68, 965 \(2005\)](#)

Th.A. Rijken

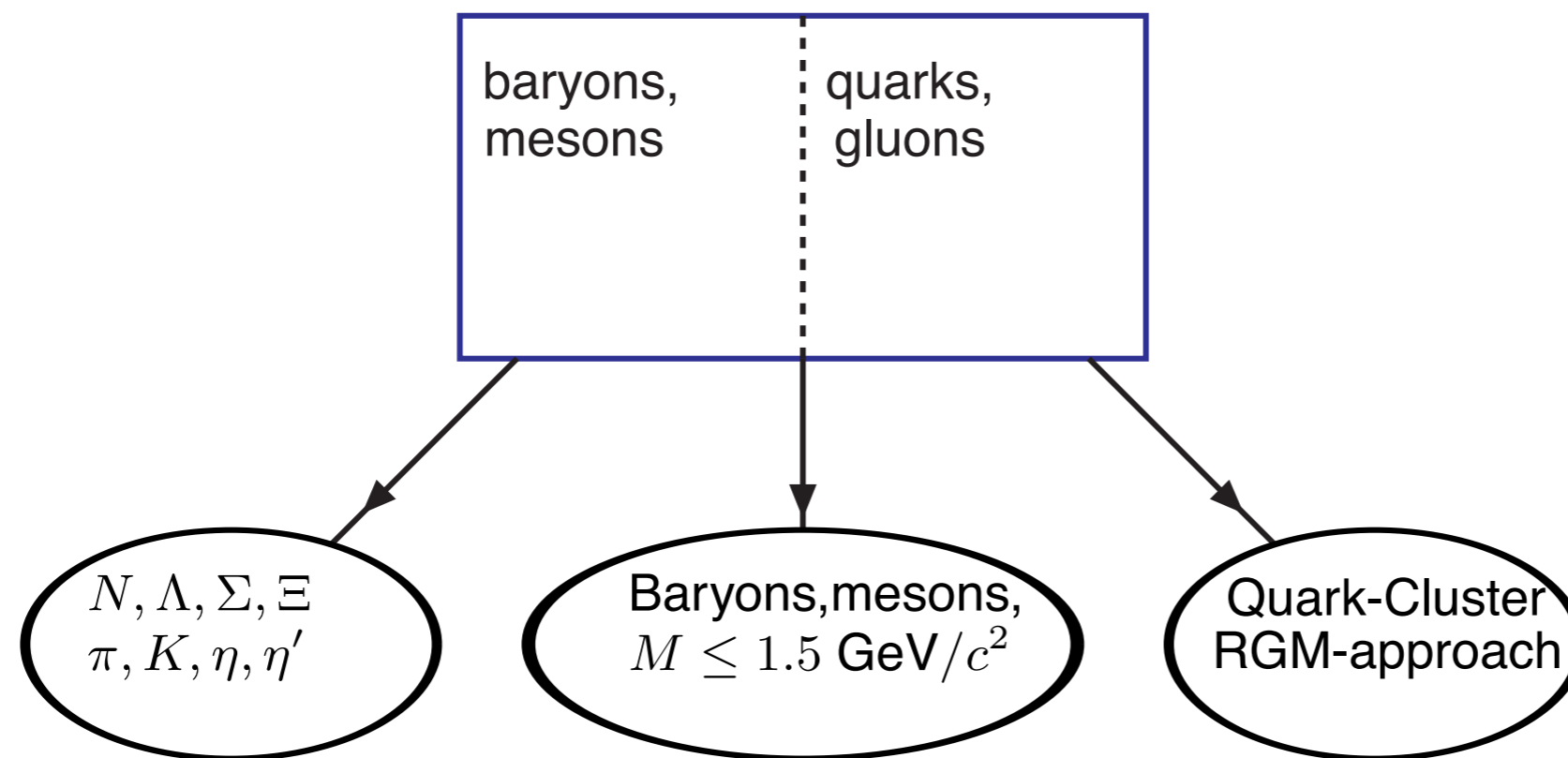
QCd-world I

QCD-world I: mesons and baryons



QCD-world II

QCD-world II: Baryon/Meson-baryon Interactions



Goldstone-boson exch.
+ contact-terms
Chiral Pert. Models:
Van Kolck, Epelbaum,
Bonn-Jülich, Barcelona, etc.

Meson-exchange models
Nijmegen NSC97, ESC04,
Ehime, Jülich, etc.

Quark-Gluon-
+ OBE-exchange
Tokyo, Kyoto-Niagatta,
Tübingen, Salamanca,
Nanjing, etc.

Th.A. Rijken

Quark Pauli principle

► $(0s)^6$ is not allowed for $[51]$

$$[222]_c \times [51]_{sf} \times [6]_o \neq [1^6]$$

► n: $-|ddu\rangle\{2|++-\rangle-|+-+\rangle-|-++\rangle\}/3\sqrt{2}$

► Σ^- : $|dds\rangle\{2|++-\rangle-|+-+\rangle-|-++\rangle\}/3\sqrt{2}$

$SU(6)_{fs}$ -contents of the various potentials on the isospin, spin basis.

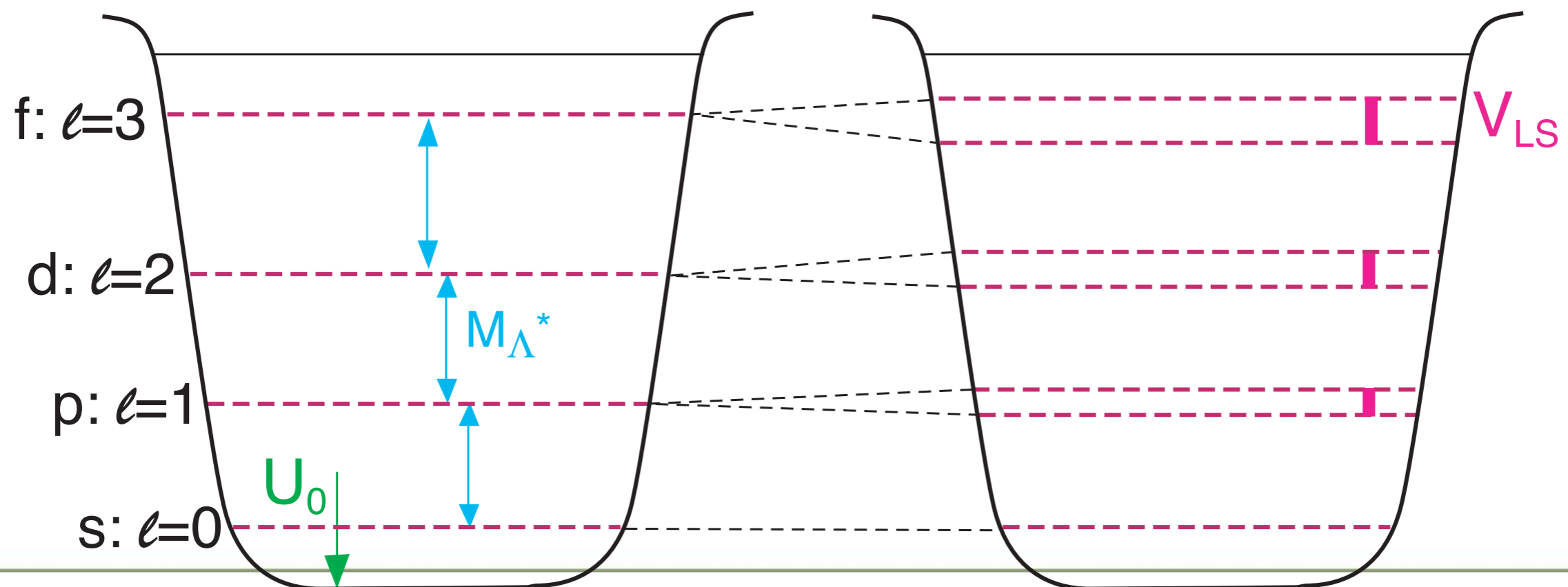
	(S, I)	$V = aV_{[51]} + bV_{[33]}$
$NN \rightarrow NN$	$(0, 1)$	$V_{NN}(I = 1) = \frac{4}{9}V_{[51]} + \frac{5}{9}V_{[33]}$
$NN \rightarrow NN$	$(1, 0)$	$V_{NN} = \frac{4}{9}V_{[51]} + \frac{5}{9}V_{[33]}$
$\Lambda N \rightarrow \Lambda N$	$(0, 1/2)$	$V_{\Lambda\Lambda} = \frac{1}{2}V_{[51]} + \frac{1}{2}V_{[33]}$
$\Lambda N \rightarrow \Lambda N$	$(1, 1/2)$	$V_{\Lambda\Lambda} = \frac{1}{2}V_{[51]} + \frac{1}{2}V_{[33]}$
$\Sigma N \rightarrow \Sigma N$	$(0, 1/2)$	$V_{\Sigma\Sigma} = \frac{17}{18}V_{[51]} + \frac{1}{18}V_{[33]}$
$\Sigma N \rightarrow \Sigma N$	$(1, 1/2)$	$V_{\Sigma\Sigma} = \frac{1}{2}V_{[51]} + \frac{1}{2}V_{[33]}$
$\Sigma N \rightarrow \Sigma N$	$(0, 3/2)$	$V_{\Sigma\Sigma} = \frac{4}{9}V_{[51]} + \frac{5}{9}V_{[33]}$
$\Sigma N \rightarrow \Sigma N$	$(1, 3/2)$	$V_{\Sigma\Sigma} = \frac{8}{9}V_{[51]} + \frac{1}{9}V_{[33]}$

Hypernuclear structure and ΛN interaction

$$V_{\Lambda N} = U_0 + V_S \sigma_N \cdot \sigma_\Lambda + V_{\Lambda} \ell_{N\Lambda} \cdot \sigma_\Lambda + V_N \ell_{N\Lambda} \cdot \sigma_N + V_{TS} S_{I2}$$

(a) Central Attraction Only

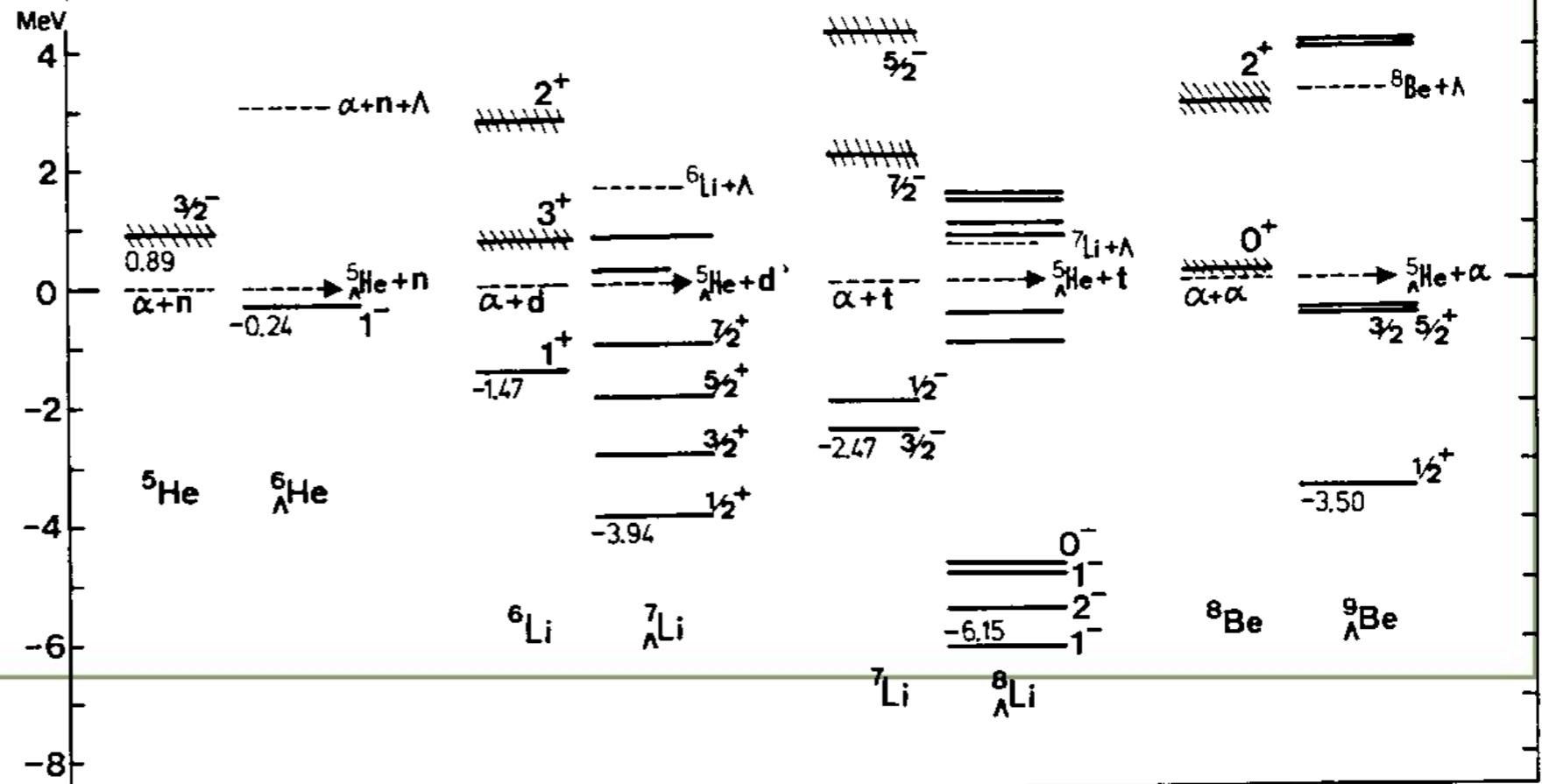
(b) Central + Spin-Orbit Force



Impurity Effect - I

► Glue-like role

- Energetical stabilization
- Resonant states in neutron-rich nuclei
→ Bound states in Λ -hypernuclei

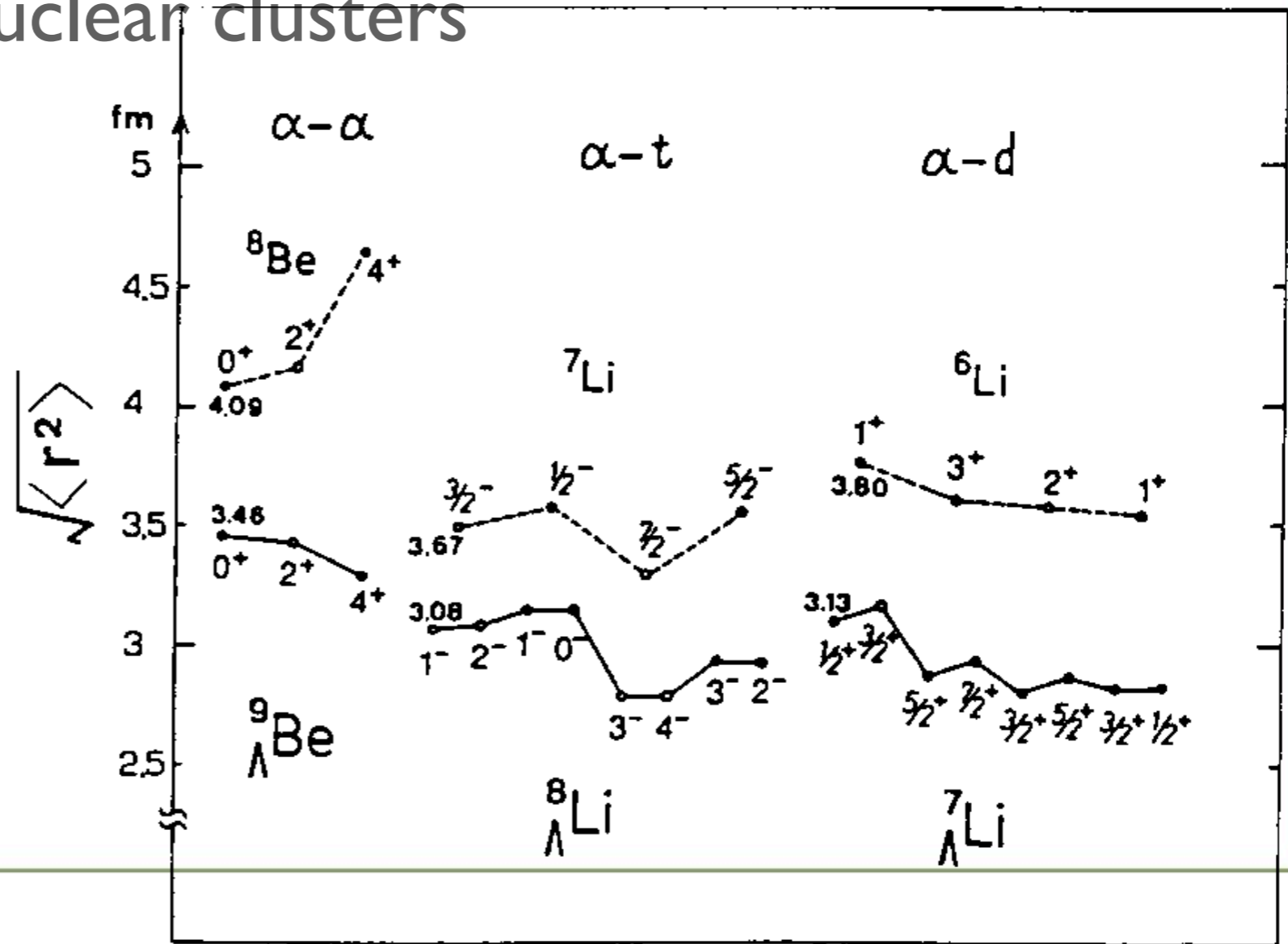


Impurity Effect -2

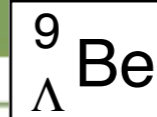
- ▶ Structure Change
- ▶ Shrinkage of nuclear clusters

$$B(E2) \propto |\langle f | e r^2 Y_2 | i \rangle|^2$$

$$\propto R^4 \text{ or } (\beta \langle r^2 \rangle)^2$$

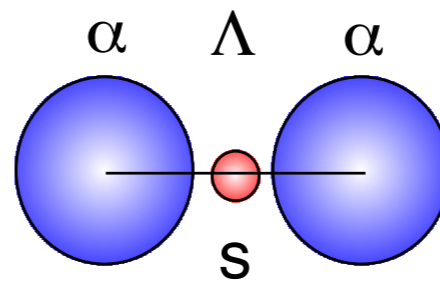
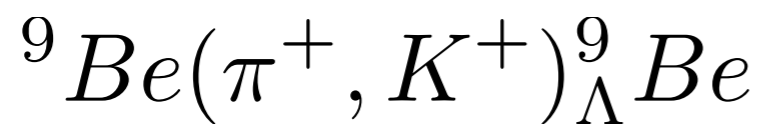
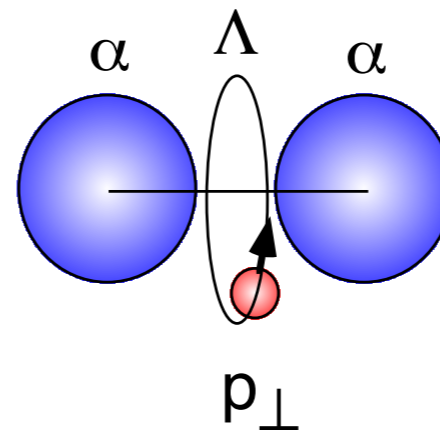
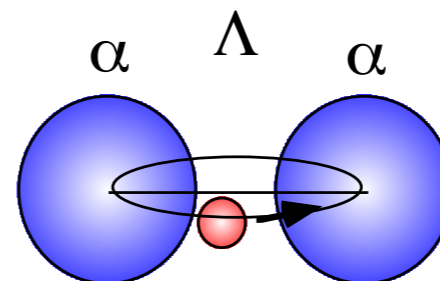


Impurity Effect -3



► New symmetry:

- Supersymmetric state or
Genuine hypernuclear state


 $[(\alpha\alpha) \otimes s\Lambda]$
 ${}^8\text{Be-analog}$

 $[(\alpha\alpha) \otimes p_{\perp}\Lambda]$
 ${}^9\text{Be-analog}$

 $[(\alpha\alpha) \otimes p_{\parallel}\Lambda]$
 $\text{Genuine hypernuclear}$
 p_{\parallel}

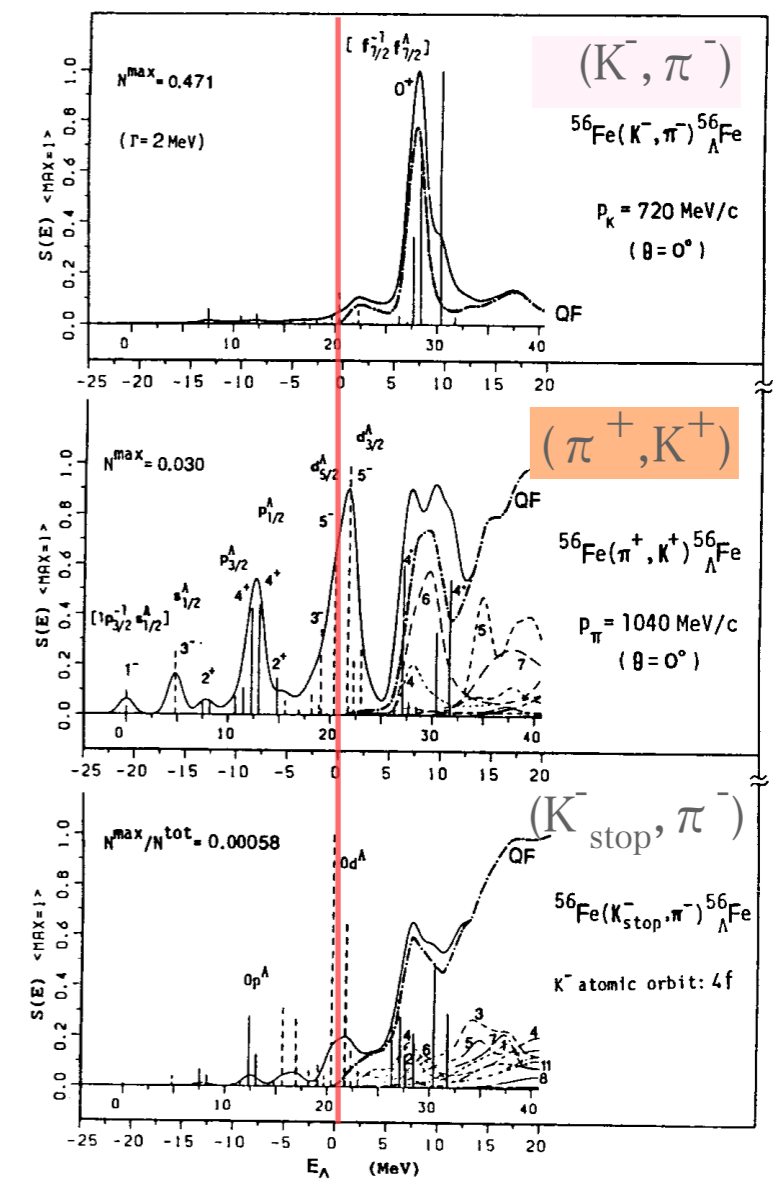
(π^+, K^+) Spectroscopy

► Merits

- ✱ Large momentum transfer $q \sim 350$ MeV/c
- ✱ Efficiently produces deeply-bound states
- ✱ Low backgrounds: γ , n

► Demerits

- ✱ No difference in angular distributions



(π^+, K^+) Spectroscopy

Reaction mechanism:

■ Dover, Ludeking, Walker, Phys. Rev. C22(1980) 2073.

Success at BNL(1985, 1988)

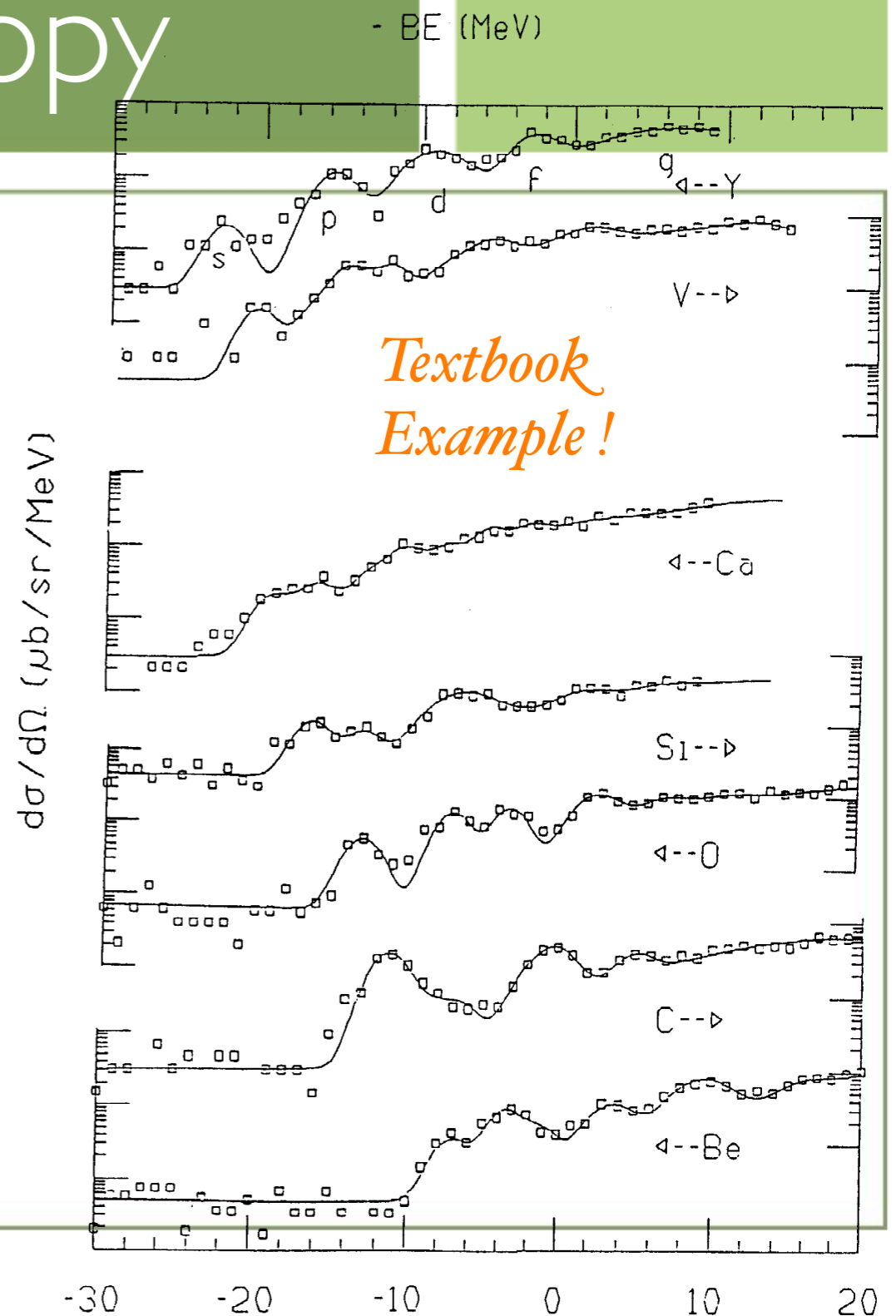
■ $\Delta E \sim 3$ MeV

■ Up to $^{89}_{\Lambda}Y$

► $q \sim 350$ MeV/c

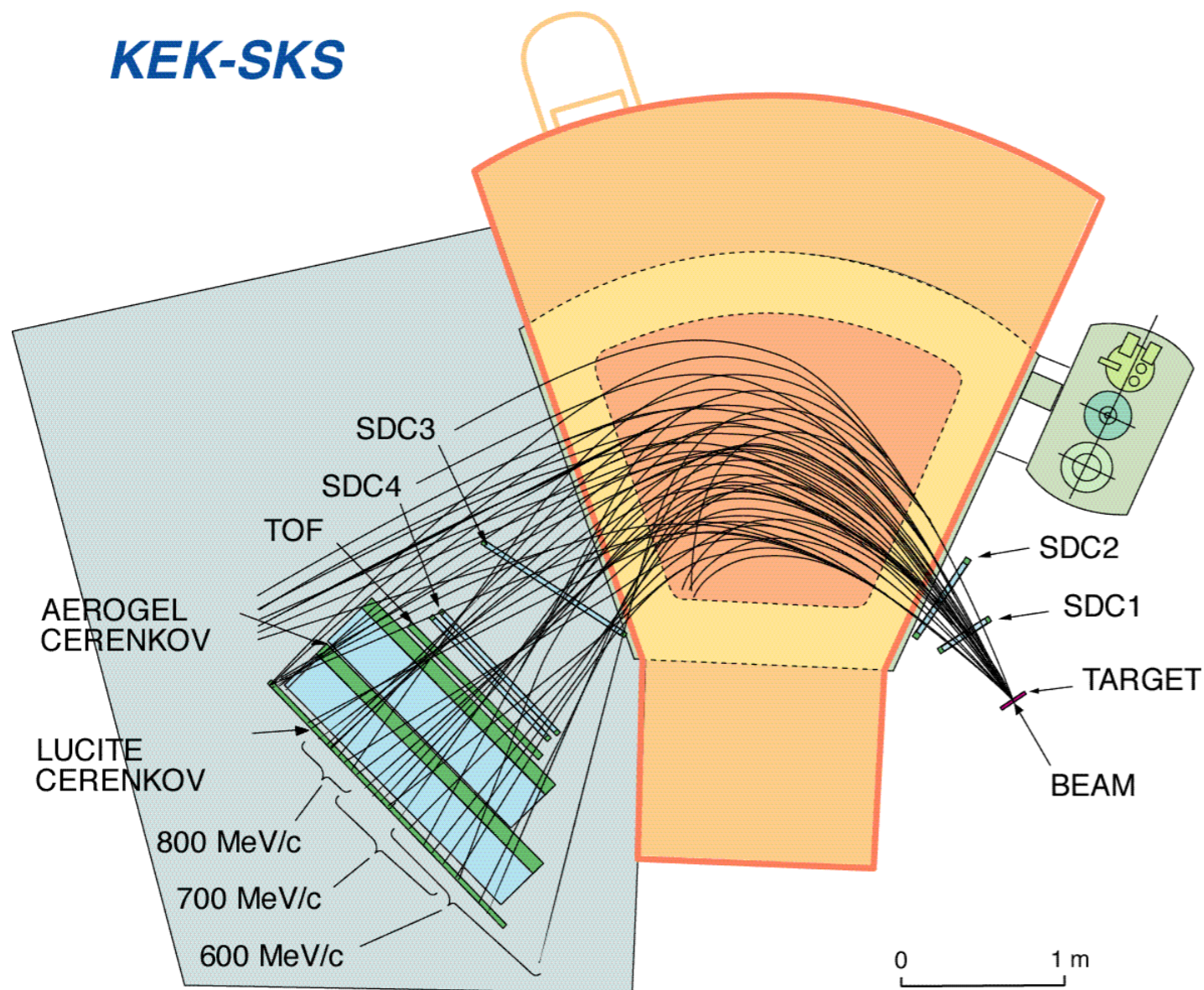
✓ natural-parity stretched states

✓ $[(\ell_N j_N)^{-1} (\ell_{\Lambda} j_{\Lambda})]$ with $J = \ell_N + \ell_{\Lambda}$



SKS spectrometer at KEK-PS

KEK-SKS



- Superconducting Kaon Spectrometer for the (π^+ , K^+) reactions
- Constructed by INS, Univ. of Tokyo, from 1987 to 1990
- In operation since 1992
- $B_{\max} = 3T$ (500A)
- Pole Gap = 50 cm
- 10.6 MJ stored
- Cold Mass ~ 4.5 t
- ~ 280 tons

Design Specifications of the SKS

- Momentum resolution:
0.1%(FWHM) at 720 MeV/c
- Solid angle: 100 msr
 - To get enough yields
- Short Flight Path: ~5 m
 - To reduce K^+ decays
- Initial Goal of Energy Resolution:
2 MeV(FWHM)

Challenges in the SKS

- Good Energy Resolution: <2 MeV(FWHM)
- Magnetic Field Mapping: $\Delta B/B < 10^{-3}$
 - Fully automated 3D positioning system
 - (120,000points x 7excitations) in 1.5 months
 - Very careful calibrations
- 3 T magnet with very low heat leak
- He transfer line with rotation capability

Momentum resolution

► K6 Beamline

- Matrix representations for magnets

$$\vec{x}'_{out} = QQDQQ\vec{x}'_{in}$$

$$\vec{x}' = (x, y, \theta \equiv dx/dz, \varphi \equiv dy/dz, \delta \equiv (p - p_0)/p_0)$$

- $\langle x' | \theta \rangle \sim 0$

- Resolution in 1st order

$$\frac{\langle x' | x \rangle \sigma_x}{\langle x' | \delta \rangle}$$

$$QQDQQ = \begin{pmatrix} \langle x' | x \rangle & \langle x' | y \rangle & \langle x' | \vartheta \rangle & \langle x' | \varphi \rangle & \langle x' | \delta \rangle \\ \langle y' | x \rangle & \langle y' | y \rangle & \langle y' | \vartheta \rangle & \langle y' | \varphi \rangle & \langle y' | \delta \rangle \\ \langle \vartheta' | x \rangle & \langle \vartheta' | y \rangle & \langle \vartheta' | \vartheta \rangle & \langle \vartheta' | \varphi \rangle & \langle \vartheta' | \delta \rangle \\ \langle \varphi' | x \rangle & \langle \varphi' | y \rangle & \langle \varphi' | \vartheta \rangle & \langle \varphi' | \varphi \rangle & \langle \varphi' | \delta \rangle \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

(π, K^+) experiments with SKS

- ▶ E140a: ^{10}B , ^{12}C , ^{28}Si , ^{89}Y , ^{139}La , ^{208}Pb

■ Phys. Rev. C 53 (1996) 1210.

- ▶ E336: ^7Li , ^9Be , ^{13}C , ^{16}O

■ Nucl. Phys. A 639 (1998) 93c, Nucl. Phys. A 691 (2001) 123c.

- ▶ E369: ^{89}Y , ^{51}V , ^{12}C in high-resolution

■ Phys. Rev. C 64 (2001) 044302.

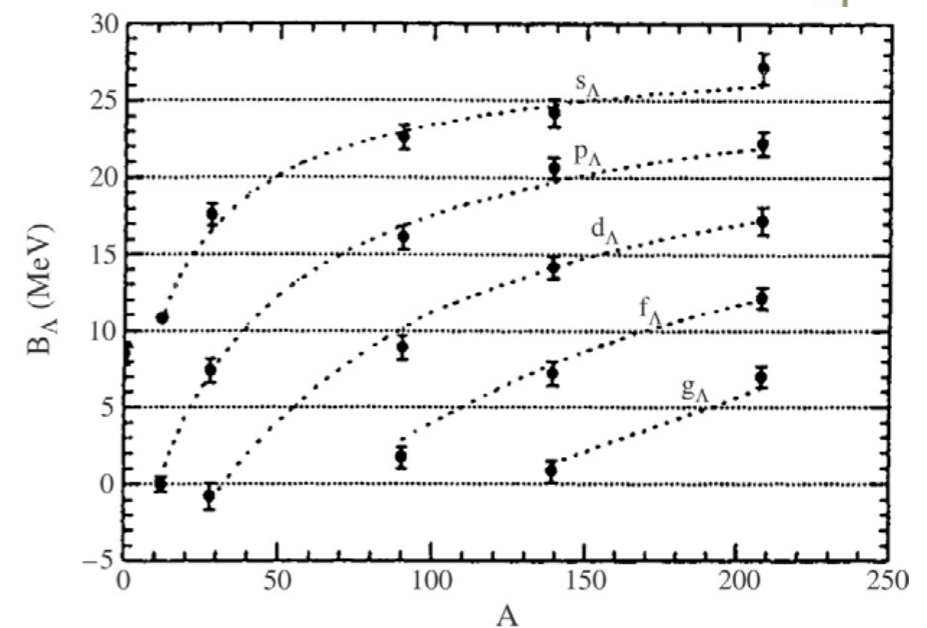
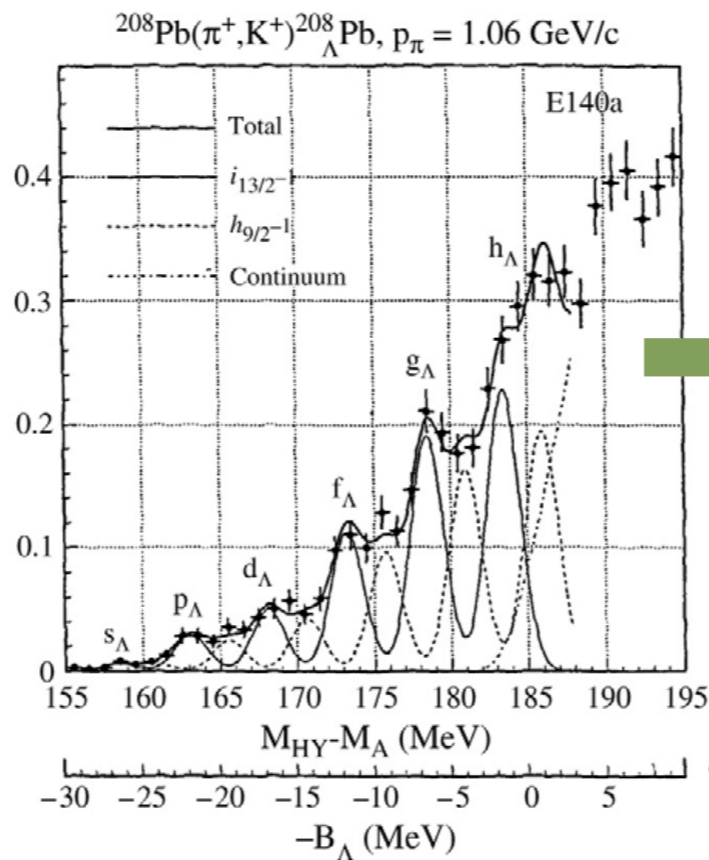
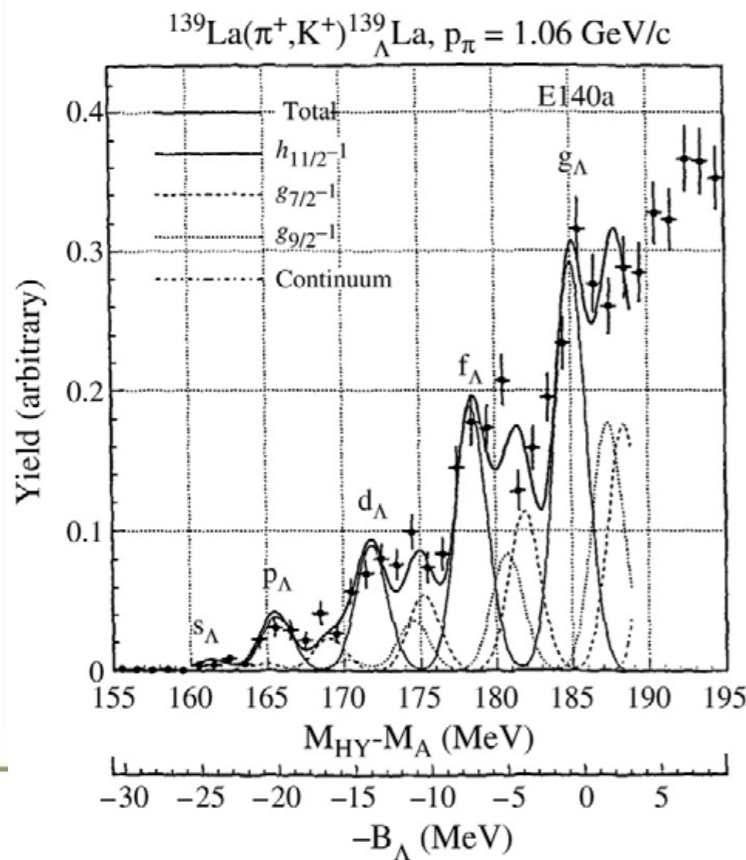
- ▶ E521: $^{10}\text{B}(\pi^-, K^+)$

■ Phys. Rev. Lett. 94 (2005) 052502.

E140a:

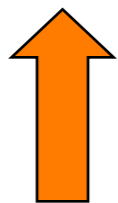
First (π^+, K^+) exp. with the SKS

- Targets: ^{10}B , ^{12}C , ^{28}Si , ^{89}Y , ^{139}La , ^{208}Pb
 - $^{12}\Lambda\text{C}$: First observation of core-excited states
 - Confirmed Λ Shell Structures up to $^{208}\Lambda\text{Pb}$

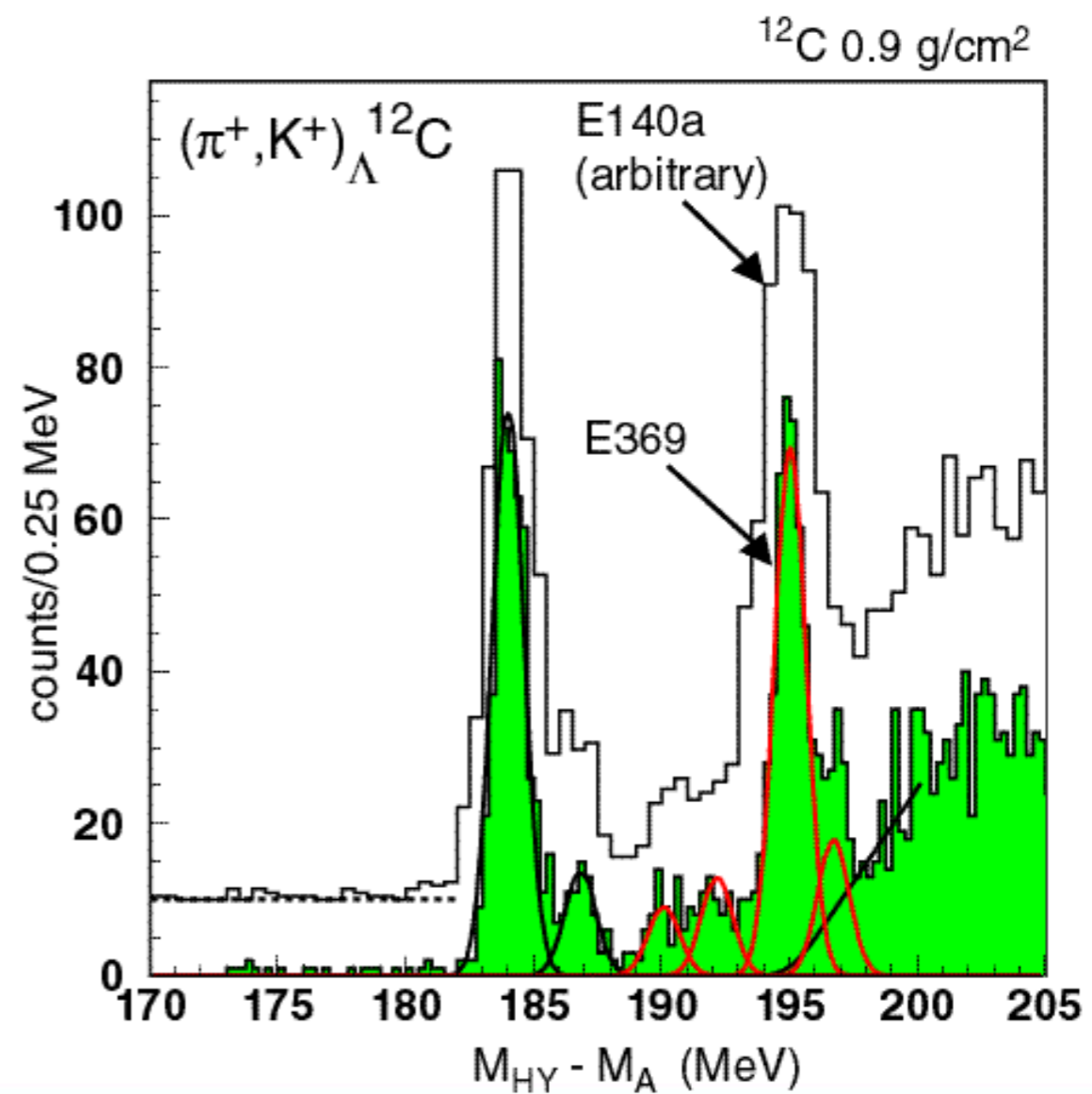


E369: Λ ^{12}C

- Best energy resolution
- $\Delta E(\text{FWHM})$
= 1.45 MeV

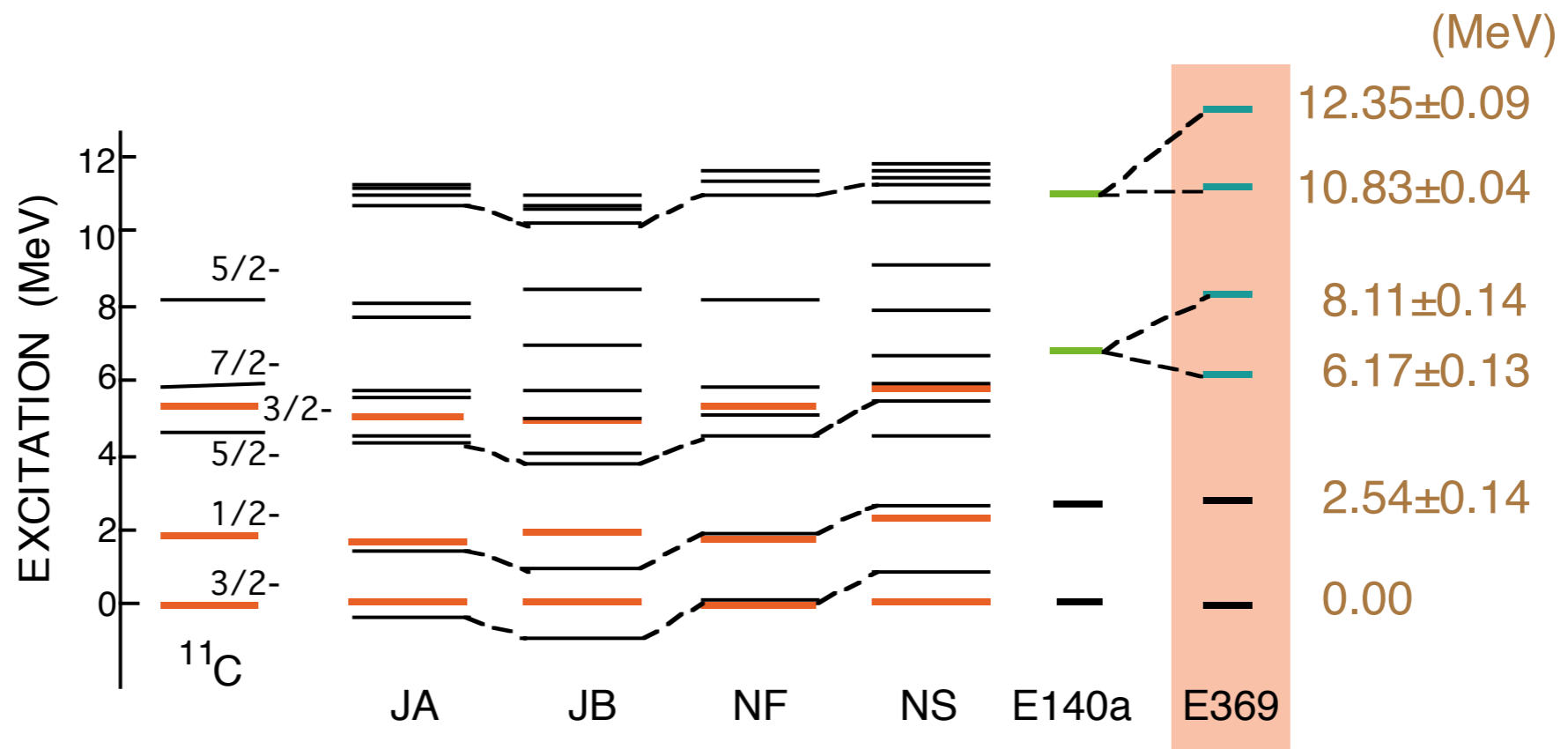


2.0 MeV



Core-excited states of $\Lambda^{12}\text{C}$

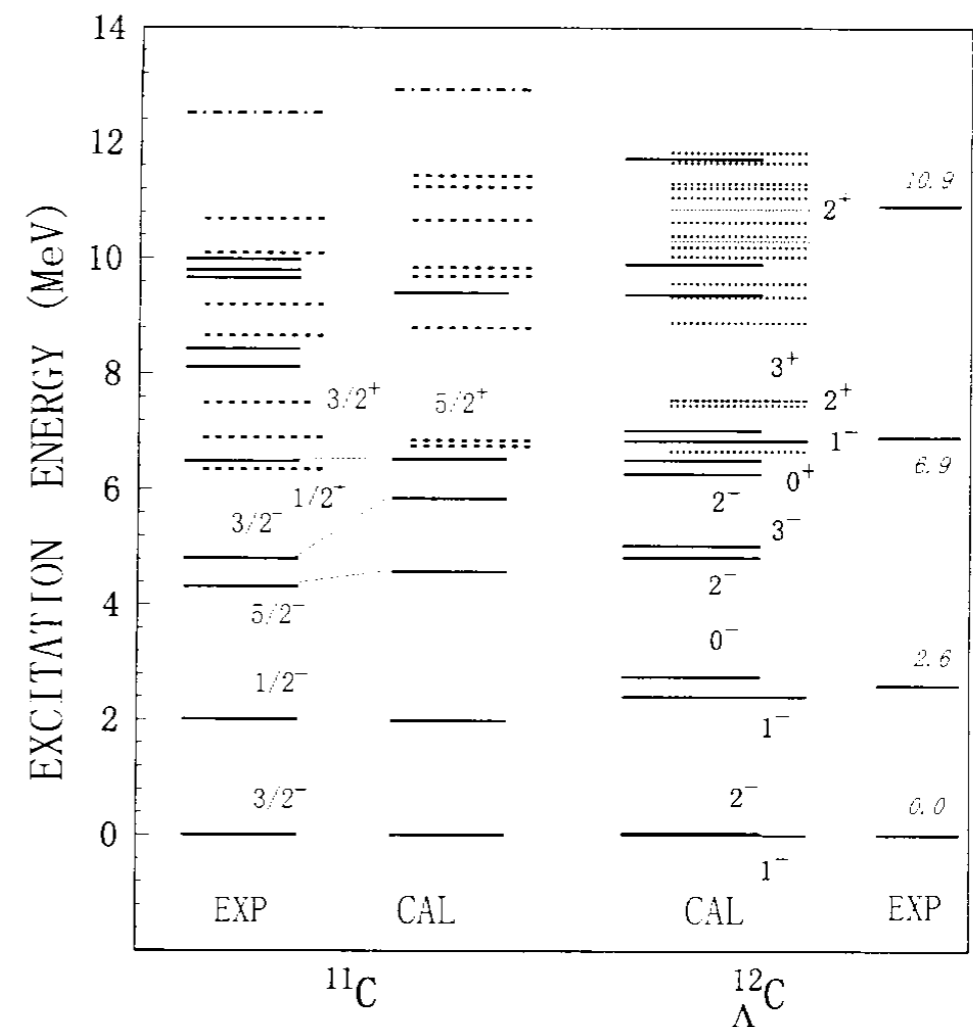
- New states are resolved.
- Effects of ΛN spin-dependent forces



Parity-mixing intershell coupling

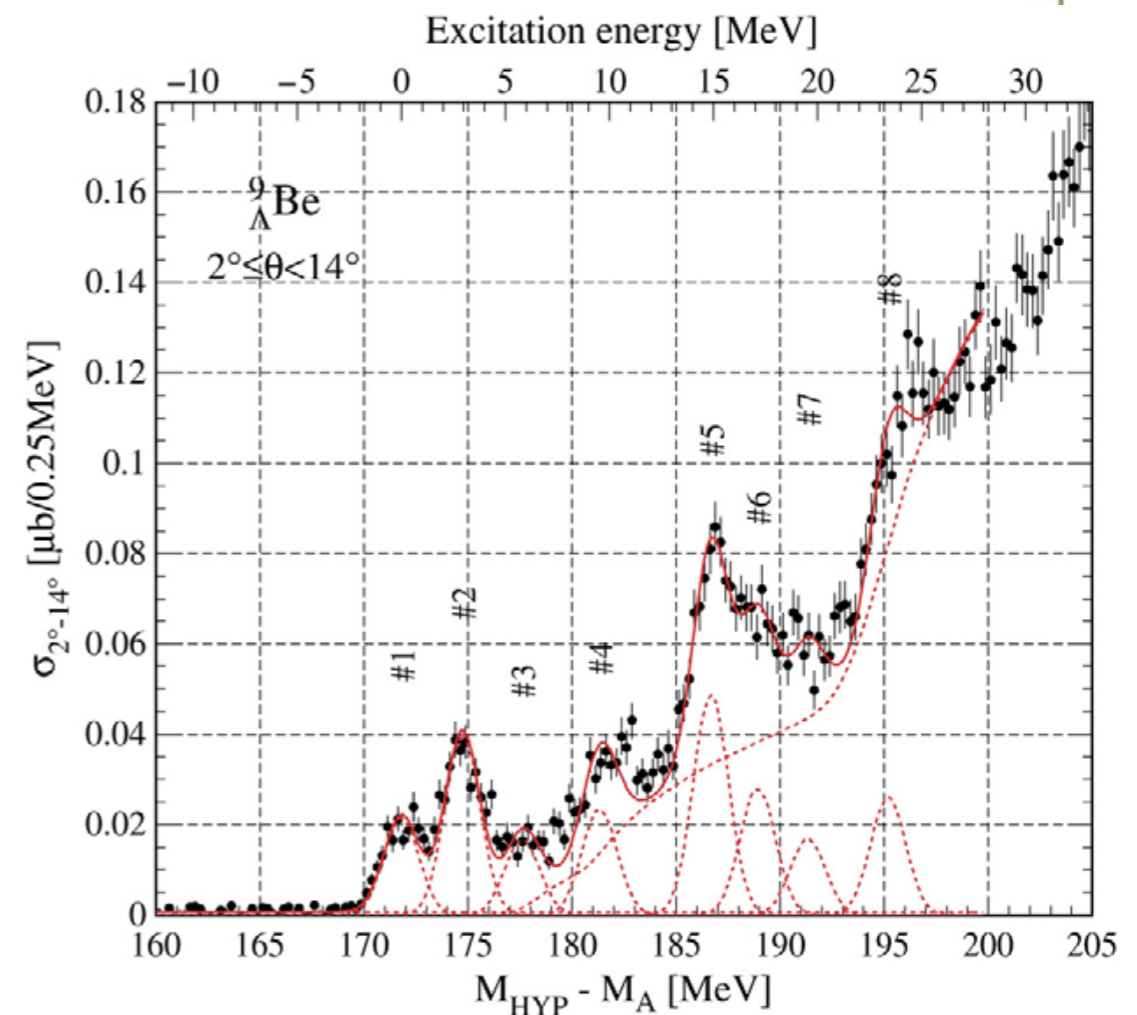
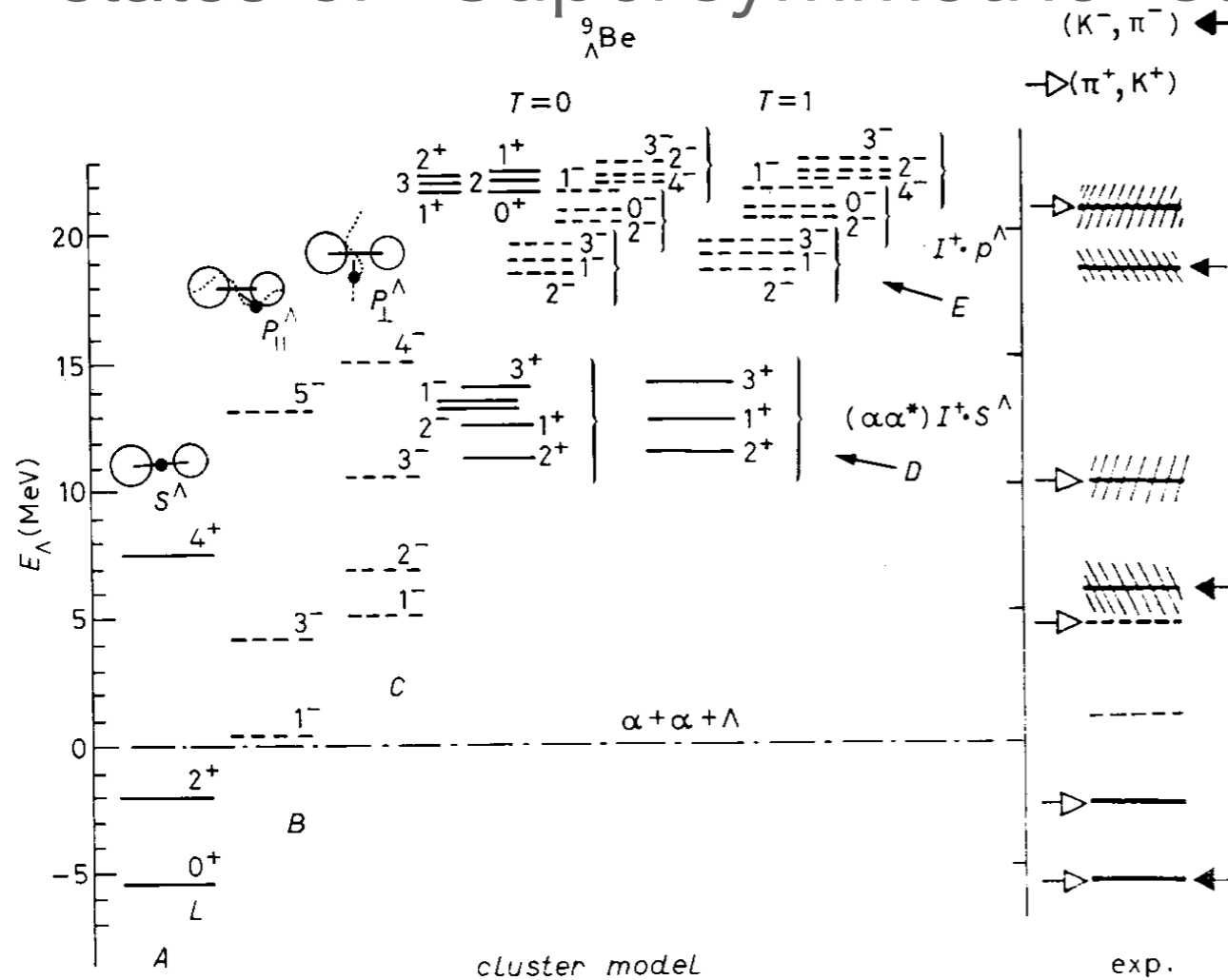
- T. Motoba, in HYP97 (Nucl. Phys. A 639 (1998) 135c.)

$$|{}_{\Lambda}^{12}\text{C}; J^+\rangle = [s^4 p^7]_{-} \otimes 1p^{\Lambda} + \left\{ [s^4 p^6 (sd)^1]_{+} + [s^3 p^8]_{+} \right\} \otimes 1s^{\Lambda}$$

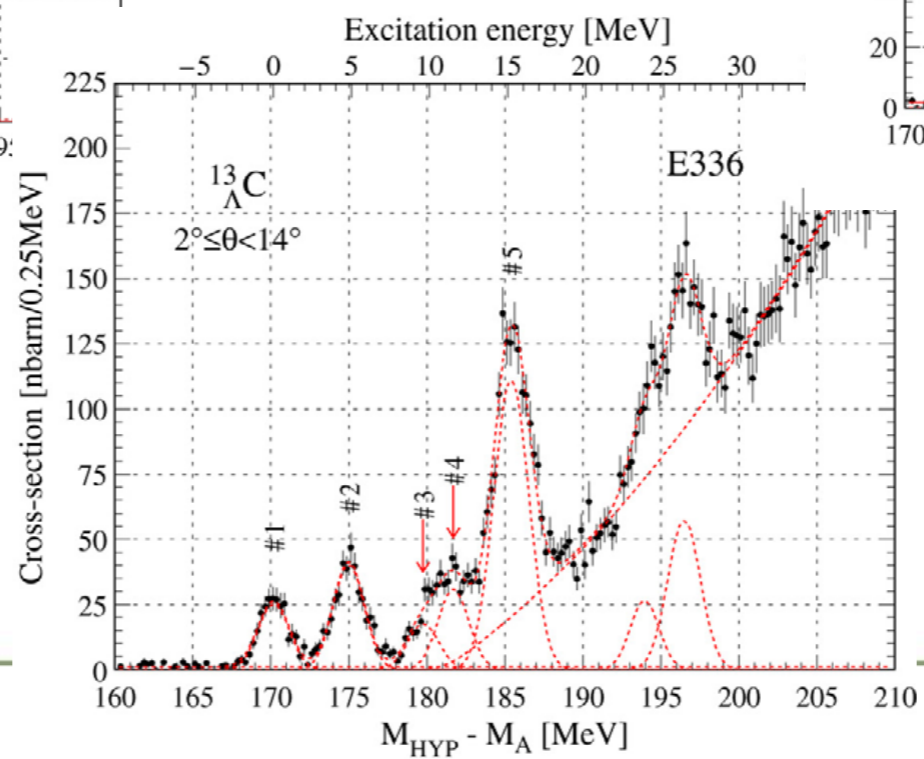
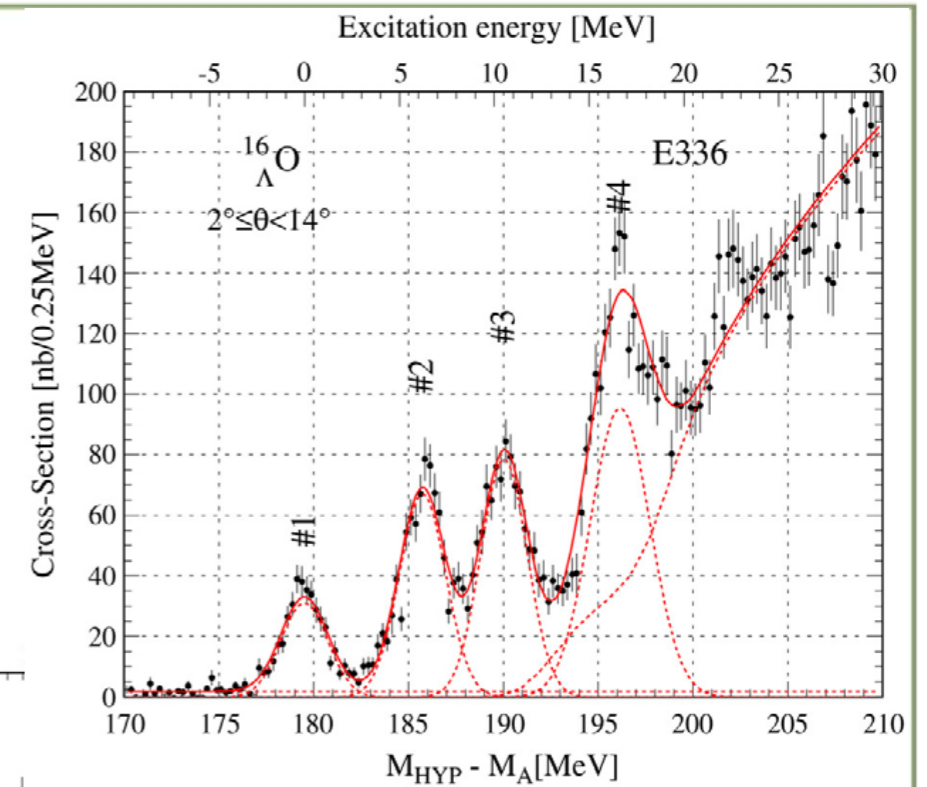
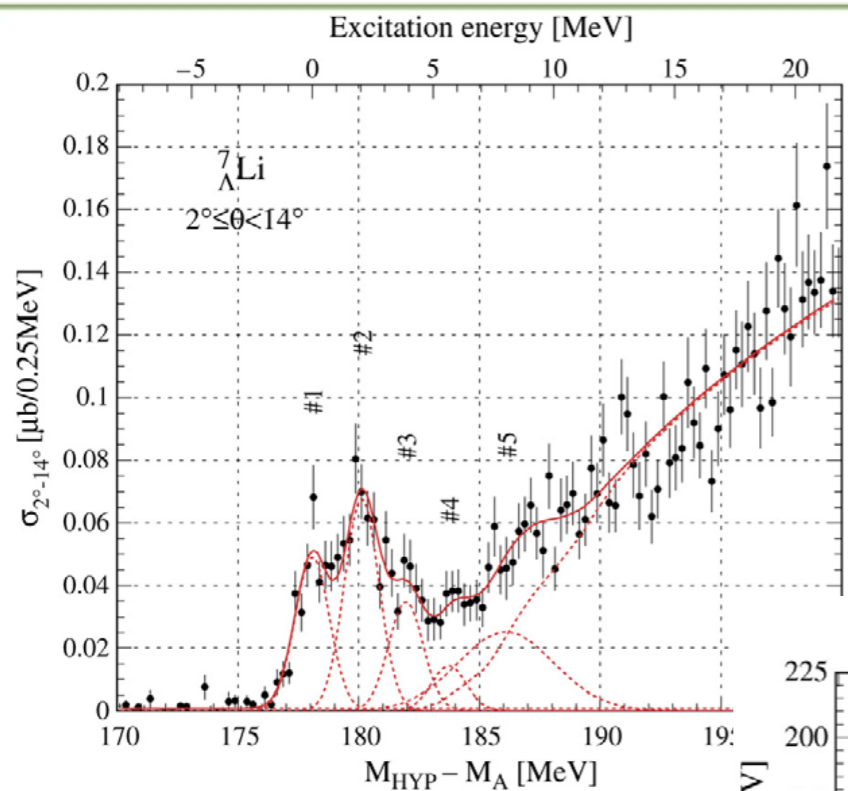


E336: ${}^9_{\Lambda}\text{Be}$

- Observation of “genuine” hypernuclear states or “Supersymmetric” states

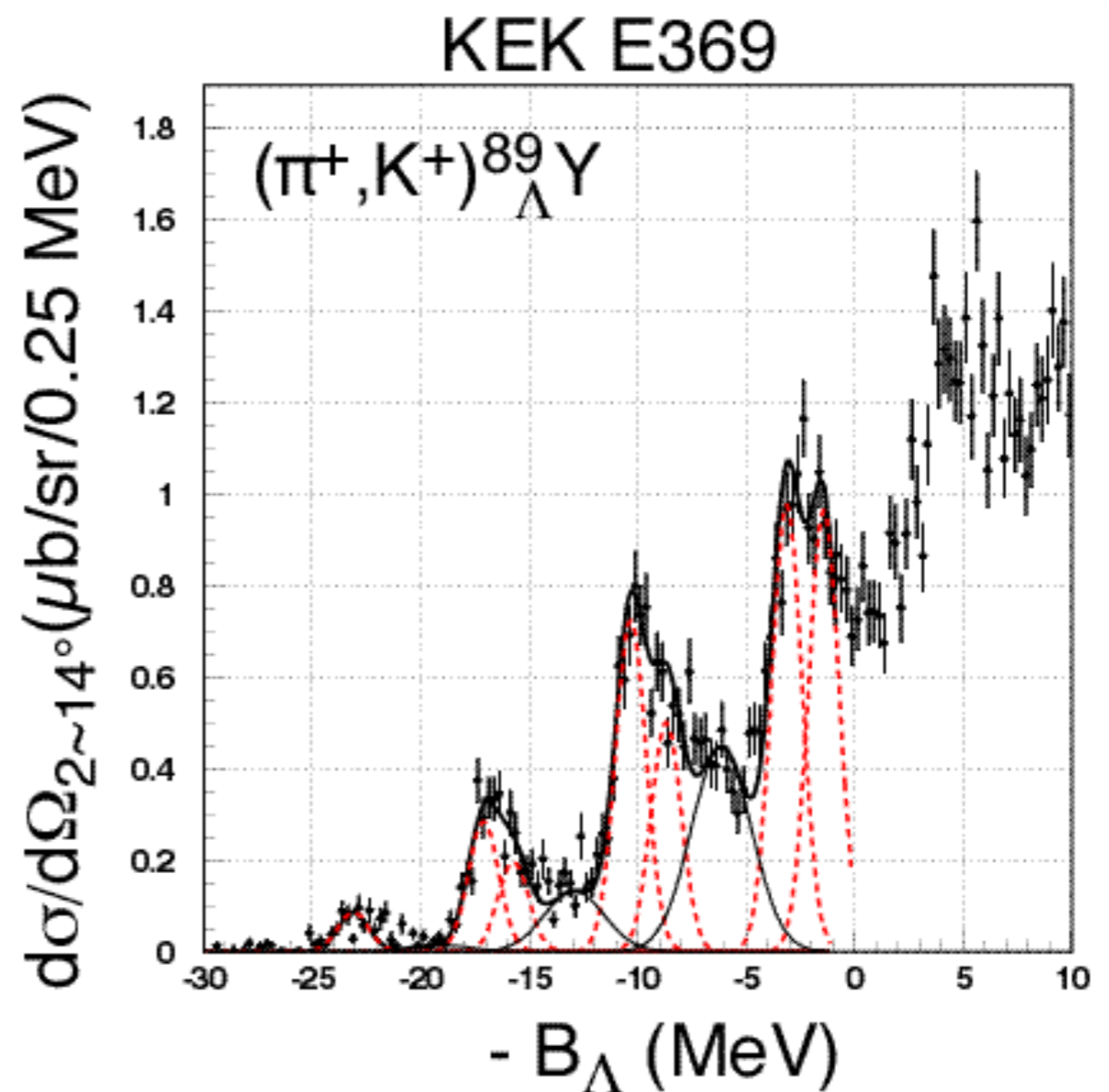


E336: $\Lambda^7\text{Li}$, $\Lambda^{13}\text{C}$, $\Lambda^{16}\text{O}$



E369: $\Lambda^{89}\text{Y}$

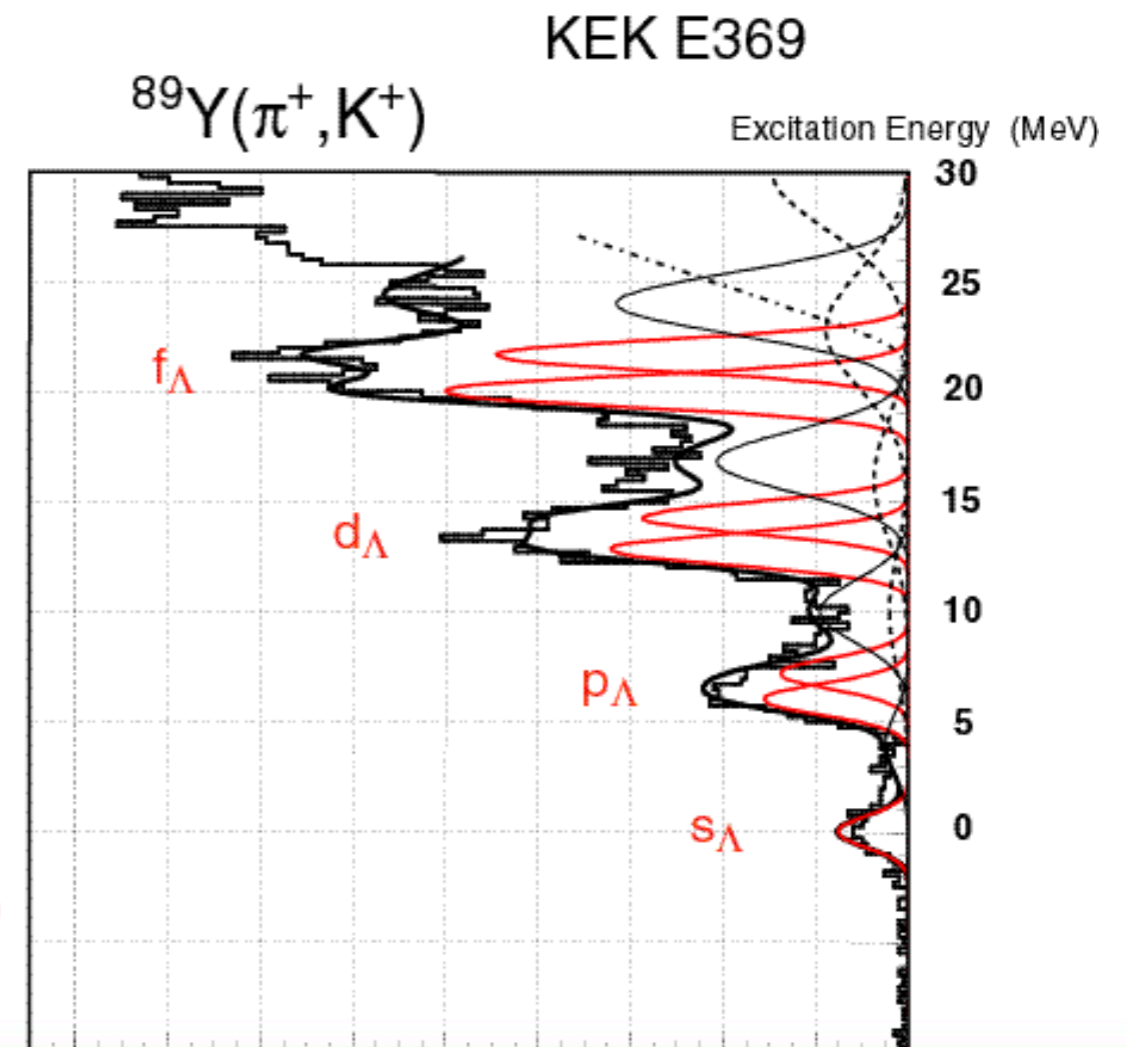
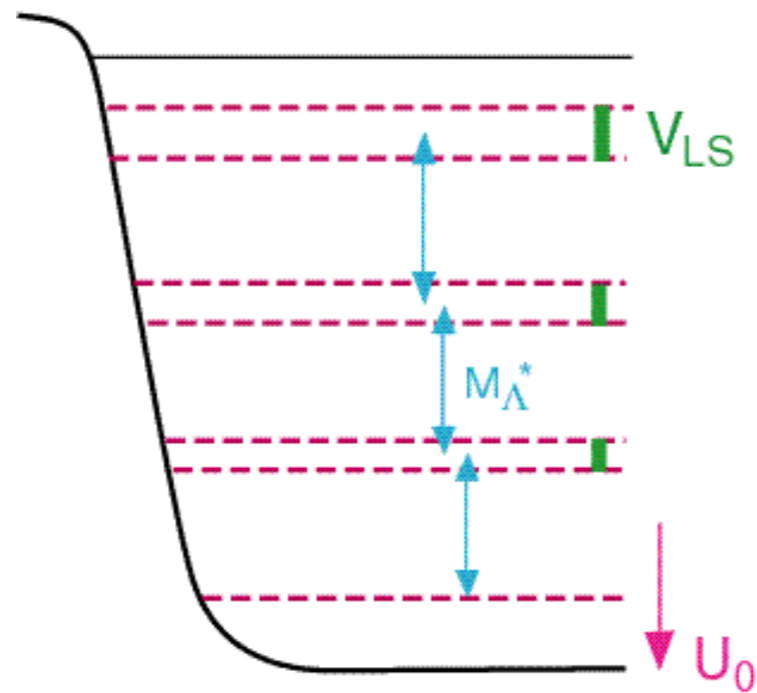
- $B_{\Lambda s} = 23.1 \pm 0.1$ MeV
- Energy Splitting
 - $\Delta E_f = 1.70 \pm 0.10$ MeV
 - $\Delta E_d = 1.63 \pm 0.14$ MeV
 - $\Delta E_p = 1.37 \pm 0.20$ MeV
- Peak Ratio
 - $R/L_f = 0.99 \pm 0.07$
 - $R/L_d = 0.69 \pm 0.06$
- Extra n-hole at $+4.1 \pm 0.1$ MeV, width = 3.2 ± 0.2 MeV



Single-particle motion of Λ in heavy hypernuclei

- $U_0 = -30.5$ MeV
- $M_{\Lambda}^* = 0.7 \sim 0.8 \times M_{\Lambda}$

by Y. Yamamoto



E369: $\Lambda^5 1V$

- Splitting in d-(and p-) orbit(s)

- $B_{\Lambda S} = (20 \pm 0.13) + 0.56$ MeV

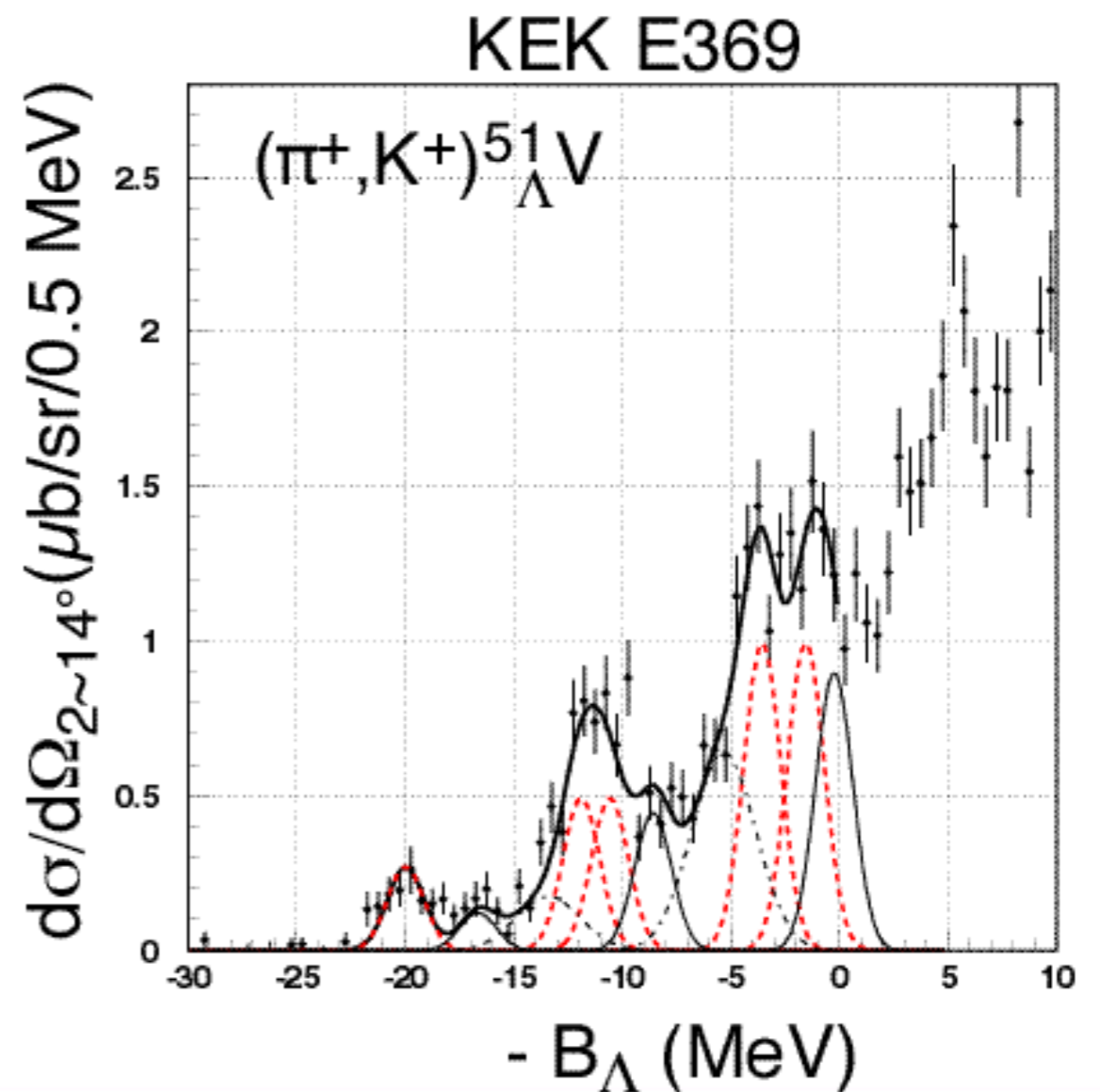
- Width = 1.95 MeV

- Peak Ratio = 1 (fixed)

- Extra n-holes

- At $+3.3 \pm 0.2$ MeV,
width = 1.95 MeV

- At $+6.6 \pm 0.2$ MeV,
width = 3.46 MeV



Heavy Λ -Hypernuclei

- *A bridge to strange matter*

- 2-body Y-N interaction

- Baryon-baryon interactions in $SU(3)_f$
 - Short range part: meson picture or quark picture ?

- Light hypernuclei ($A < \sim 20$)

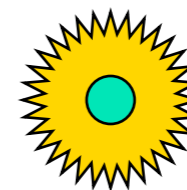
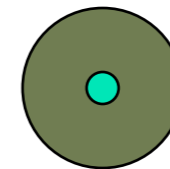
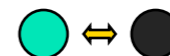
- Fine structure \longleftrightarrow Spin-dependent interactions
 - Cluster structure

- Heavy hypernuclei ($A > \sim 80$)

- Single-particle potential: $U_0(r), m_{\Lambda}^*(r), V_{\Lambda NN}, \dots$

- Neutron star ($A \sim 10^{57}$): $\rho > 5 \rho_0$

- Hyperonization \longrightarrow Softening of E.O.S.
 - Superfluidity



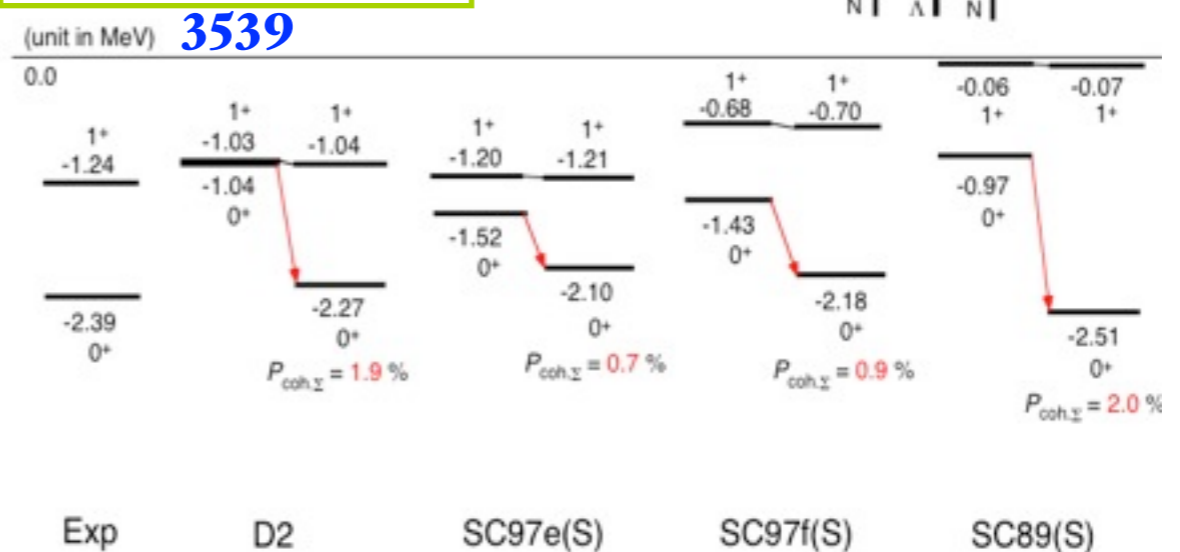
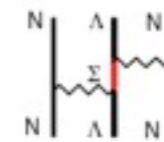
E52 I: Production of neutron-rich Λ hypernuclei by the (π^-, K^+) double-charge-exchange reaction

A pilot experiment for spectroscopic studies of
the neutron-rich Λ hypernuclei via the (π^-, K^+) reaction

Production cross section/ Background (sensitivity)
⇒ Understanding of the Reaction Mechanism

Akaishi et al.
PRL 84(2000)

${}^4_\Lambda\text{He}$



Λ - Σ coherent coupling in $A=4$ hypernuclei

...solved an underbinding problem,
known as an overbinding problem in

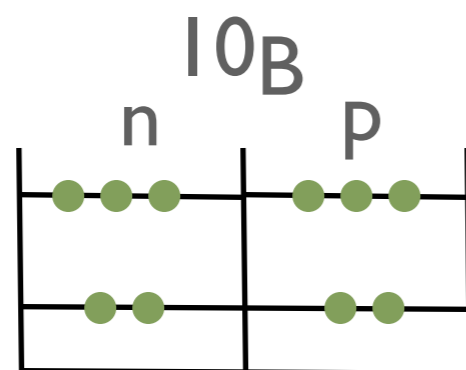
$5 \Lambda \text{He}$

Y.Akaishi *et al.*, PRL84(2000)3539

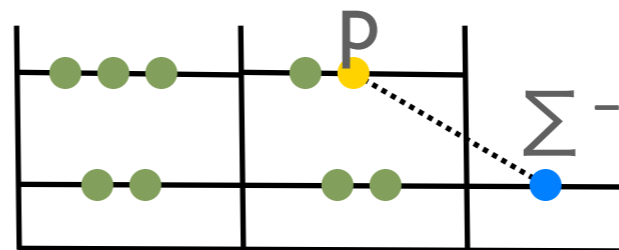
To be confirmed/examined in other examples

In the (π, K^+) reaction...

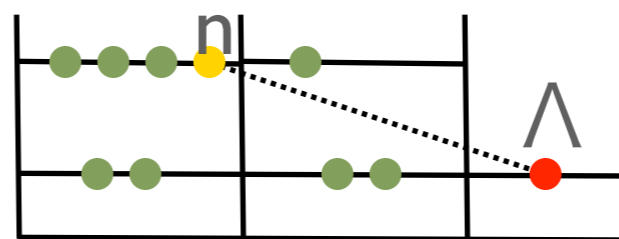
(KEK-E521, Fukuda *et al.*)



Two-step



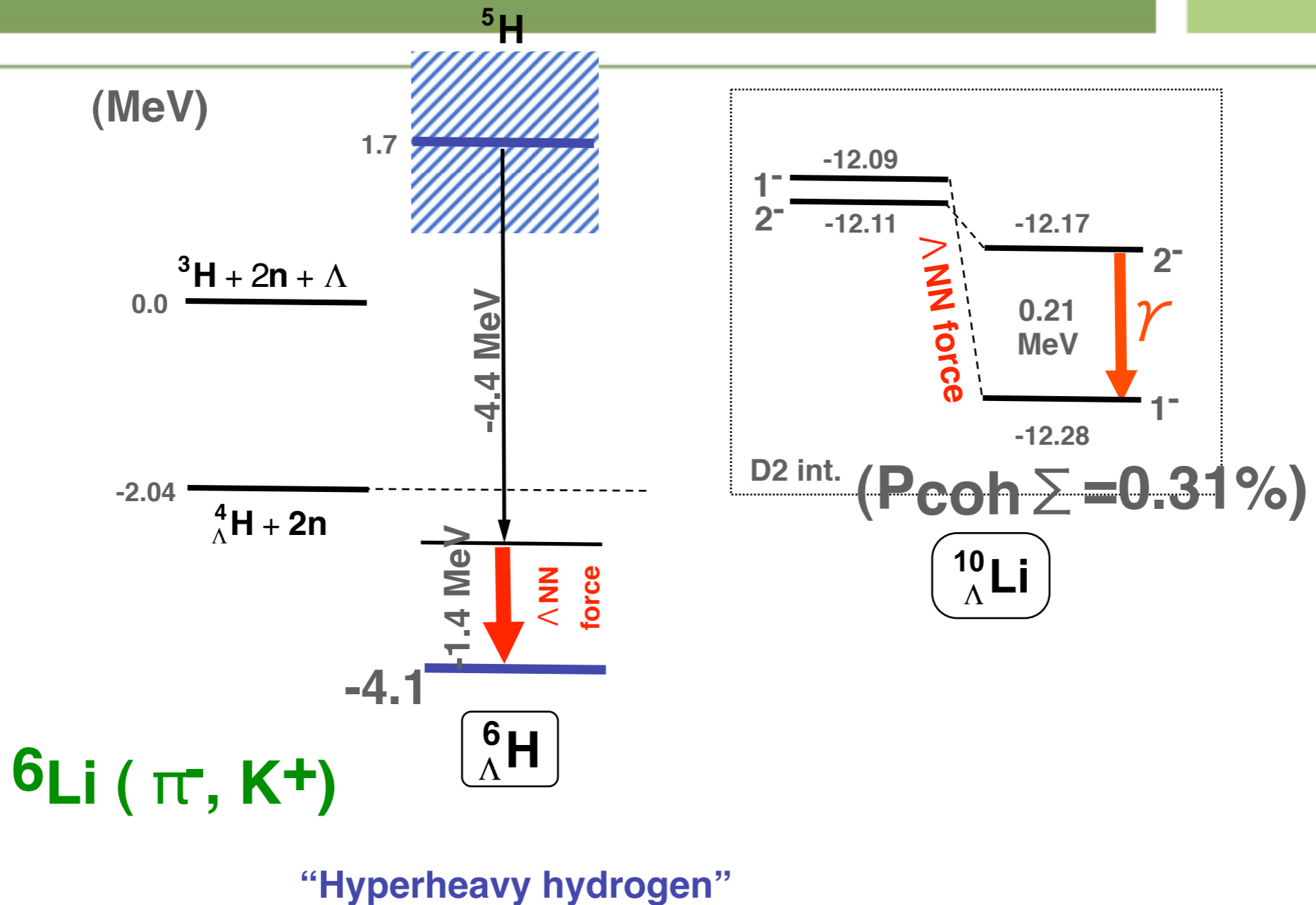
Coherent coupling



$10 \Lambda \text{Li}$

Effect of Coherent Σ mixing in n-rich hypernuclei

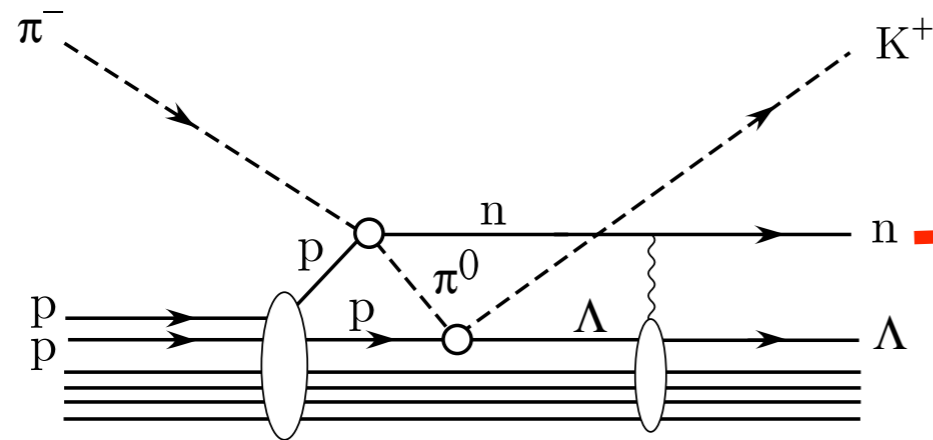
Superheavy hydrogen



Reaction mechanism

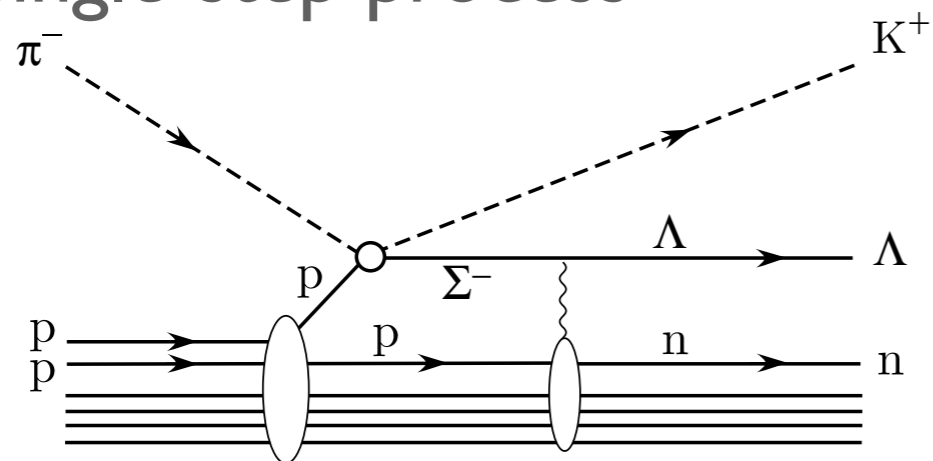
Tretyakova, Akaishi et al.

► Two-step process:



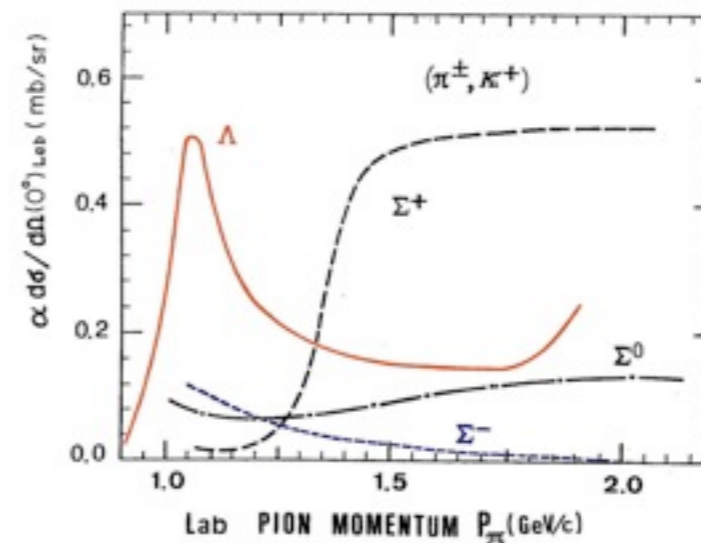
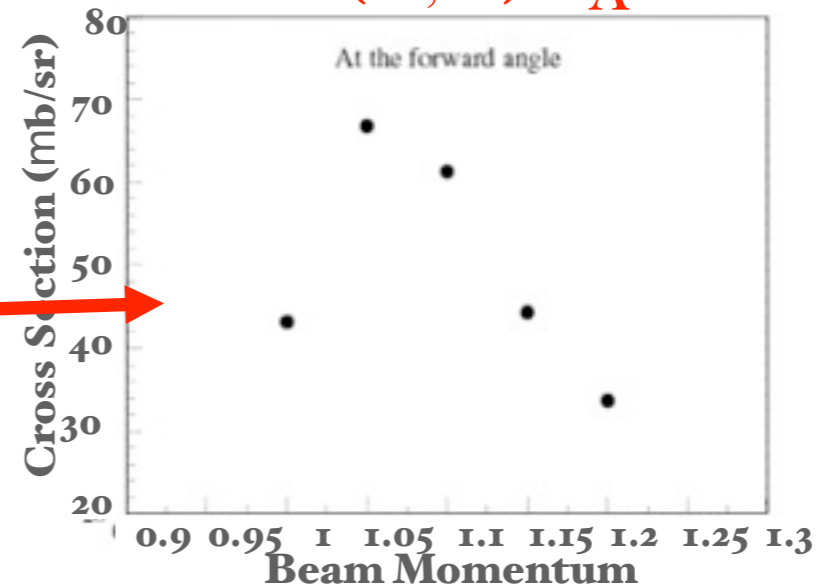
(a)

► Single-step process



(b)

$^{10}\text{B}(\pi^-, \text{K}^+)^{10}\text{B} \Lambda \text{Li}$



Experimental Results

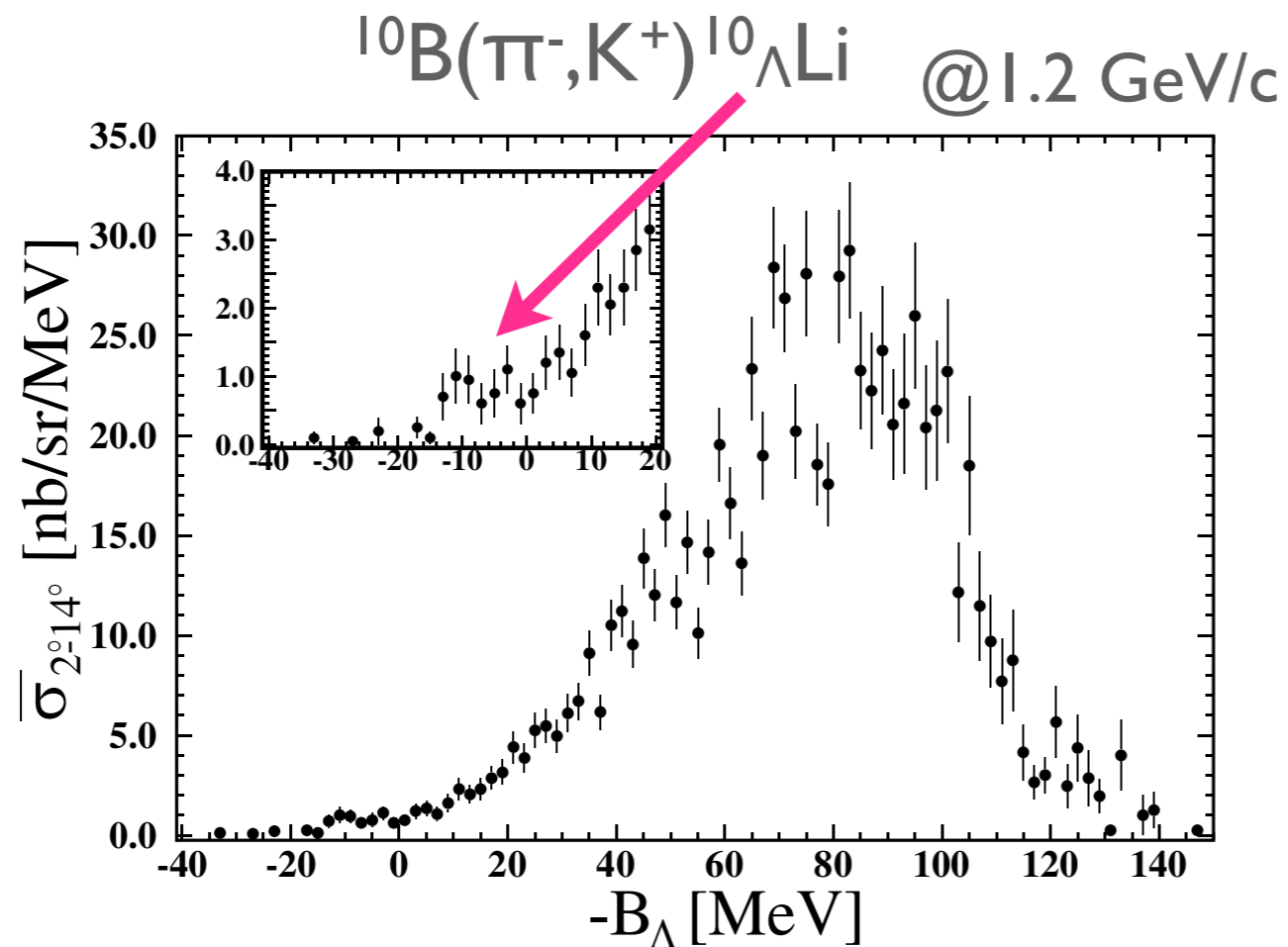


FIG. 3. Missing-mass spectrum of the (π^-, K^+) reaction on a ^{10}B target at 1.2 GeV/c. The horizontal and vertical axes are the same as Fig. 2. An expanded view near the Λ bound region is shown in the inset.

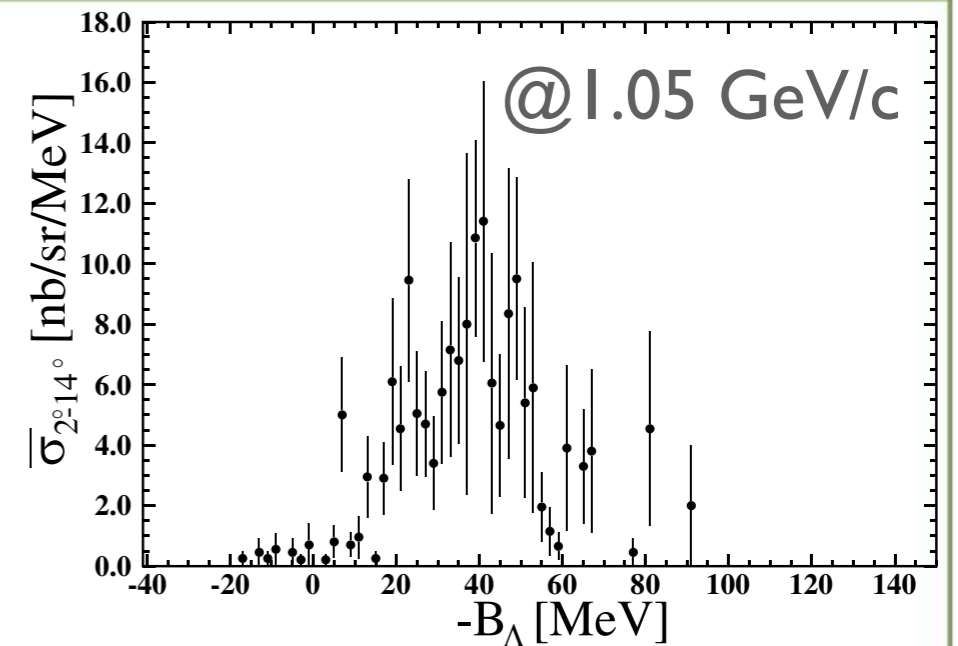


FIG. 2. Missing-mass spectrum of the (π^-, K^+) reaction on a ^{10}B target at 1.05 GeV/c. The horizontal axis shows the binding energy of a Λ , whereas the vertical axis shows the cross section in terms of nb/sr/MeV.

Ratio of the Λ production cross section (π^-, K^+) to (π^+, K^+)

TABLE I. Hypernuclear production cross sections for the bound region averaged over the scattering angle from 2° to 14° . The cross section with an asterisk shows a lower limit by extrapolating the quasifree components linearly. The quoted errors are statistical.

Reaction	Cross Section	
	1.05 GeV/ c	1.2 GeV/ c
$^{12}\text{C}(\pi^+, K^+)_{\Lambda}^{12}\text{C}$	$18.0 \pm 0.7 \mu\text{b/sr}$	$17.5 \pm 0.6 \mu\text{b/sr}$
$^{10}\text{B}(\pi^+, K^+)_{\Lambda}^{10}\text{B}$	$7.8 \pm 0.3 \mu\text{b/sr}$	
$^{10}\text{B}(\pi^-, K^+)_{\Lambda}^{10}\text{Li}$	$5.8 \pm 2.2 \text{ nb/sr}$	$11.3 \pm 1.9 \text{ nb/sr}$ $9.6 \pm 2.0^* \text{ nb/sr}$

Σ mixing ?

- ▶ T. Harada et al., PRC 79 (2009) 014603.

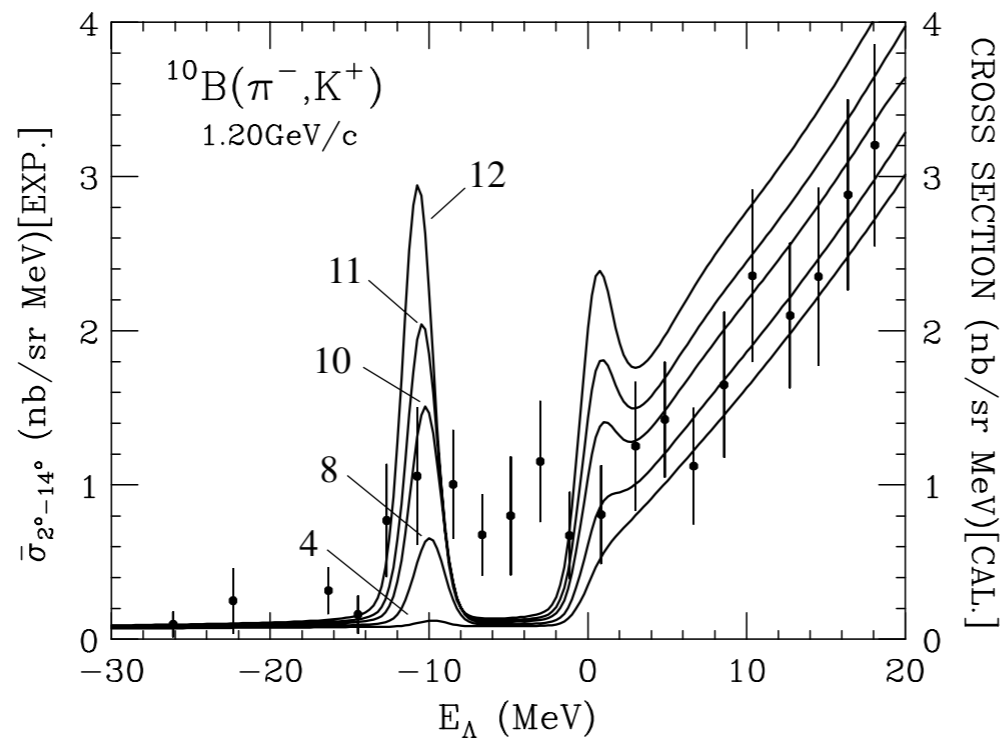


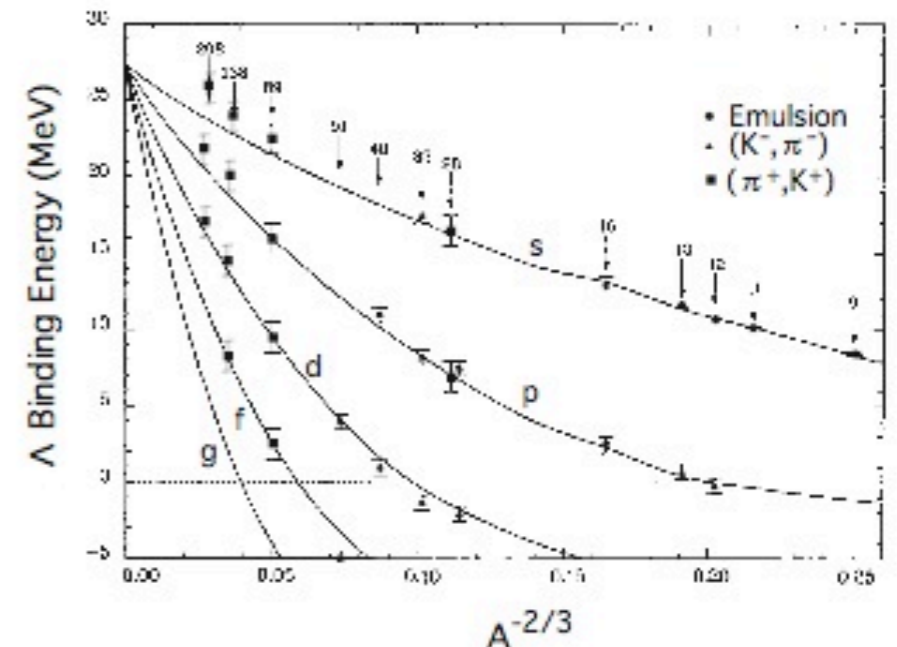
FIG. 3. Calculated inclusive Λ spectra obtained by the one-step mechanism near the Λ threshold in the $^{10}\text{B}(\pi^-, K^+)$ reaction at $1.20 \text{ GeV}/c$ (6°), by changing $V_{\Sigma\Lambda}$ for the Λ - Σ coupling potential. The experimental data are taken from Ref. [12]. The solid curves denote $V_{\Sigma\Lambda} = 4, 8, 10, 11,$ and 12 MeV when $-W_\Sigma = 20 \text{ MeV}$, with a detector resolution of 2.5 MeV FWHM .

$$P_\Sigma \sim 0.47 - 0.68\%$$

Summary

on (π, K) spectroscopy

- ▶ The (π, K) Spectroscopy has been successful.
 - ▶ Gross feature of Single-particle levels of Λ
 - ▶ Effective for Heavy Λ hypernuclei
 - ▶ *High-resolution spectroscopy ($\Delta E \sim 0.2$ MeV) will be interesting*
 - ▶ Possibility to study neutron-rich hypernuclei with (π^-, K^+)



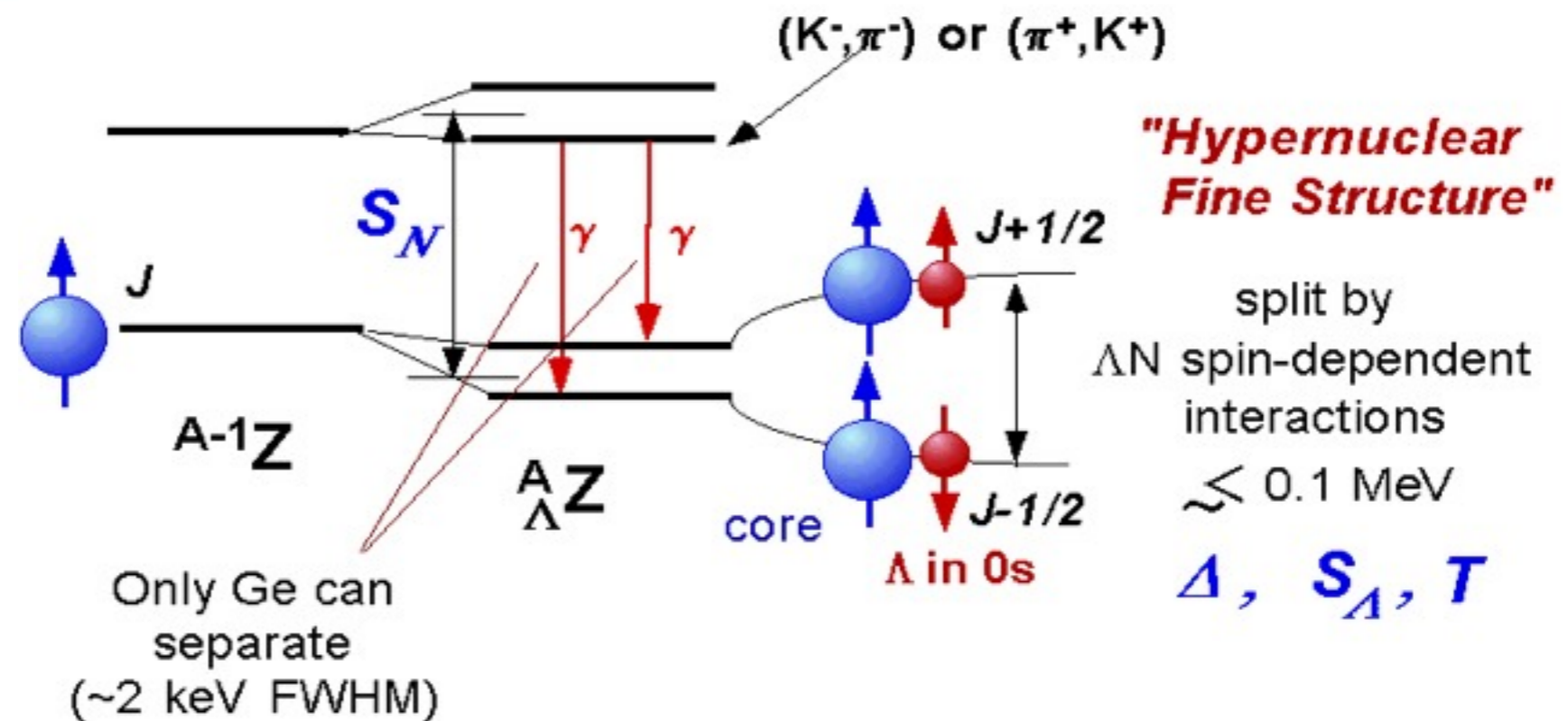


Second day in UT



γ spectroscopy

- Low-lying levels of Λ hypernucleus



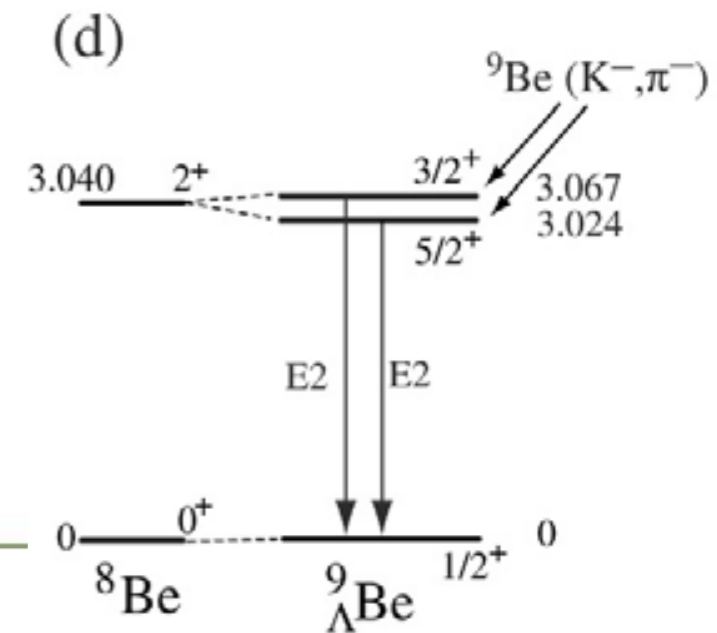
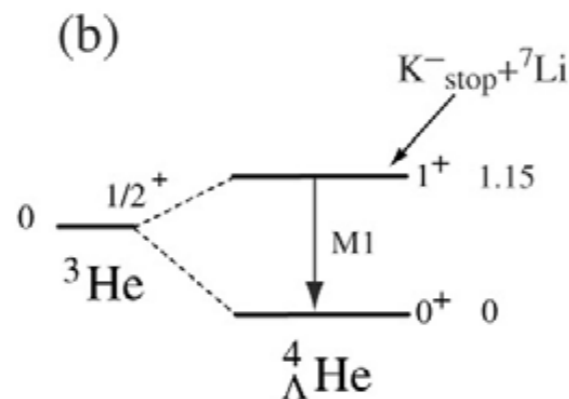
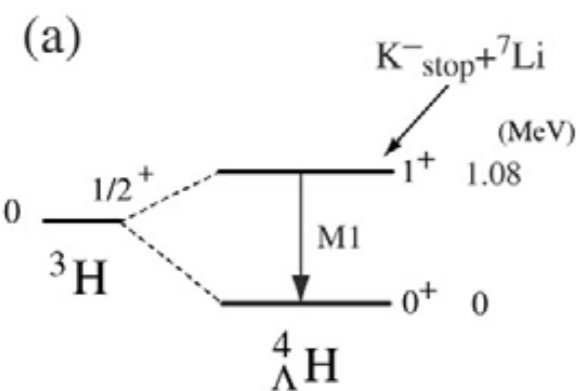
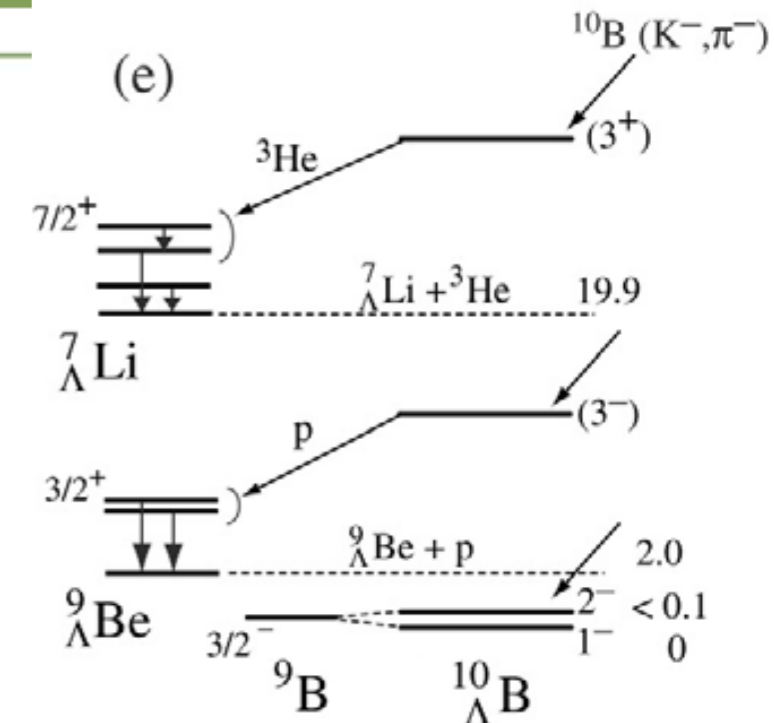
- 2-body ΛN effective interaction

$$V_{\Lambda N}^{\text{eff}} = V_0(r) + \underset{\Delta}{V_\sigma(r)} \vec{s}_\Lambda \vec{s}_N + \underset{S_A}{V_\Lambda(r)} \vec{l}_{\Lambda N} \vec{s}_\Lambda + \underset{S_N}{V_N(r)} \vec{l}_{\Lambda N} \vec{s}_N + \underset{T}{V_T(r)} S_{12}$$

p-shell : 4 radial integrals for $p_N s_\Lambda$ w.f.

Hypernuclear γ -rays before Hyperball

${}^4_{\Lambda}\text{H}, {}^4_{\Lambda}\text{He}$	$1.10 \pm 0.04 \text{ MeV}$	Nal
${}^7_{\Lambda}\text{Li}$	$2.034 \pm 0.023 \text{ MeV}$	Nal
${}^9_{\Lambda}\text{Be}$	$3.079 \pm 0.04 \text{ MeV}$	Nal
${}^{10}_{\Lambda}\text{B}$	not observed	Ge



Hyperball

(Tohoku/ Kyoto/ KEK, 1998)

- Large acceptance for small hypernuclear γ yields

Ge (r.e. 60%) x 14

$\Delta\Omega \sim 15\%$

$\eta_{\text{peak}} \sim 3\%$ at 1 MeV

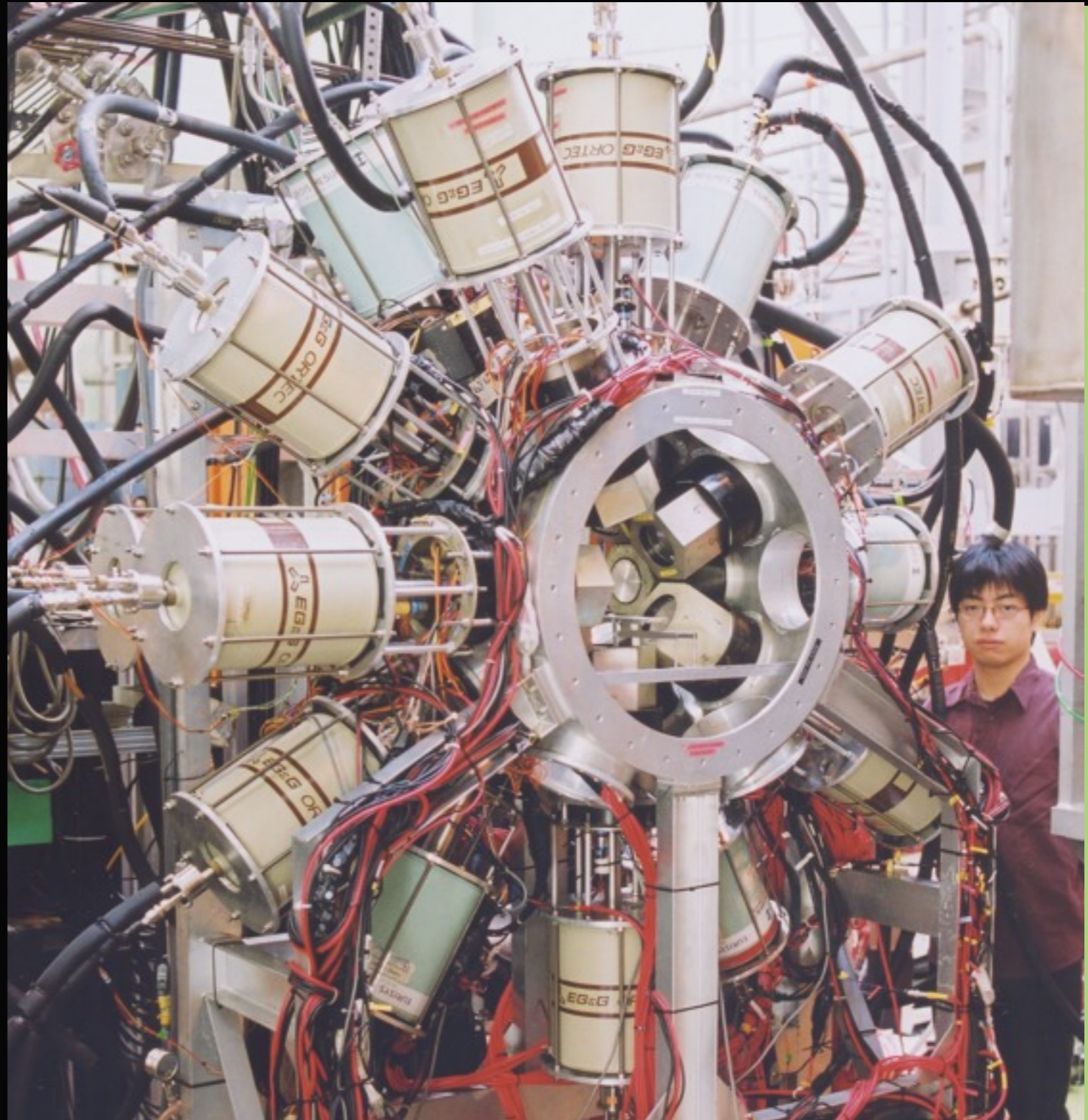
- High-rate electronics for huge background

1 TeV/sec, 100 kHz

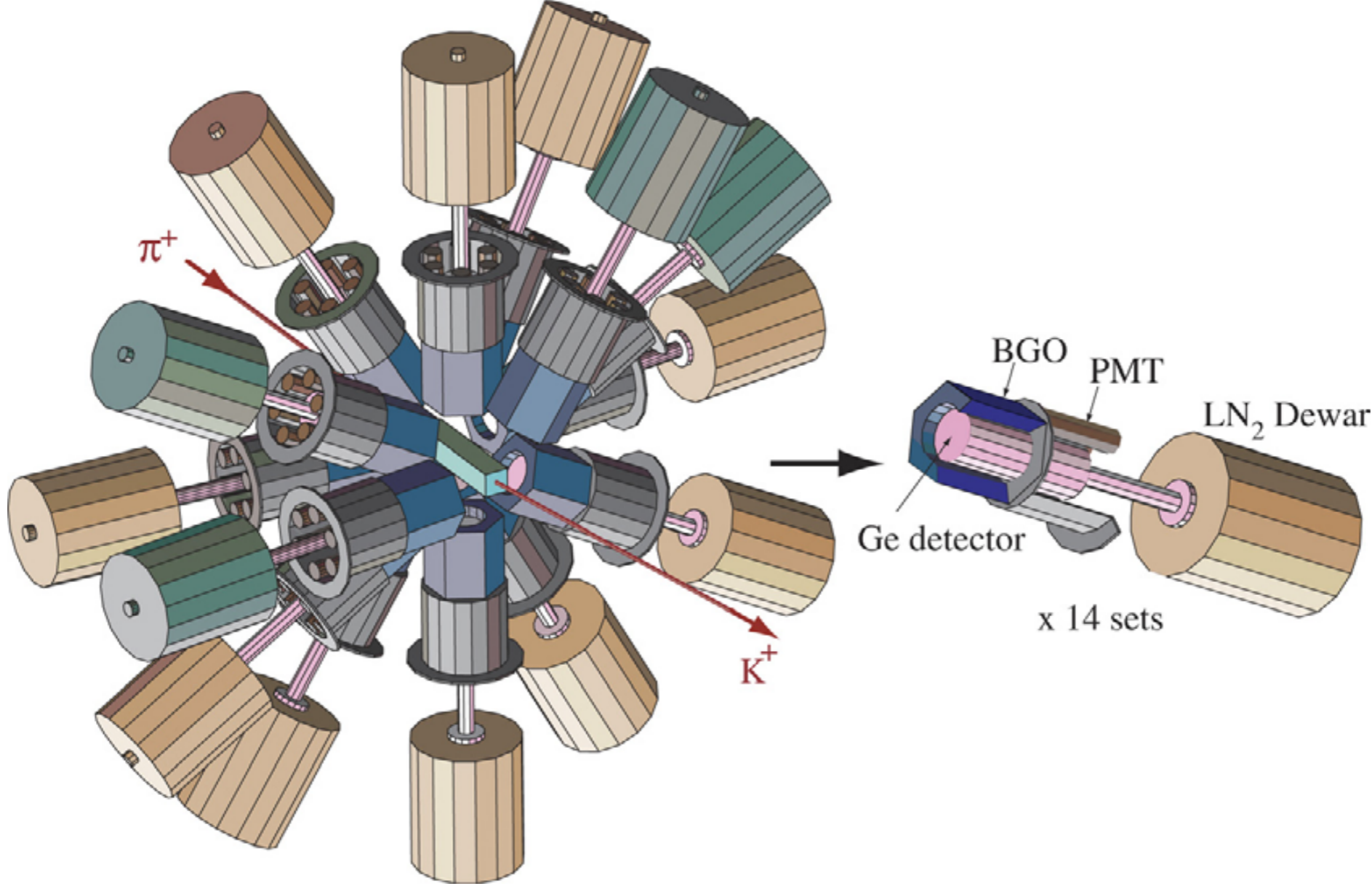
- BGO counters for π^0 and Compton suppression

Resolution of hypernuclear spectroscopy

1 MeV \rightarrow 2 keV FWHM

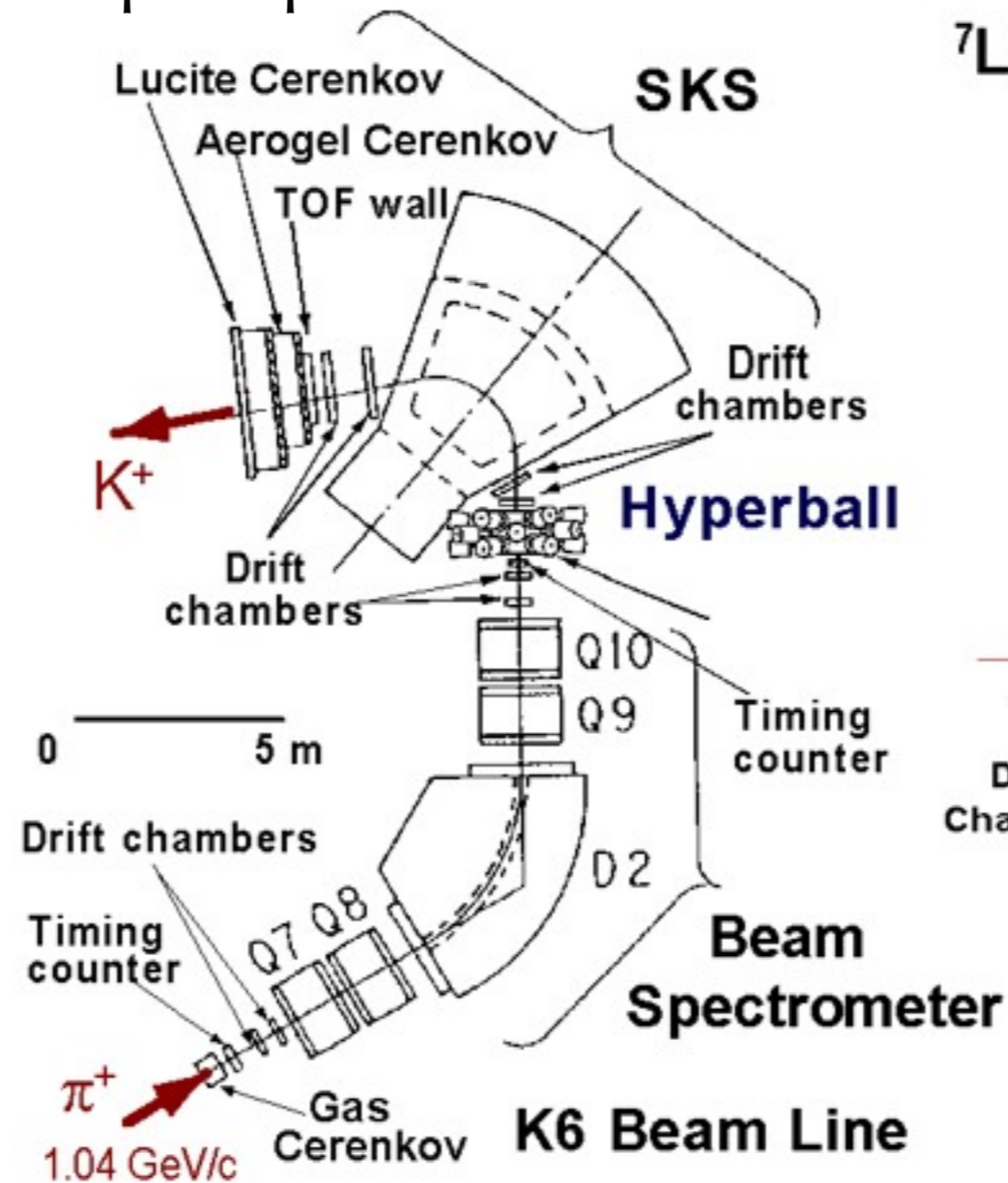


Hyperball

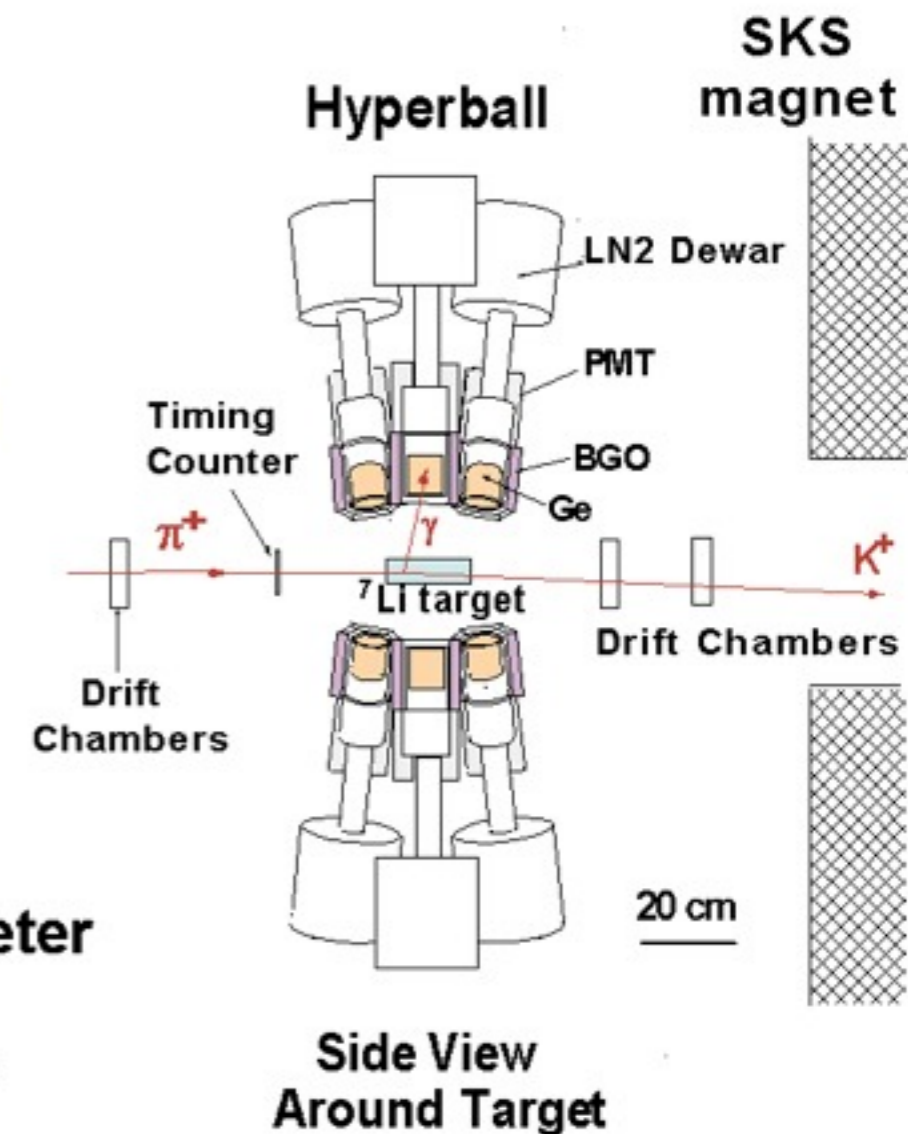
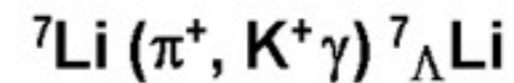


E419: γ spectroscopy of ${}^7_{\Lambda}\text{Li}$

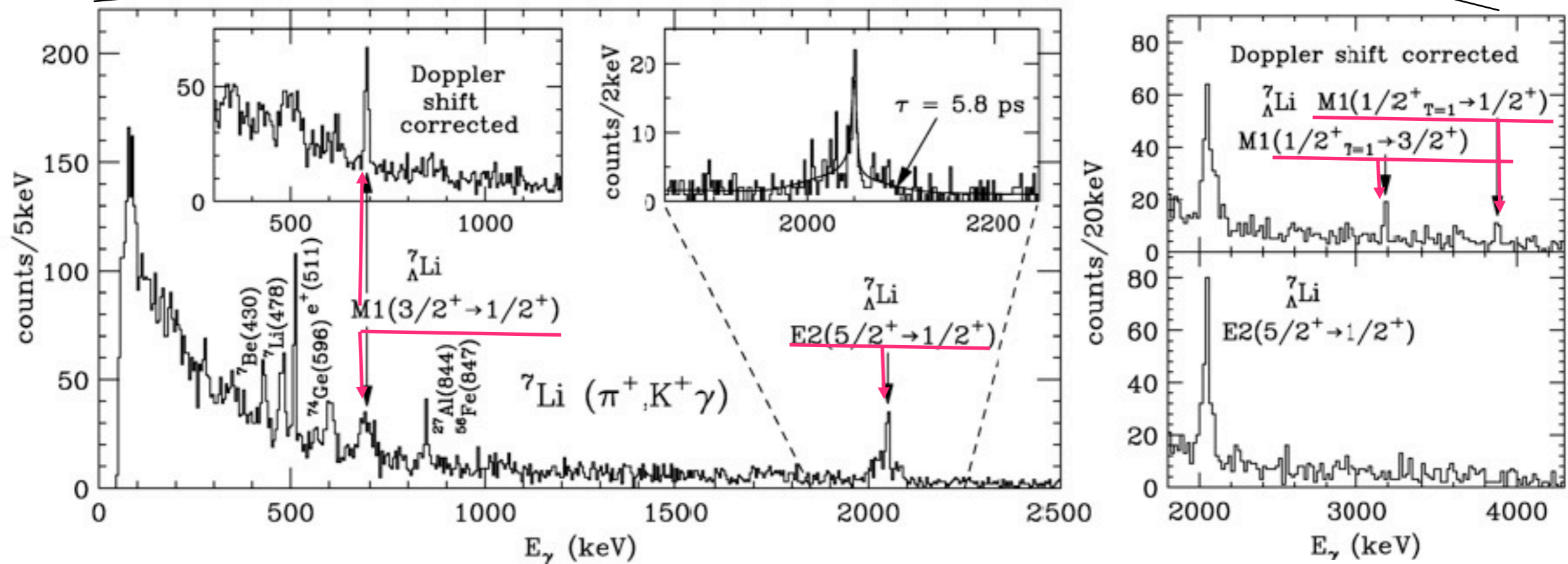
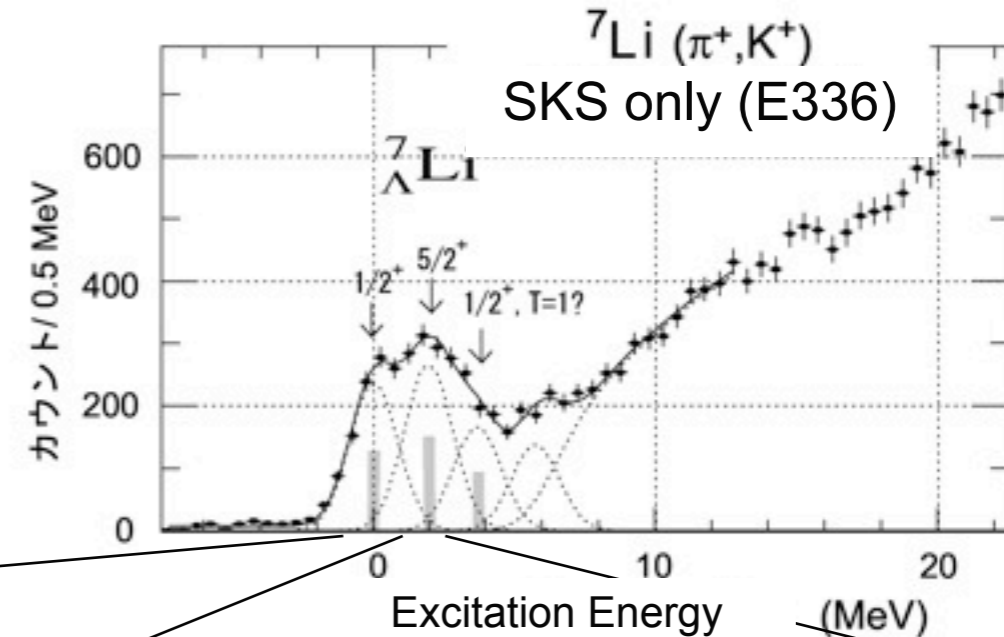
- ▶ First exp. with Hyperball
- ▶ B(E2) \rightarrow shrinking effect
- ▶ Spin-flip M1 \rightarrow Λ N spin-spin force



Setup for KEK-E419

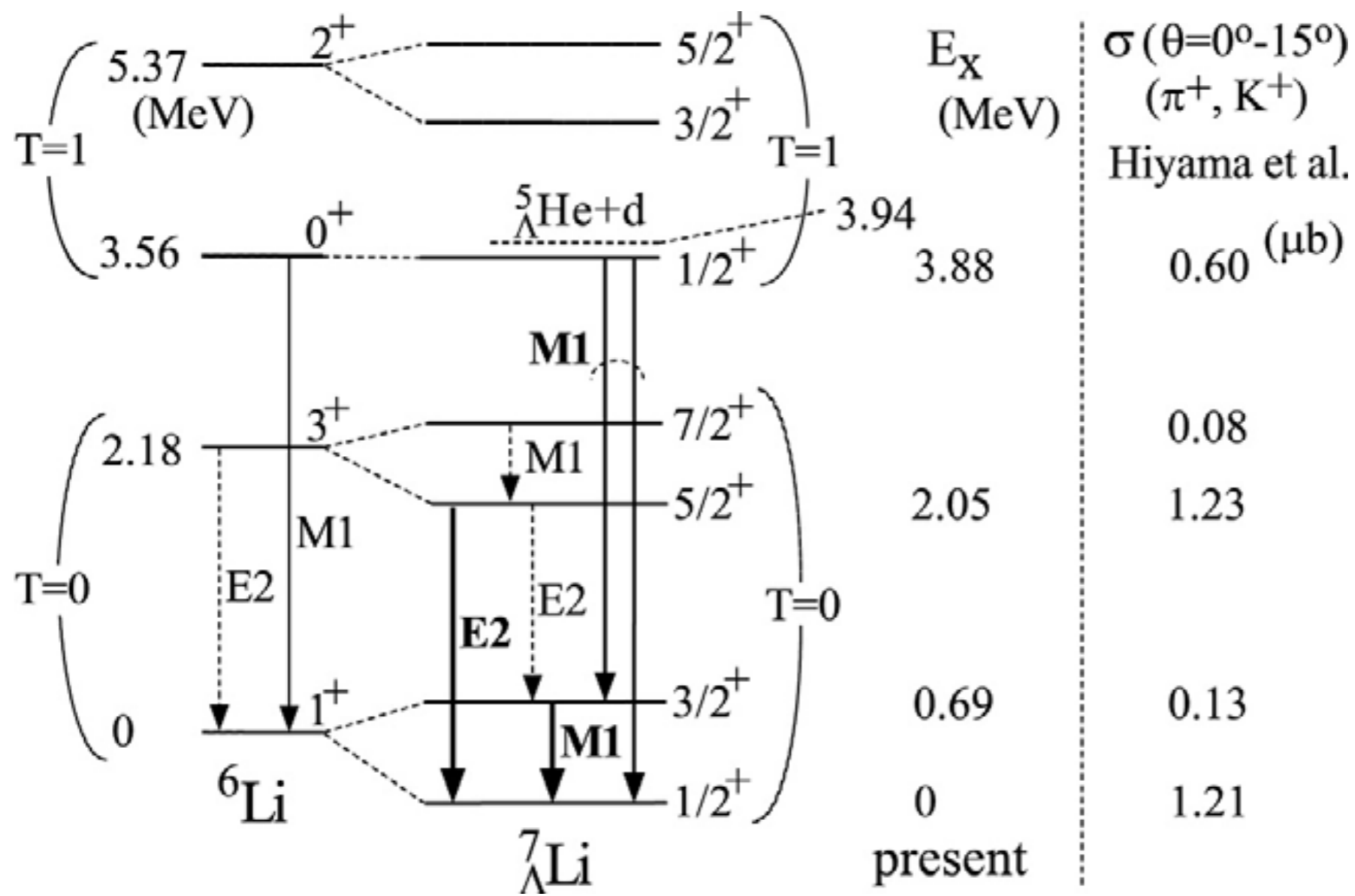


E419: SKS+Hyperball



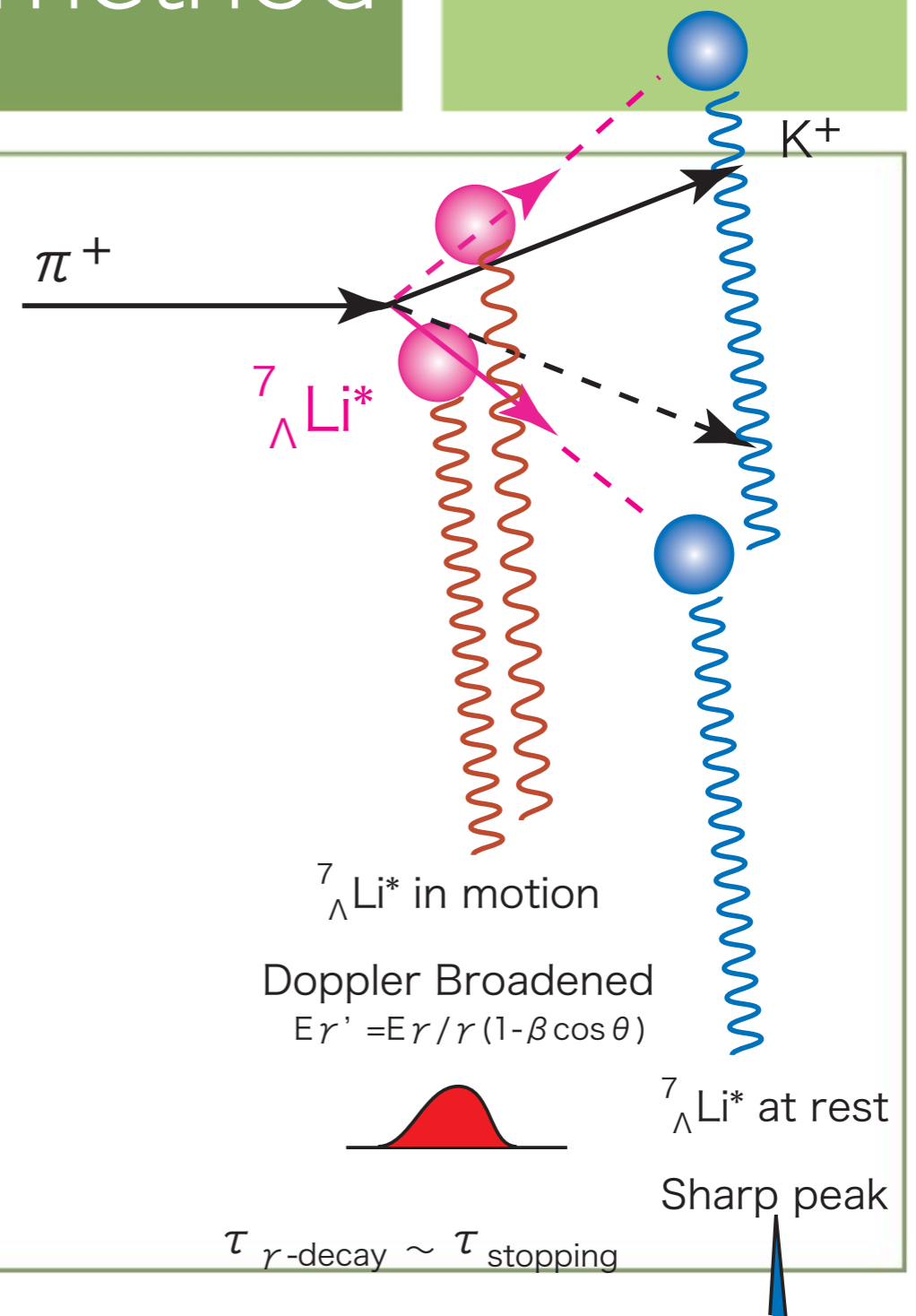
Tamura et al., PRL 94(2000) 5963

First observation of well-identified hypernuclear γ rays with Ge.



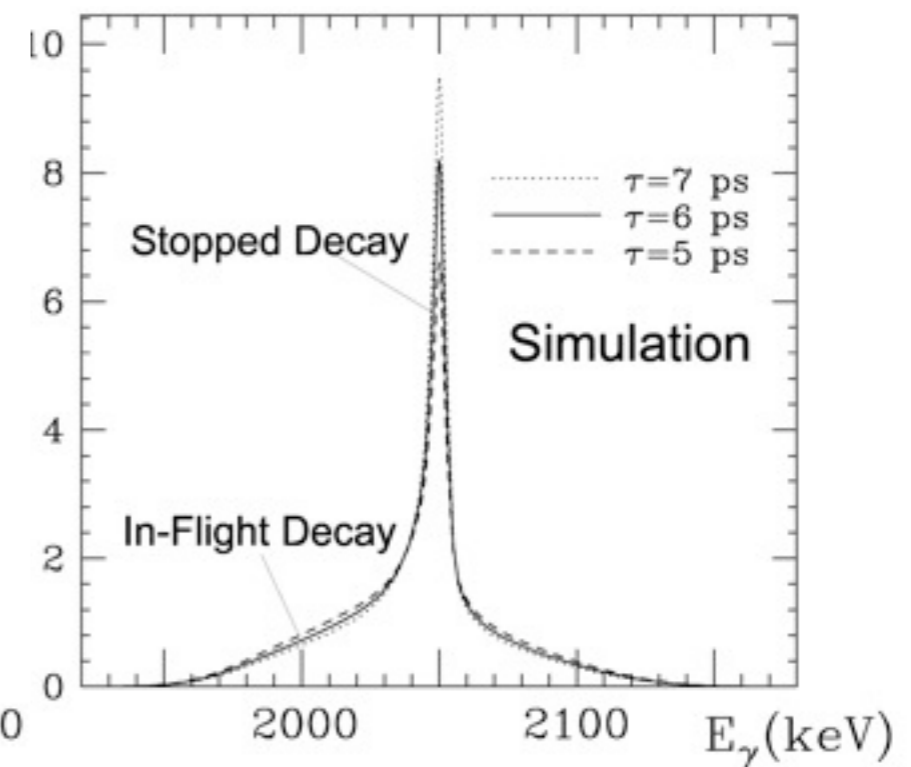
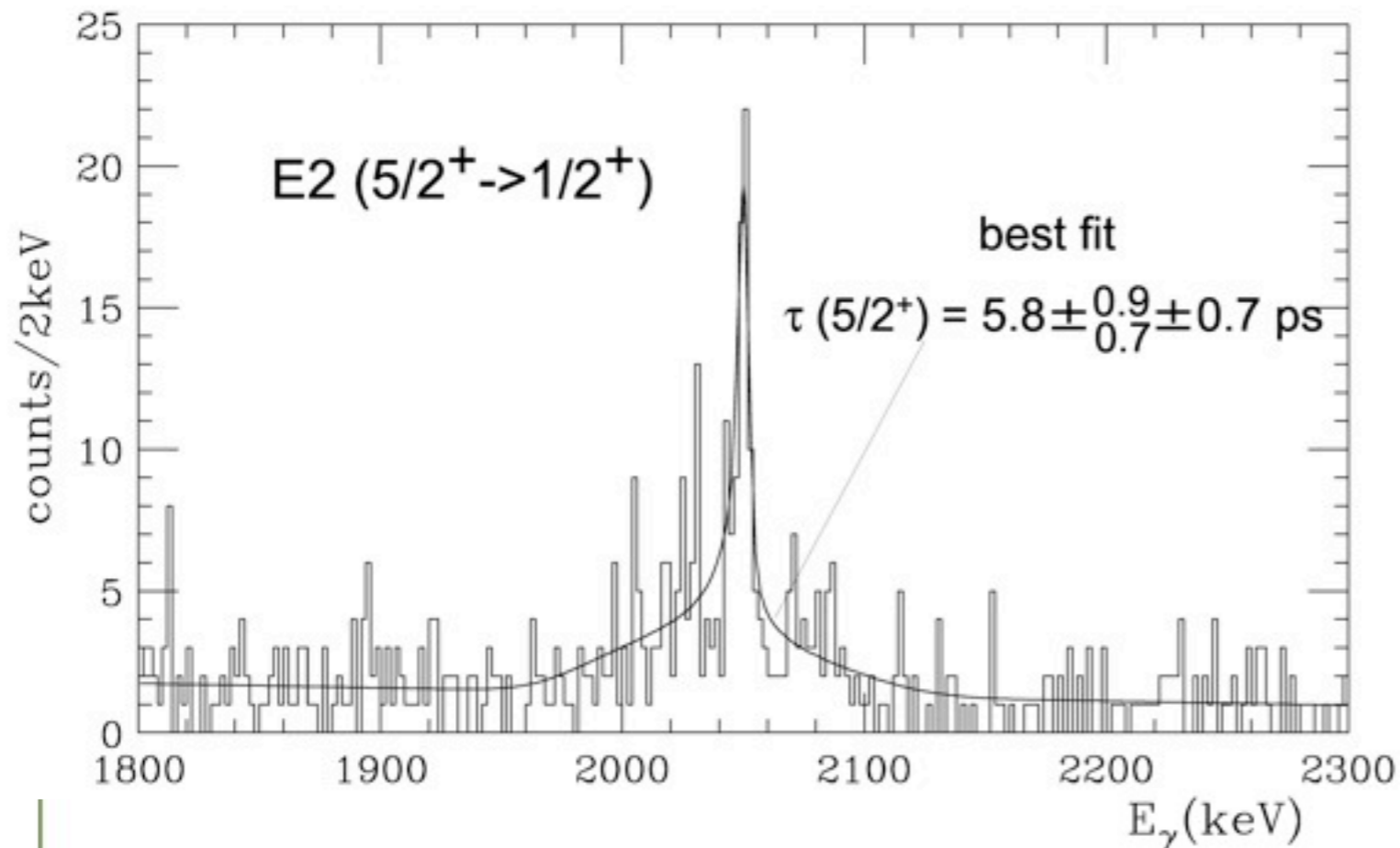
Doppler shift attenuation method

- ▶ $\tau_{\gamma\text{-decay}} \sim \tau_{\text{stopping}}$
- ▶ 5.8 ps 13 ps
- ▶ mixture of a sharp peak and a broad peak



Lifetime and B(E2)

Lifetime Measurement
using Doppler Shift Attenuation Method



$$\Gamma(E2; 5/2^+ \rightarrow 1/2^+) = BR / \tau (5/2^+) = 1.22 \times 10^9 E^5 B(E2)$$

$$BR = 93.6 \pm 3.8 \%$$

$$[\text{weak decay } (230 \pm 40 \text{ ps})^{-1}, BR(5/2^+ \rightarrow 3/2^+) = 3.8 \pm 0.5\%]$$

$$\Rightarrow B(E2) = 3.6 \pm 0.5 \pm 0.5 / 0.4 e^2 \text{fm}^4$$

B(E2)

$$\Gamma(E(M)\lambda : I_i \rightarrow I_f) = \frac{8\pi(\lambda + 1)}{\lambda[(2\lambda + 1)!!]^2} \frac{1}{\hbar} \left(\frac{\omega}{c}\right)^{2\lambda+1} B(E(M)\lambda; I_i \rightarrow I_f)$$

$$\begin{aligned} B(E(M)\lambda; I_i \rightarrow I_f) &= \sum_{\mu M_f} |\langle I_f M_f | \mathcal{M}(E(M)\lambda, \mu) | I_i M_i \rangle|^2 \\ &= \frac{1}{2I_i + 1} |\langle I_f || \mathcal{M}(E(M)\lambda) || I_i \rangle|^2 \end{aligned}$$

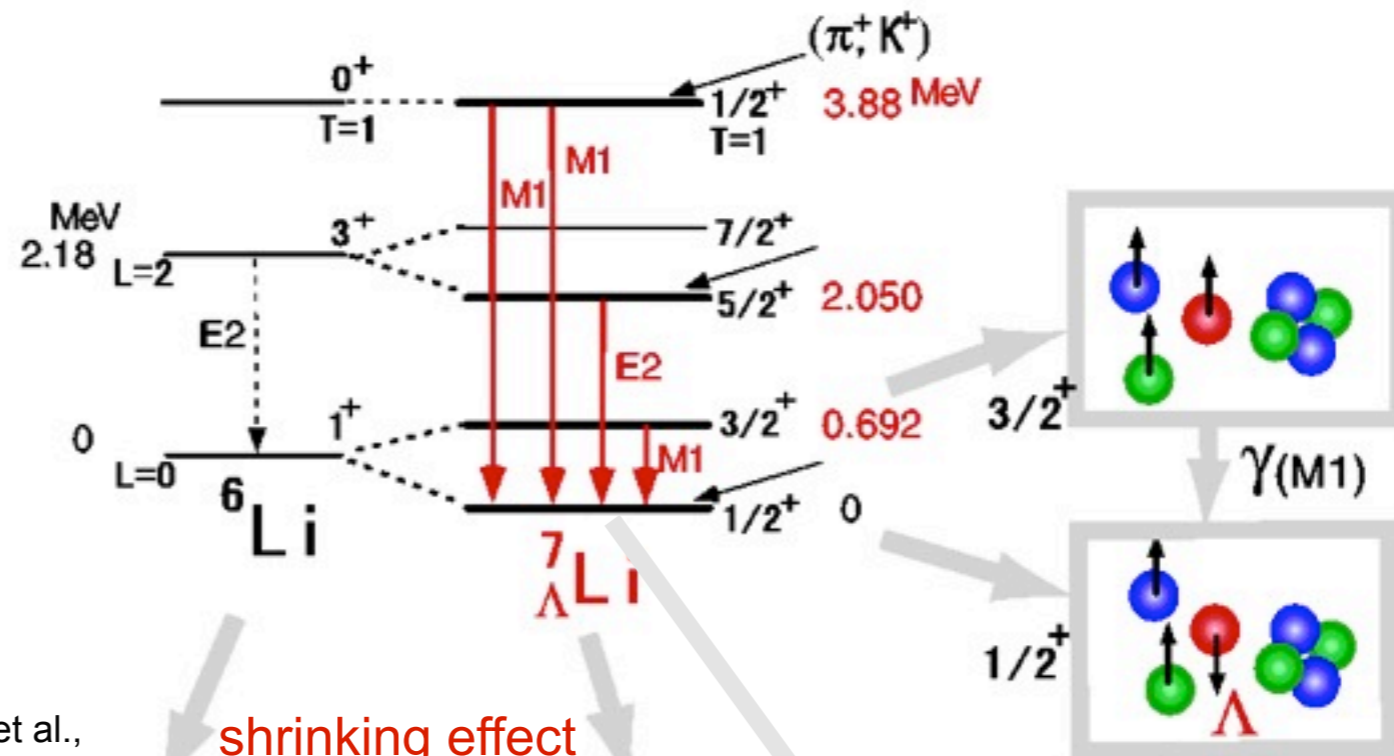
$$\mathcal{M}(E\lambda, \mu) = \int \rho(\vec{r}) r^\lambda Y_{\lambda\mu}(\hat{r}) d\tau$$

$$\mathcal{M}(M\lambda, \mu) = \frac{-1}{c(\lambda + 1)} \int \vec{j}(\vec{r}) \cdot (\vec{r} \times \nabla) r^\lambda Y_{\lambda\mu}(\hat{r}) d\tau$$

$$\Gamma(E1) = 1.59 \times 10^{15} (E)^3 B(E1)$$

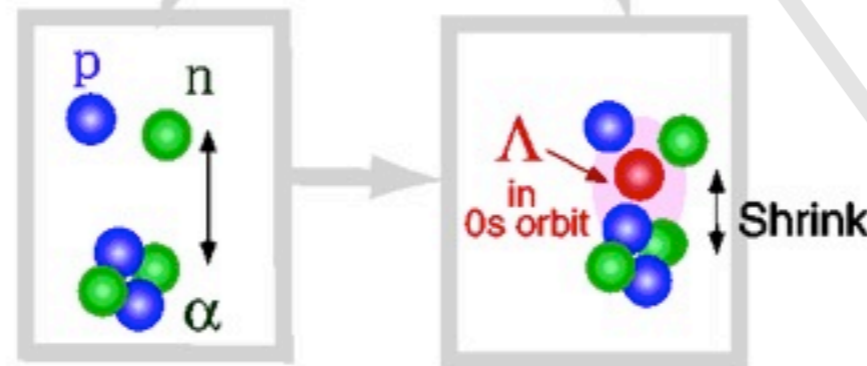
$$\Gamma(E2) = 1.22 \times 10^9 (E)^5 B(E2) \quad \text{in } e^2(\text{fm})^{2\lambda}$$

Summary on ${}^7_{\Lambda}\text{Li}$



Predicted by Motoba et al.,
Prog.Theor.Phys.
70 (1983) 189.

shrinking effect



spin-spin interaction
 $\Delta = 0.50 \text{ MeV}$

N-LS interaction
 $S_N \sim -0.4 \text{ MeV}$

PRL 84 (2000) 5963

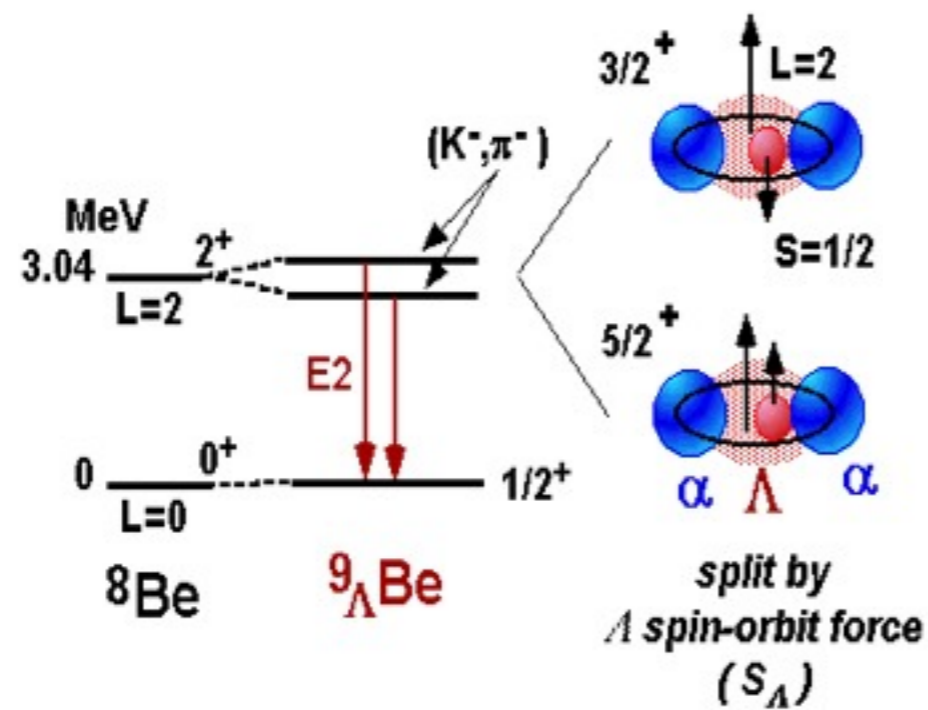
$$B(E2) \propto |\langle f | e r^2 Y_2 | i \rangle|^2$$

$$\propto R^4 \text{ or } (\beta \langle r^2 \rangle)^2$$

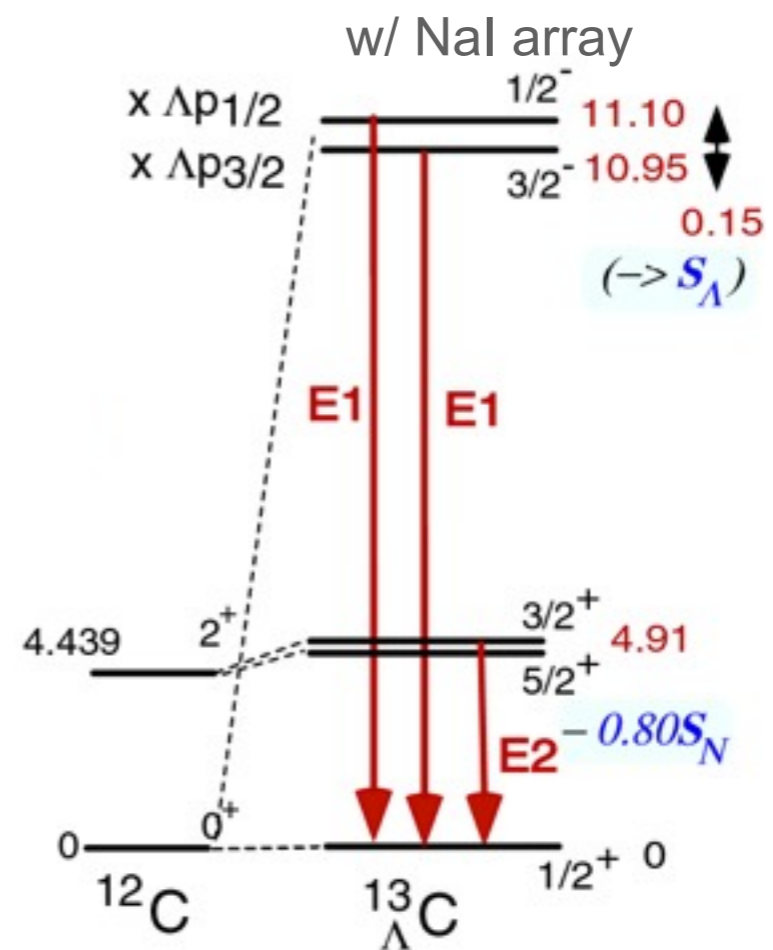
$B(E2) \text{ [e}^2 \text{ fm}^4\text{]}$
 $10.9 \pm 0.9 \longrightarrow 3.6 \pm 0.5 \pm 0.4$
 $\Rightarrow 19 \pm 4\% \text{ shrinkage by } \Lambda$
 Tanida et al., PRL 86(2001) 1982

ΛN spin-orbit force

${}^9\text{Be} (K^-, \pi^- \gamma) {}^9\Lambda\text{Be}$
BNL E930-1



${}^{13}\text{C} (K^-, \pi^- \gamma) \text{BNL E929}$



Ajimura et al., PRL 86 (2001) 4255

$^{13}_{\Lambda}C$

$p_{1/2}$, $p_{3/2}$ single-particle level splitting

$$E(1/2^-) - E(3/2^-) = 152 \pm 54 \pm 36 \text{ keV}$$

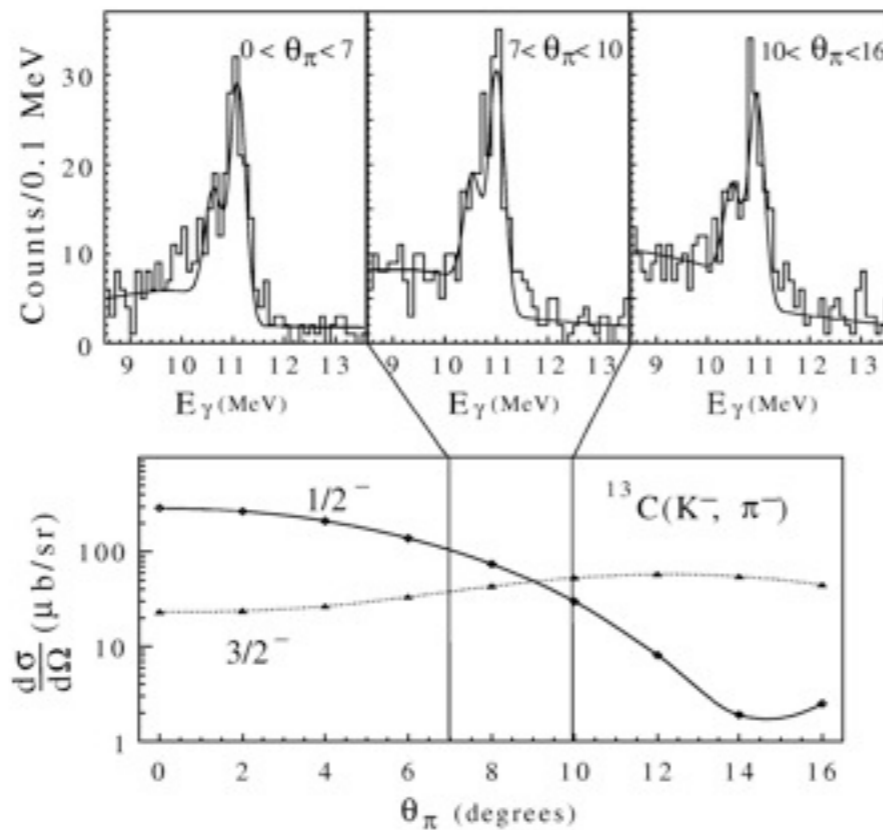


FIG. 2. γ ray spectra taken in coincidence with scattered π^- 's (upper panel) and differential cross section of $1/2^-$ and $3/2^-$ states calculated by Motoba [18] (lower panel) are shown.

-forward

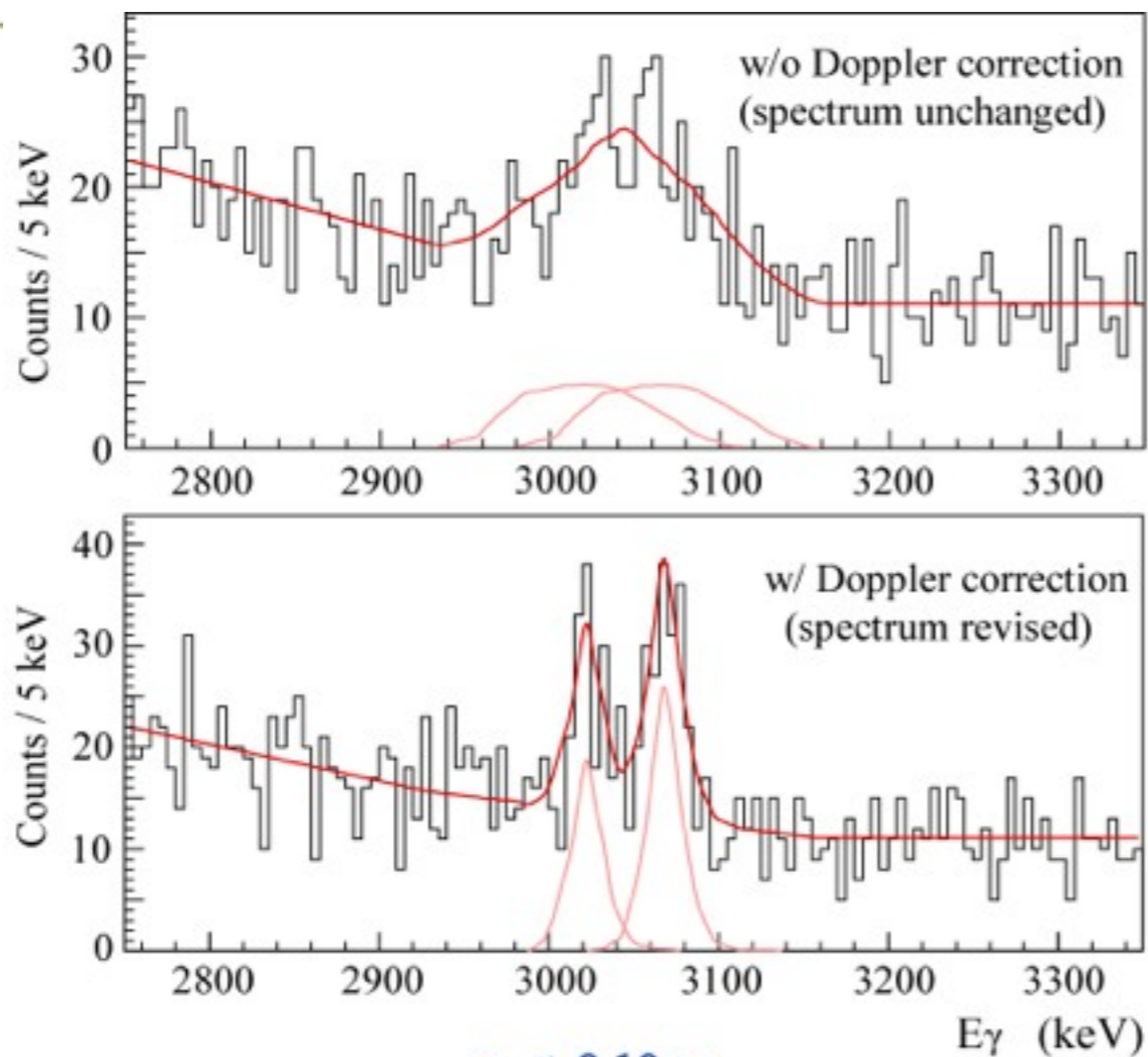
$$(p_{1/2,n}^{-1}, p_{1/2,\Lambda}) \quad \Delta L=0$$

-backward

$$(p_{1/2,n}^{-1}, p_{3/2,\Lambda}) \quad \Delta L=2$$

${}^9_{\Lambda}\text{Be}$

Revised



Revised
Results

$\tau < 0.10$ ps
 $\Delta E = 43 \pm 5$ keV
 $E = 3024 \pm 3 \pm 1, 3067 \pm 3 \pm 1$ keV
 $\chi^2/\text{dof} = 1.22$

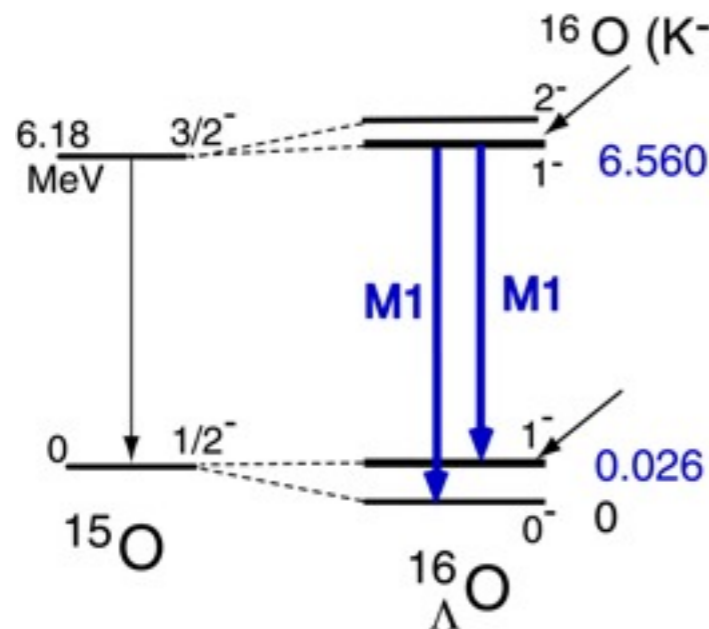
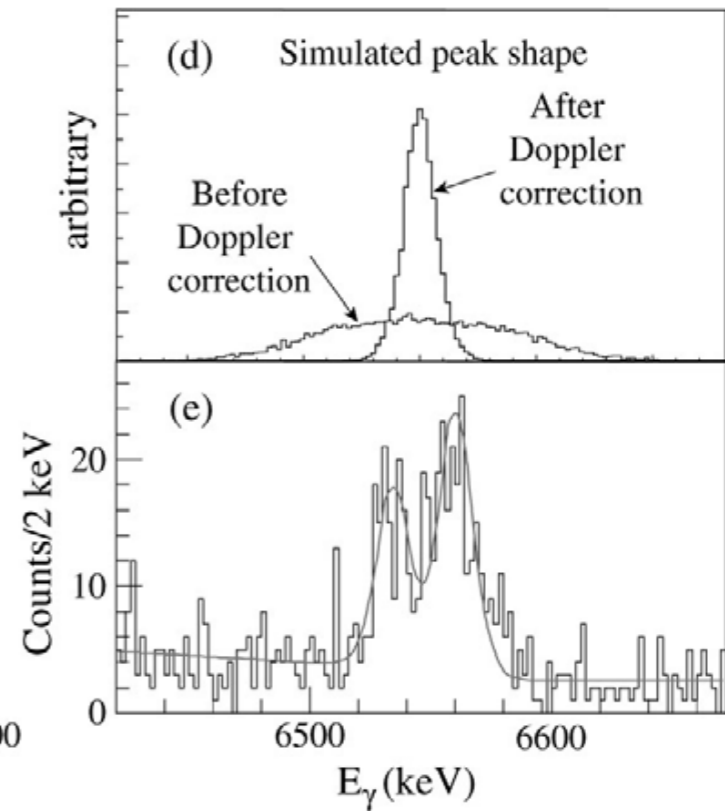
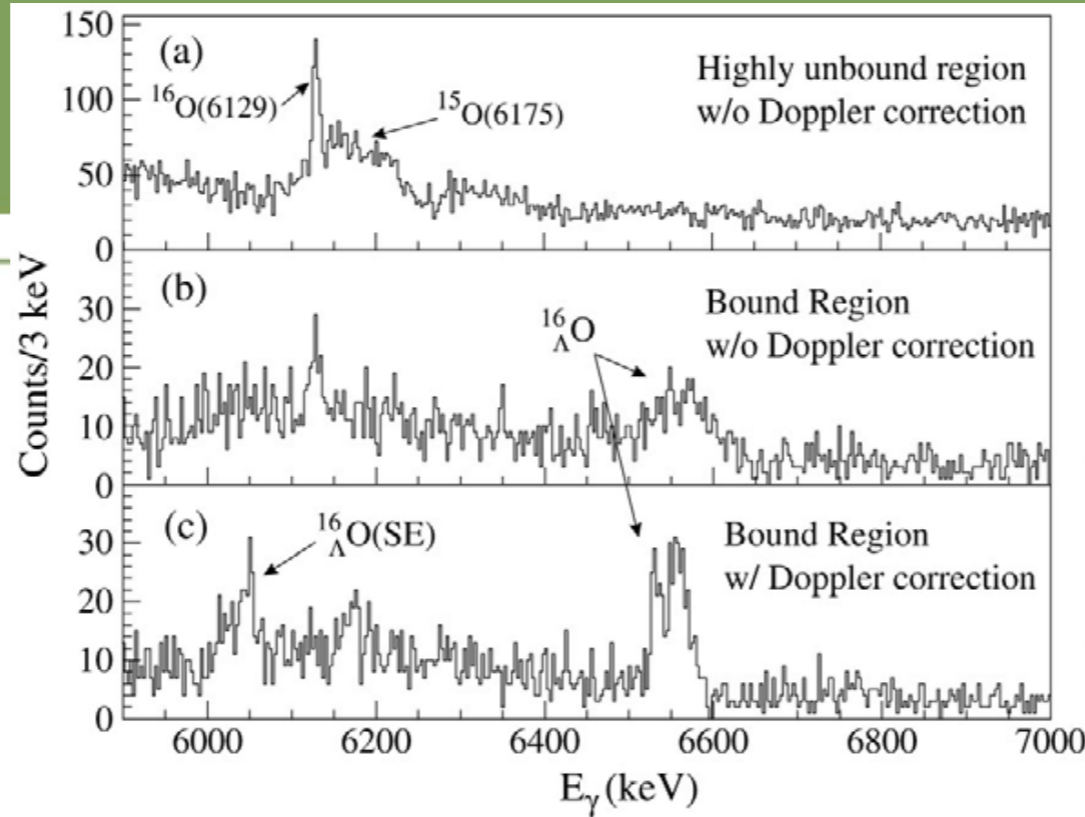
Hiyama et al: PRL 85 (2000) 270
 $E(3/2^+) - E(5/2^+)$
 Meson exch. 0.08 - 0.20 MeV
 quark 0.035 - 0.040 MeV

• Millener:
 $E(3/2^+) - E(5/2^+)$
 $= -0.035 \Delta - 2.465 S_{\Lambda} + 0.936 T$

$S_{\Lambda} = -0.02$ MeV

Consistent with
 very small LS splitting in ${}^{13}_{\Lambda}\text{C}$

$^{16}_{\Lambda}O$



$$\Delta E = 26.1 \pm 1.4 \pm 0.6 \text{ keV}$$

$$E(1^-) - E(0^-) = -0.39 \Delta + 1.4 S_{\Lambda} - 0.005 S_N + 7.8 T + LS$$

(Millener, 2001)

$$\leftarrow \Delta = 0.46 \text{ MeV}, S_{\Lambda} = -0.01 \text{ MeV}$$

$\rightarrow T = 26 - 32 \text{ keV}$ First info. on T

	ND	NF	NSC89	NSC97f
T	18	33	36	54 (keV)

Some of Meson Exchange model predictions agree

Summary of p-shell levels

► $\Delta=0.48$ MeV, $S_\Lambda=-0.01$ MeV, $S_N=-0.43$ MeV, $T=0.03$ MeV

Table 18

Energies of the four hypernuclear level spacings that are described in terms of the spin-dependent ΛN interaction parameters obtained by Millener's shell model calculations [101]

Hypernuclear levels	Shell model calculation by Millener	$\Lambda\Sigma$ (MeV)	Exp. (MeV)
${}^7_\Lambda\text{Li}$ $E(3/2^+) - E(1/2^+)$	$1.444\Delta + 0.054S_\Lambda + 0.016S_N - 0.271T$	+0.071	0.692
${}^7_\Lambda\text{Li}$ $\overline{E(7/2^+, 5/2^+)}$ $- \overline{E(3/2^+, 1/2^+)}^a$	$-0.05\Delta + 0.07S_\Lambda + 0.70S_N - 0.08T$ $+ \Delta E_{\text{core}}^b$		1.858
${}^9_\Lambda\text{Be}$ $E(3/2^+) - E(5/2^+)$	$-0.037\Delta - 2.464S_\Lambda + 0.003S_N + 0.994T$	-0.008	0.043
${}^{16}_\Lambda\text{O}$ $E(1^-) - E(0^-)$	$-0.382\Delta + 1.378S_\Lambda - 0.004S_N + 7.850T$	-0.014 ^c	0.026

Experimental energies obtained by the Hyperball experiments are also shown. The effect of the $\Lambda-\Sigma$ coupling estimated by Millener is listed as $\Lambda\Sigma$.

^a $\overline{E(J_1, J_2)} = [(2J_1 + 1)E(J_1) + (2J_2 + 1)E(J_2)] / (2J_1 + 2J_2 + 2)$ denotes the center of gravity energy for the doublet (J_1, J_2) .

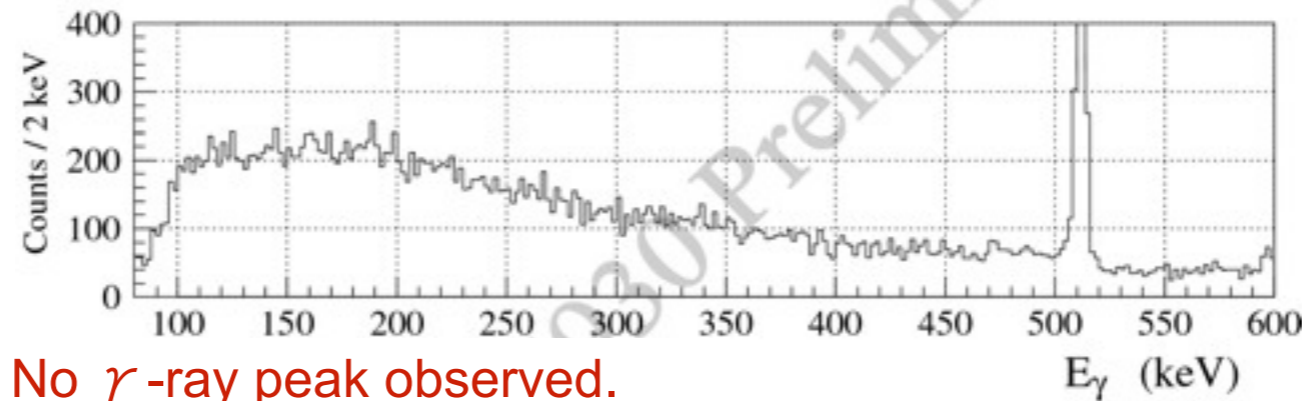
^b $\Delta E_{\text{core}} = E({}^6\text{Li}; 3^+) - E({}^6\text{Li}; 1^+) = 2.186$ MeV.

^c A small 1^- mixing effect of 0.016 MeV is added to a $\Lambda-\Sigma$ coupling effect of -0.030 MeV.

γ spectrum of $^{10}_{\Lambda}\text{B}$ (E930-2)

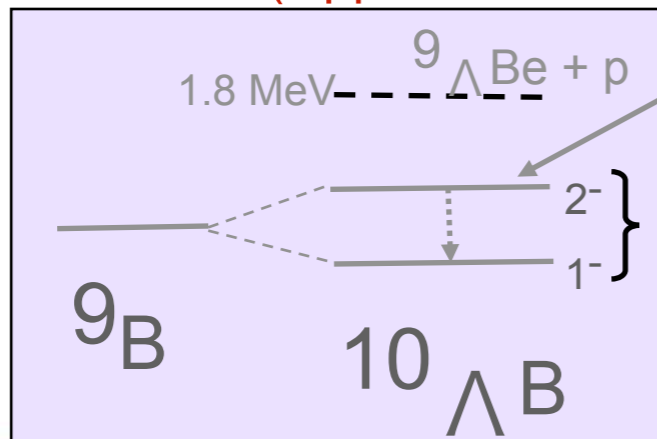
$^{10}\text{B} (\text{K}^-, \pi^-) ^{10}_{\Lambda}\text{B}$

$-40 < -B_{\Lambda}^* < -10 \text{ MeV}$ *uncalibrated
(5 MeV lower than the $^9_{\Lambda}\text{Be}$ gate)



No γ -ray peak observed.

(Upper limit to be determined.)



(K^-, π^-)

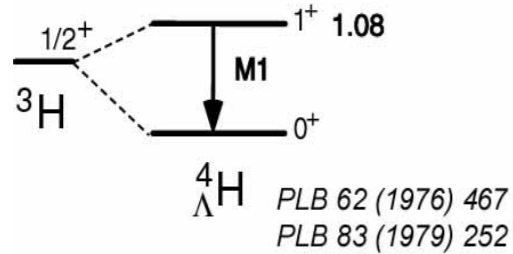
$< 100 \text{ keV}$ $\delta \sim 200 \text{ keV}$ from $\Delta = 0.5 \text{ MeV}$

Confirmed

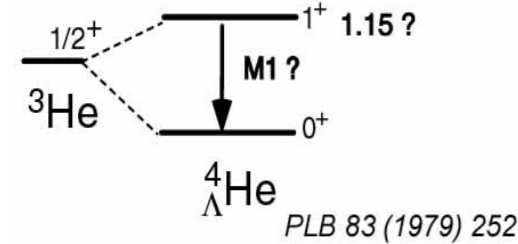
Chrien et al., Phys. Rev. C 41 (1990) 1062.

Summary of Hypernuclear γ rays

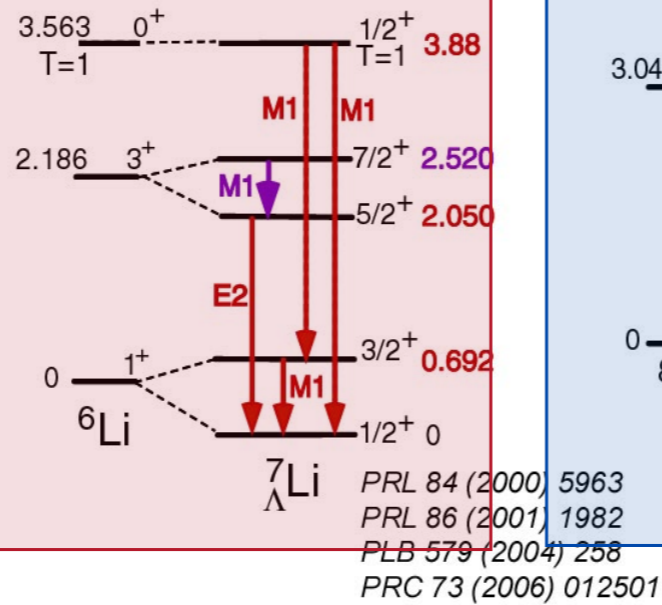
${}^7\text{Li}$ etc. ($K^-_{\text{stop}}, \gamma \pi^-$)



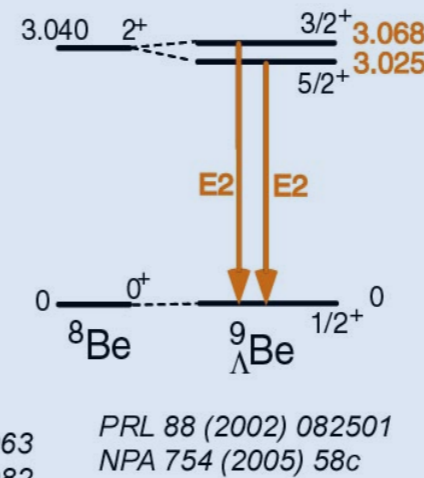
${}^7\text{Li}$ ($K^-_{\text{stop}}, \gamma \pi^0$)



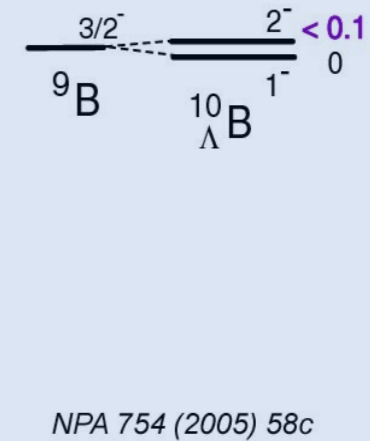
${}^7\text{Li}$ ($\pi^+, K^+\gamma$) KEK E419



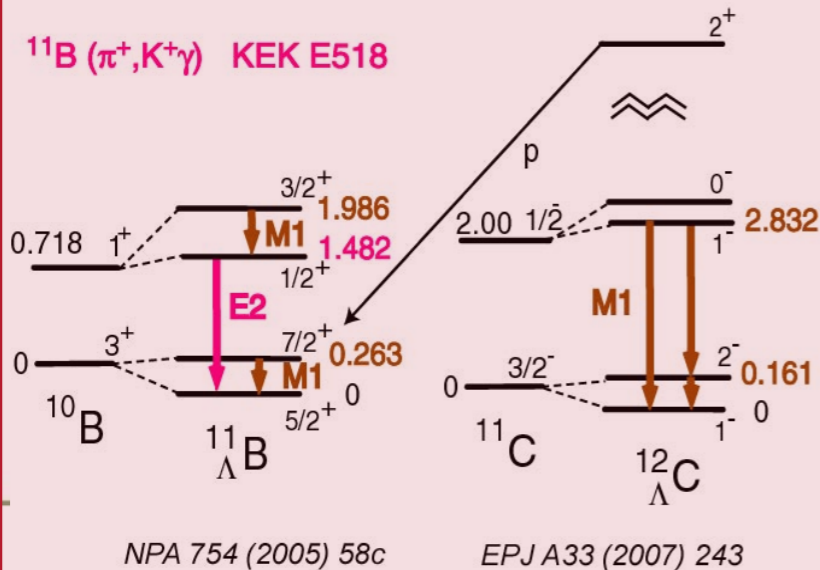
${}^9\text{Be}$ ($K^-, \pi^-\gamma$) BNL E930('98)



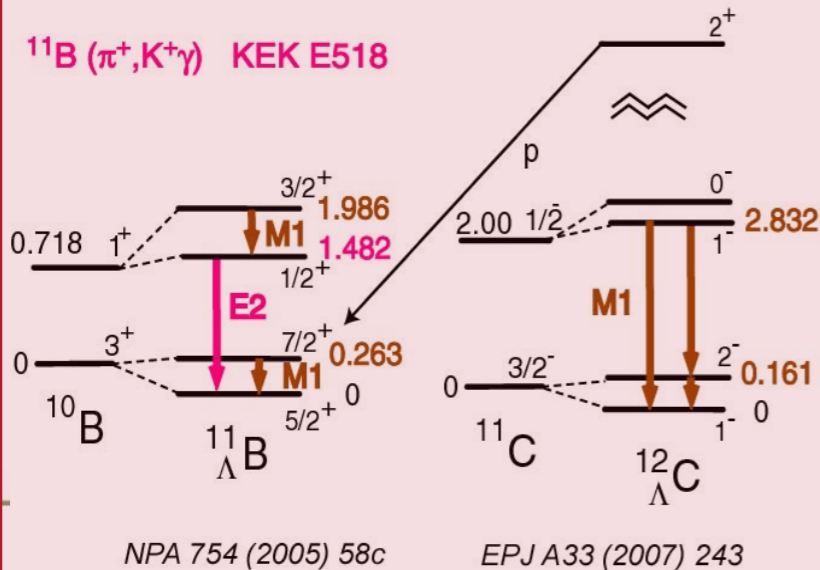
${}^{10}\text{B}$ ($K^-, \pi^-\gamma$) BNL E930('01)



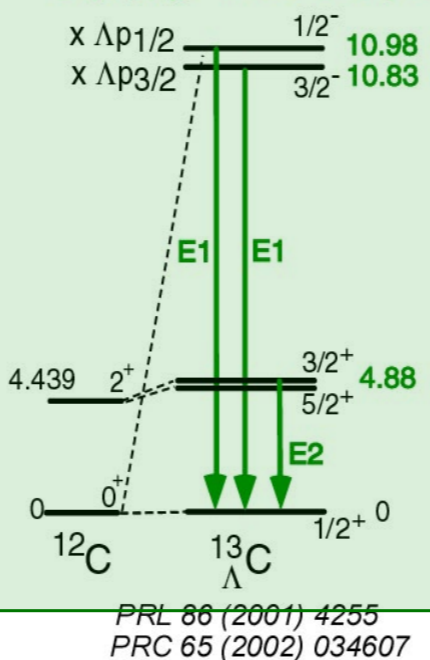
${}^{12}\text{C}$ ($\pi^+, K^+\gamma$) KEK E566



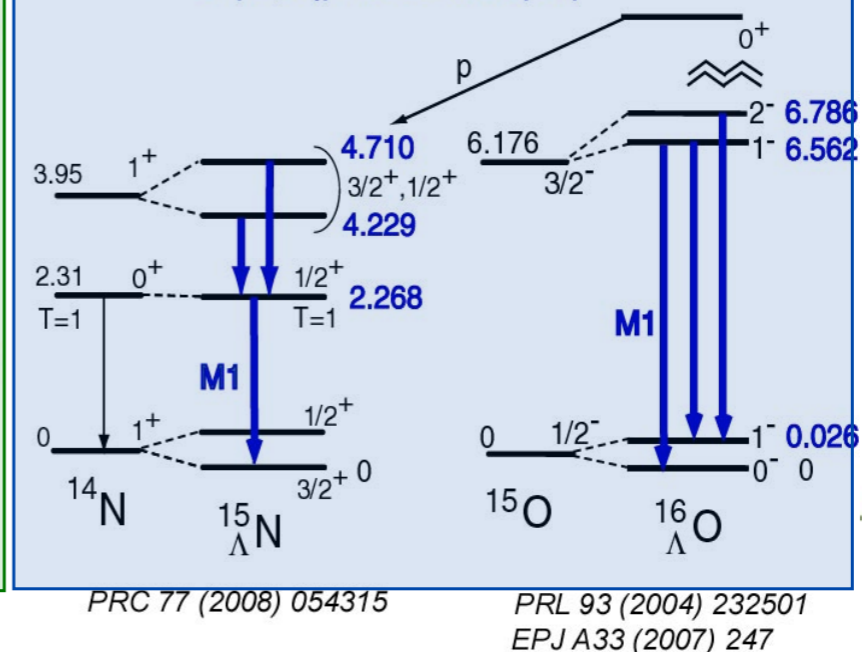
${}^{11}\text{B}$ ($\pi^+, K^+\gamma$) KEK E518



${}^{13}\text{C}$ ($K^-, \pi^-\gamma$) BNL E929 (NaI)

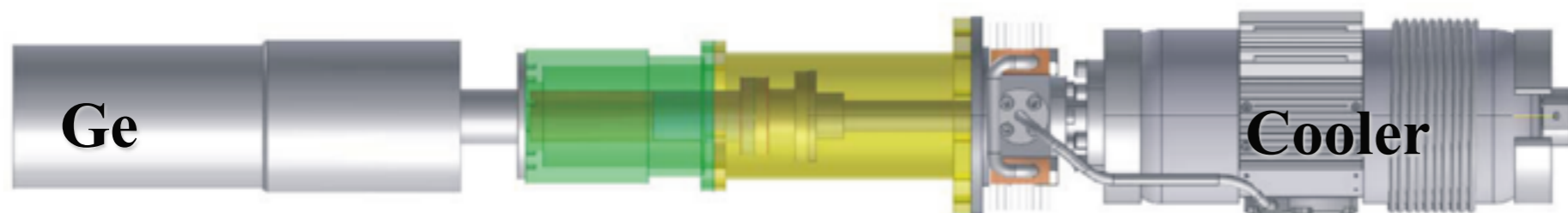
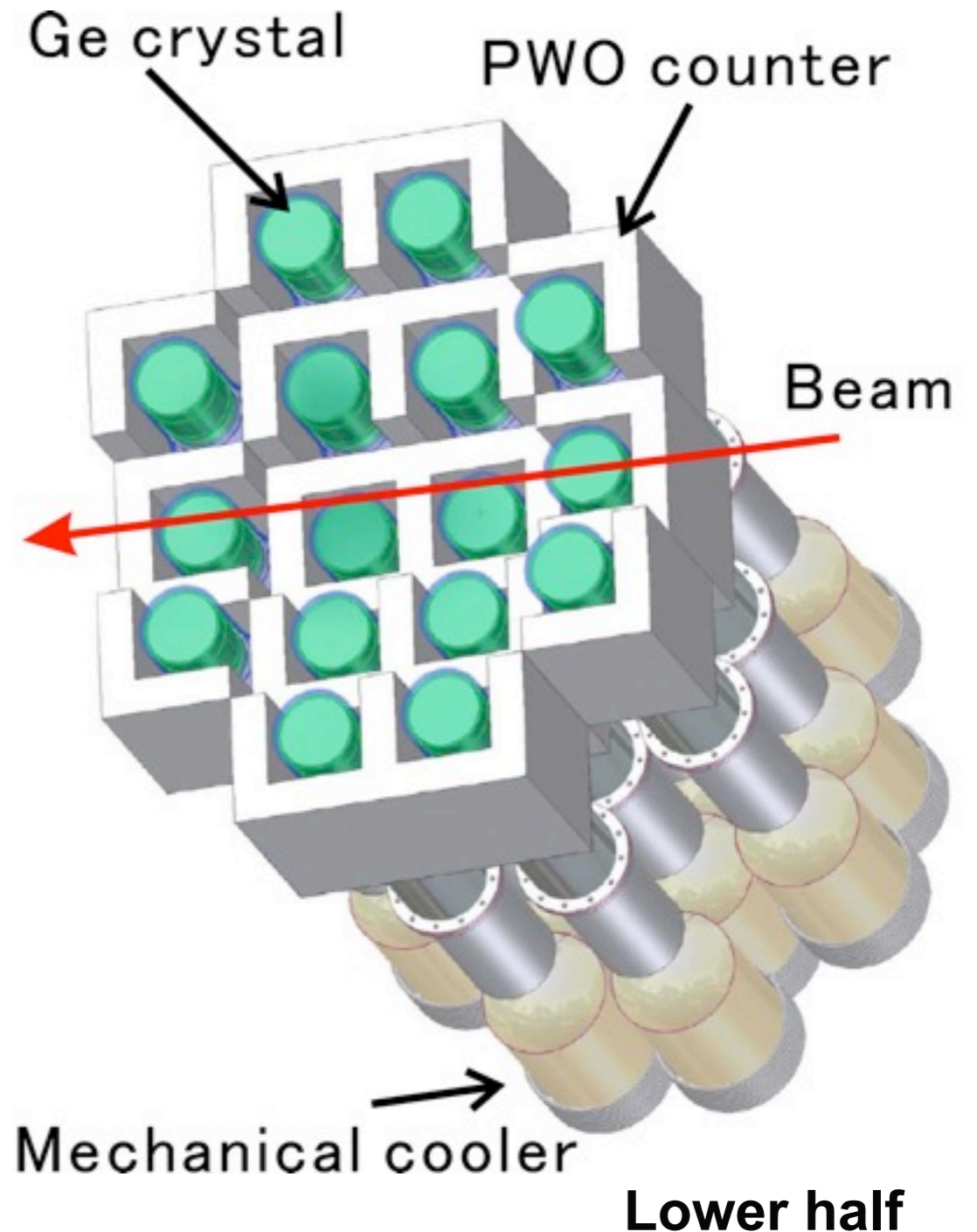


${}^{16}\text{O}$ ($K^-, \pi^-\gamma$) BNL E930('01)

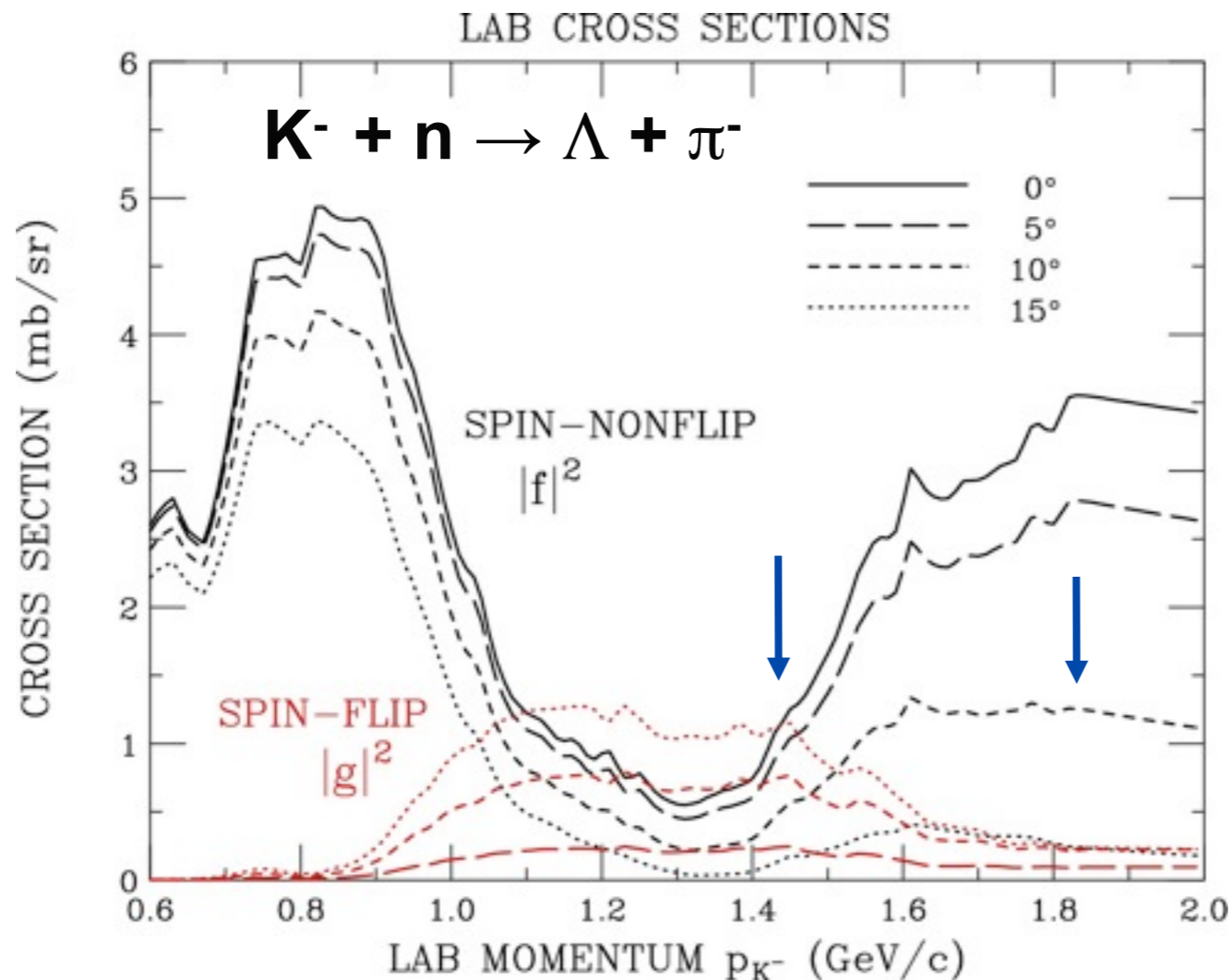


Hyperball-J

- Ge (single, r.e.~60%) x ~32
→ peak efficiency ~6% at 1 MeV
(x ~3 of Hyperball)
- Mechanical cooling
 - Lower temp. for less radiation damage
 - Save space for flexible arrangement
- PWO background suppression counters replaced from BGO for higher rate
- Waveform readout (under development)
=> Rate limit $\sim 2 \times 10^7$ particles /s
(x5 of Hyperball)



Best K^- beam momentum



Both spin-flip and nonflip states should be produced.

→ $p_K = 1.1$ or 1.5 GeV/c

$p_K = 1.1$ GeV/c : K1.1 + “SKS” (ideal)
 $p_K = 1.5$ GeV/c : K1.8 + SKS (realistic)

High K/π ratio to minimize radiation damage to Ge detectors

→ Double-stage separation. K1.8BR is not good.

Beam and Setup

(K^-, π^-, γ) at $p_K = 1.5 \text{ GeV}/c$

Both spin-flip and nonflip states produced
Spin assignment from angular distribution

■ Spectrometer: SksMinus

$\Delta p \sim 4 \text{ MeV}$ (FWHM)

$\Omega \sim 110 \text{ msr}$

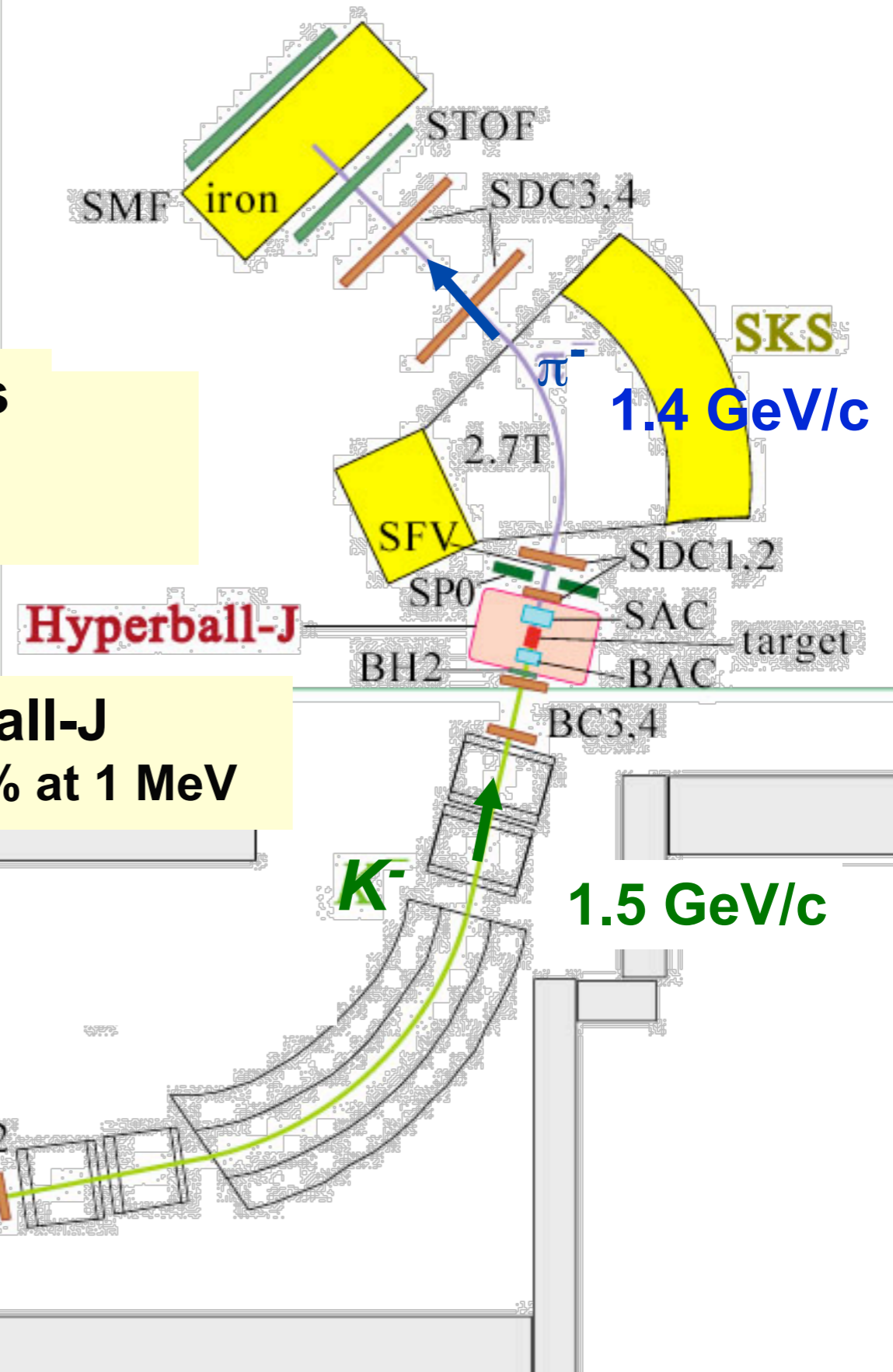
■ Hyperball-J

$\varepsilon \sim 6\%$ at 1 MeV

■ Beamline: K1.8

$0.5 \times 10^6 \text{ K}^-/\text{spill}$ at $1.5 \text{ GeV}/c$ ($9 \mu\text{A}$)

$K/\pi \gg 1$



g factor of Λ in nucleus

■ Motivation

μ_Λ in nucleus \rightarrow medium effect of baryons

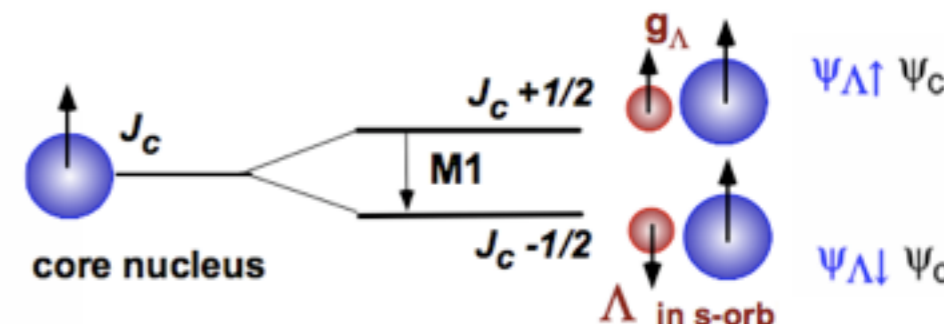
Can be investigated using a Λ in 0s orbit



■ B(M1) of Λ -spin-flip M1 transition $\rightarrow g_\Lambda$

$$\begin{aligned}
 B(M1) &= (2J_{up} + 1)^{-1} |\langle \Psi_{low} \| \mu \| \Psi_{up} \rangle|^2 \\
 &= (2J_{up} + 1)^{-1} |\langle \Psi_{\Lambda\downarrow} \Psi_c \| \mu \| \Psi_{\Lambda\uparrow} \Psi_c \rangle|^2 \\
 \mu &= g_c \mathbf{J}_c + g_\Lambda \mathbf{J}_\Lambda = g_c \mathbf{J} + (g_\Lambda - g_c) \mathbf{J}_\Lambda \\
 &= \frac{3}{8\pi} \frac{2J_{low} + 1}{2J_c + 1} (g_\Lambda - g_c)^2 \quad [\mu_N^2]
 \end{aligned}$$

Reduction of constituent q mass?
Swelling?



■ How to measure

Doppler-shift attenuation method :

applied to “hypernuclear shrinkage”
in ${}^7_\Lambda\text{Li}$ ($5/2^+ \rightarrow 1/2^+$) from B(E2)

$$\Gamma = BR / \tau = \frac{16\pi}{9} E_\gamma^3 B(M1)$$

PRL 86 ('01)1982

■ Preliminary data (statistical error only) from ${}^7_\Lambda\text{Li}$ ($3/2^+ \rightarrow 1/2^+$) (BNL E930)

$$g_\Lambda = -1.1^{+0.6}_{-0.4} \mu_N \longleftrightarrow g_\Lambda(\text{free}) = -1.226 \mu_N \quad \rightarrow < 5\% \text{ accuracy at J-APRC}$$

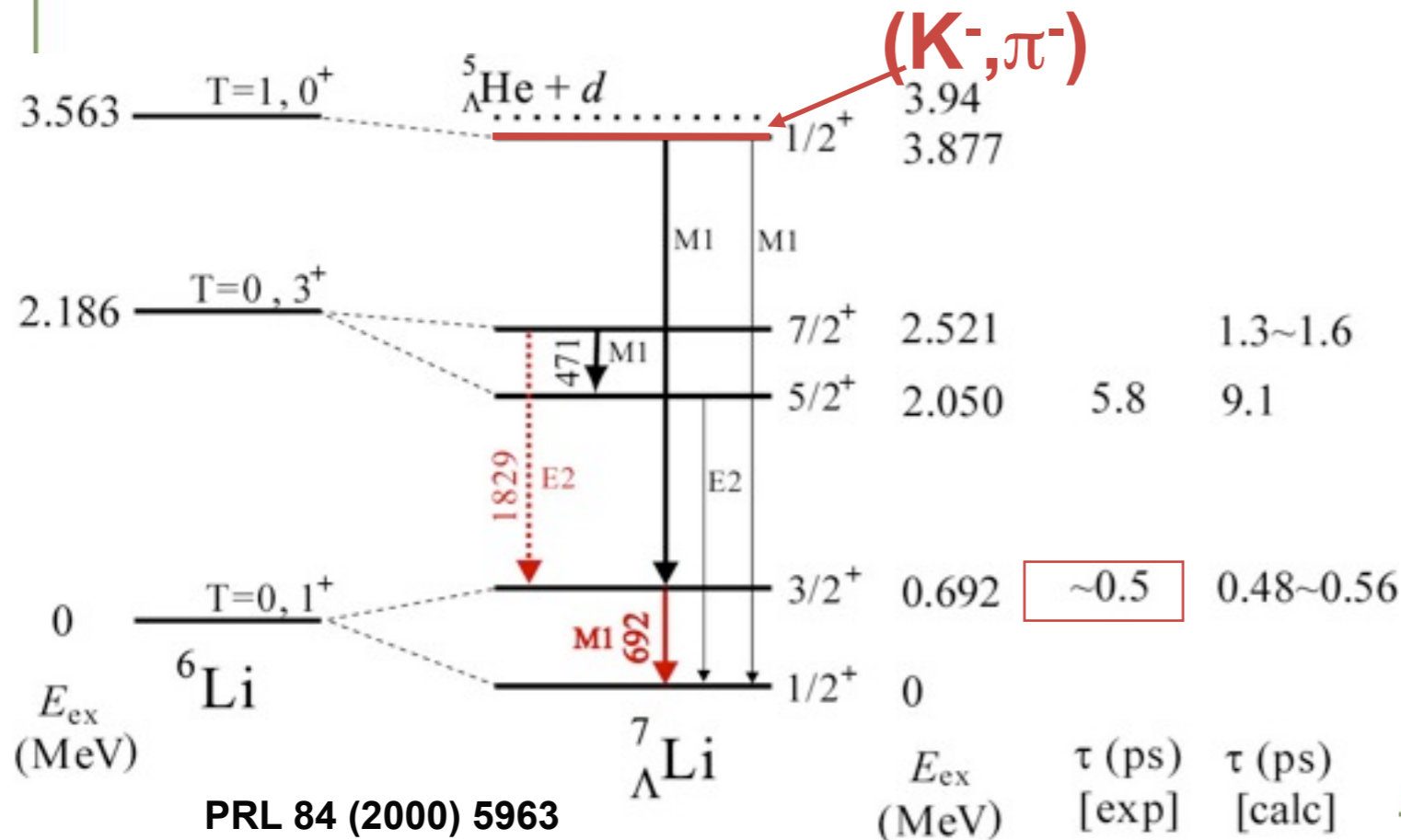
Proposed B(M1) measurement

Difficulties in B(M1) measurement

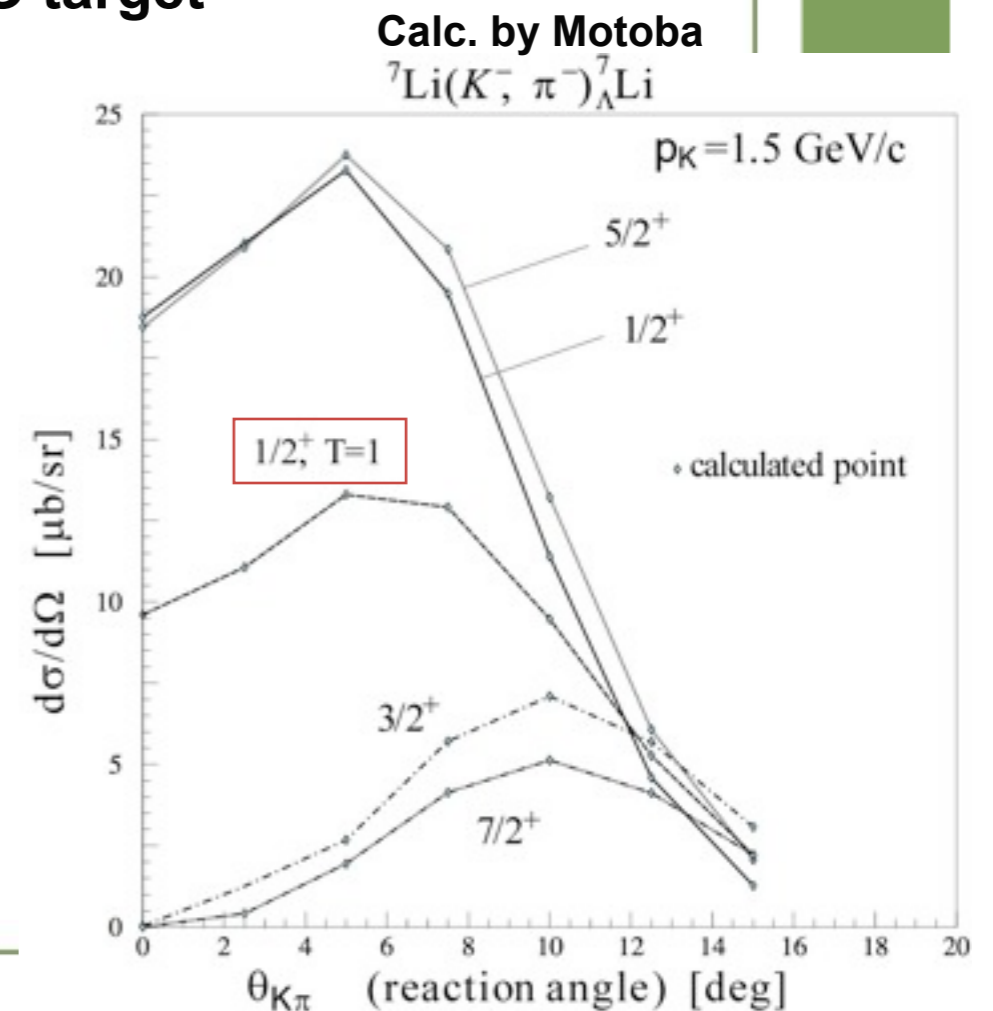
- Doppler Shift Attenuation Method works only when $\tau < t_{\text{stop}}$
 - τ is very sensitive to E_γ because $B(M1) \propto 1/\tau \propto E_\gamma^3$. But E_γ is unknown.
 - Cross sections and background cannot be accurately estimated.
- Previous attempts: $^{10}_\Lambda\text{B}$, $^{11}_\Lambda\text{B}$ (E_γ too small $\rightarrow \tau \gg t_{\text{stop}}$), $^7_\Lambda\text{Li}$ (by product: indirect population)

To avoid ambiguities, we use the best-known hypernucleus, $^7_\Lambda\text{Li}$.

- Energies of all the bound states and B(E2) were measured,
- γ -ray background level was measured,
- cross sections are reliably calculated.
- $\tau = 0.5\text{ps}$, $t_{\text{stop}} = 2\text{-}3\text{ ps}$ for 1.5 GeV/c (K^-, π^-) and Li_2O target



PRL 84 (2000) 5963
PRC 73 (2006) 012501



Expected yield and sensitivity

Yield estimate

$$N_K = 0.5 \times 10^6 / \text{spill}$$

$$\text{Target } (^7\text{Li in Li}_2\text{O}) = 20\text{cm} \times 2.0\text{g/cm}^3 \times 14/30 \times 0.934 / 7 \times 6.02 \times 10^{23}$$

$$\int d\sigma/d\Omega(1/2;1) \Delta\Omega \times \text{BR}(1/2^+;1 \rightarrow 3/2^+) = 0.84 \mu\text{b} \times 0.5$$

$$\varepsilon(\text{Ge}) \times \varepsilon(\text{tracking}) = 0.7 \times 0.6$$

→

$$\text{Yield } (3/2^+ \rightarrow 1/2^+) = 7.3 / \text{hr} (1000 \text{ spill})$$

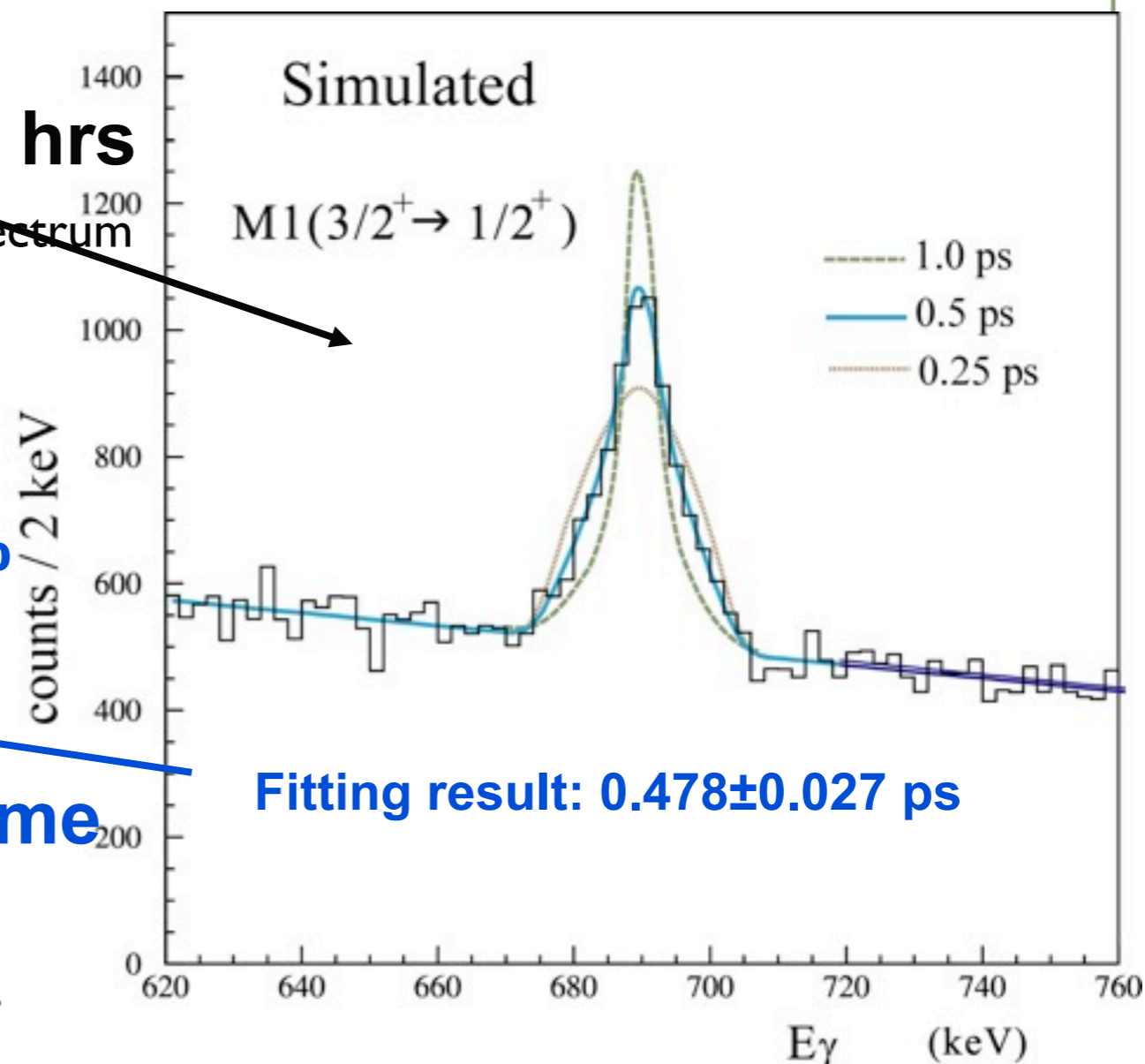
$$= \mathbf{3600 / 500 \text{ hrs}}$$

Background estimated from E419 $^7_\Lambda\text{Li}$ spectrum

■ **Stat. error** $\Delta\tau/\tau = 5.4\%$

$$\rightarrow \frac{\Delta|g_\Lambda - g_c|}{|g_\Lambda - g_c|} \sim 3\%$$

■ **Syst. error < 5%**
mainly from stopping time



Σ

Hypernuclei

History of Σ Hypernuclei

- ✓ Σ^- atom X-ray : Level shifts, widths
 - CERN('75), RAL('78), BNL('93)
 - $^{12}\text{C} \sim ^{208}\text{Pb}$, 23 data points
 - $V_{\text{opt}}(r) = t_{\text{eff}} \cdot Q(r)$ (C.J.Batty, Nucl. Phys. A372 (81) 433)
 - $-\text{Re } V_{\text{opt}}(0) \sim 25\text{-}30 \text{ MeV}$, **Attractive**
 - $-\text{Im } V_{\text{opt}}(0) \sim 10\text{-}15 \text{ MeV}$, **Absorptive**
 - $\Sigma\text{N} \rightarrow \Lambda\text{N}$ conversion (strong interaction)
 - Σ hypernuclei may exist, but the widths are broad
 - **No Spectroscopy** $\Gamma \sim 2\text{Im}V$

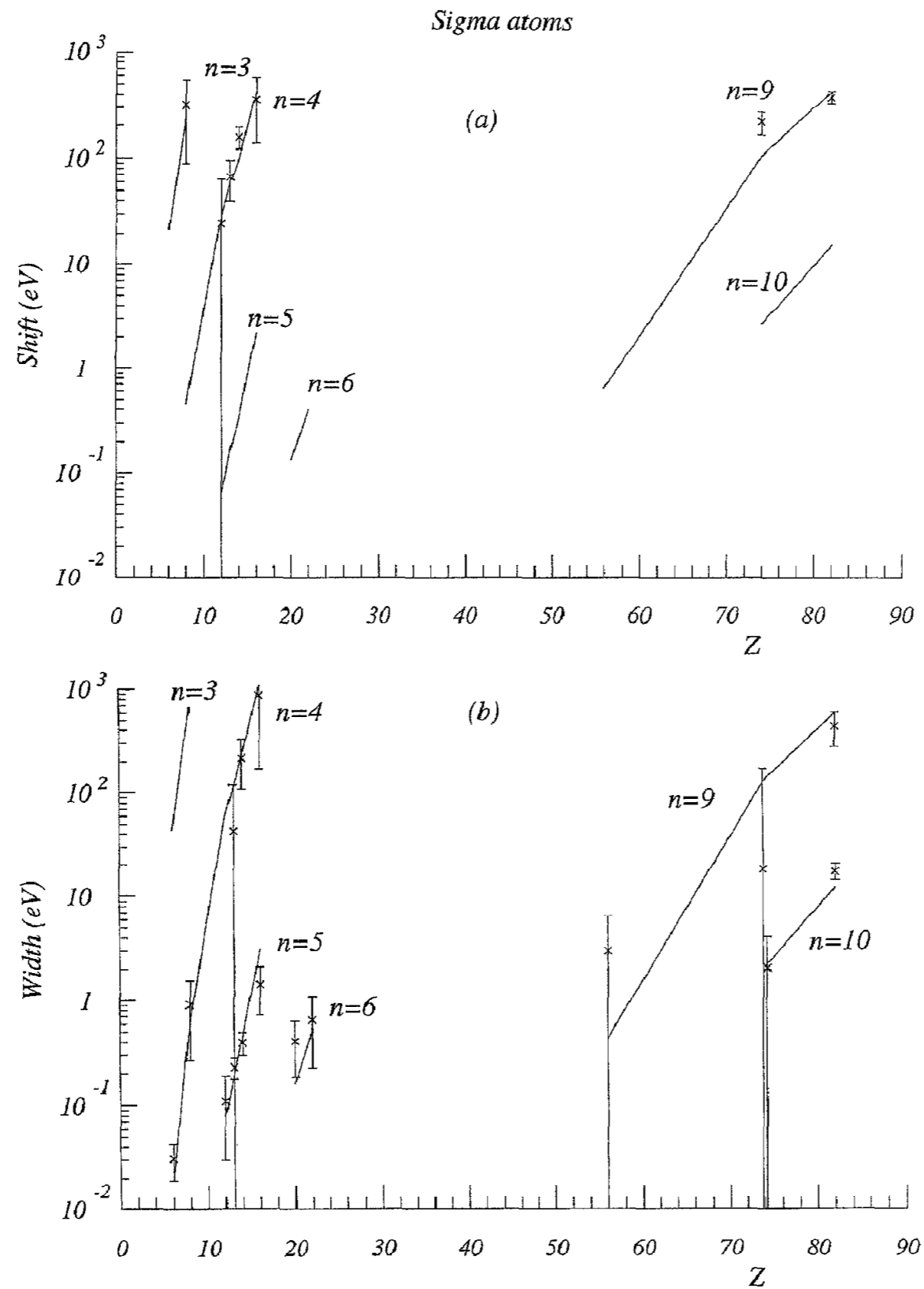


Fig. 9. Shift and width values for sigma atoms. The continuous lines join points calculated with the best-fit optical potential discussed in Section 6.2.

Σ -Nucleus potential

✓ Σ -atom X-ray

C.J.Batty et al., NP A372(81)433.

$$V(r) + iW(r) = -\left(\frac{4\pi\hbar^2}{2\mu}\right)\left(1 + \frac{\mu}{M_N}\right)\bar{a}\rho(r) \quad \bar{a} = 0.35 + i0.19 : \text{scattering - length,}$$
$$= -(28 + i15)\text{MeV}\rho(r)/\rho_0 \quad \mu : \text{reduced - mass}$$

✓ DWIA analysis: Green Function method

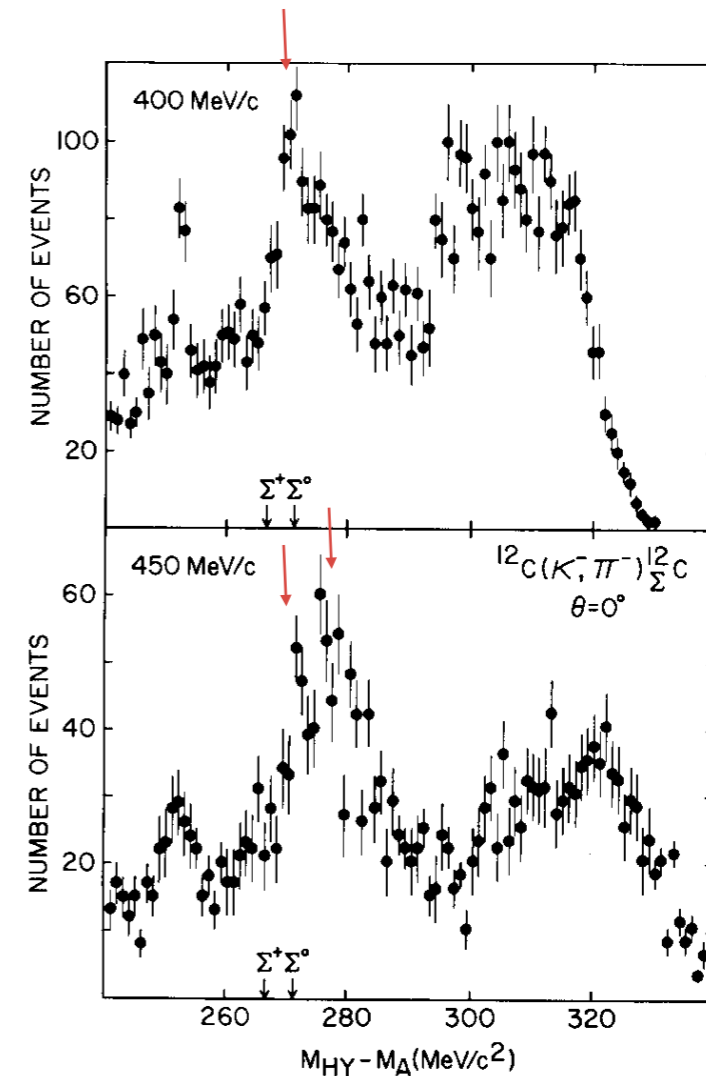
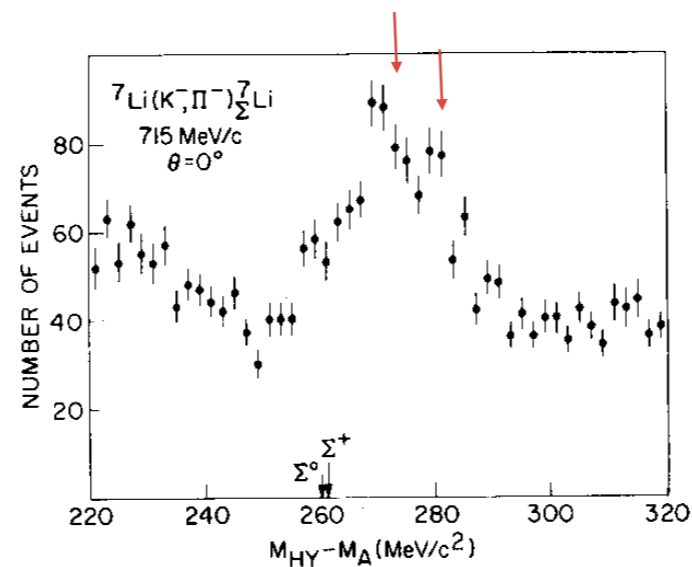
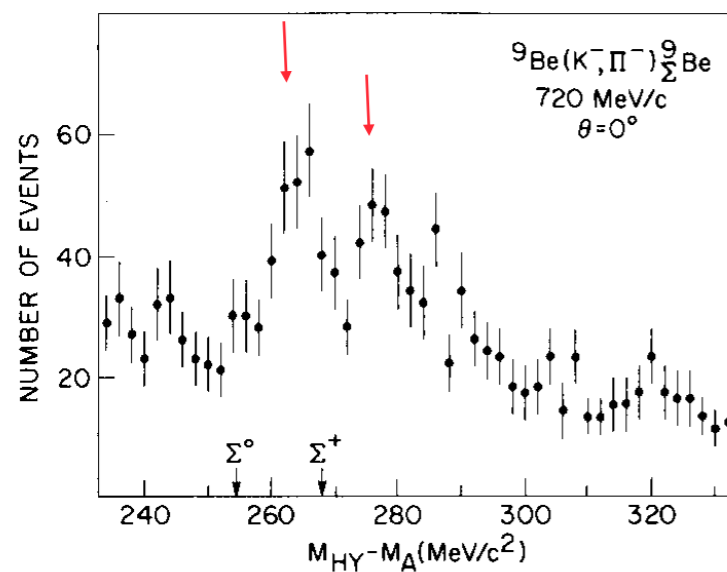
Morimatsu and Yazaki, NP A483(88)493,

R.S.Hayano, NP A478(88)113c.

$V_0 < 12$ MeV, $W_0 > 6$ MeV for ^{12}C

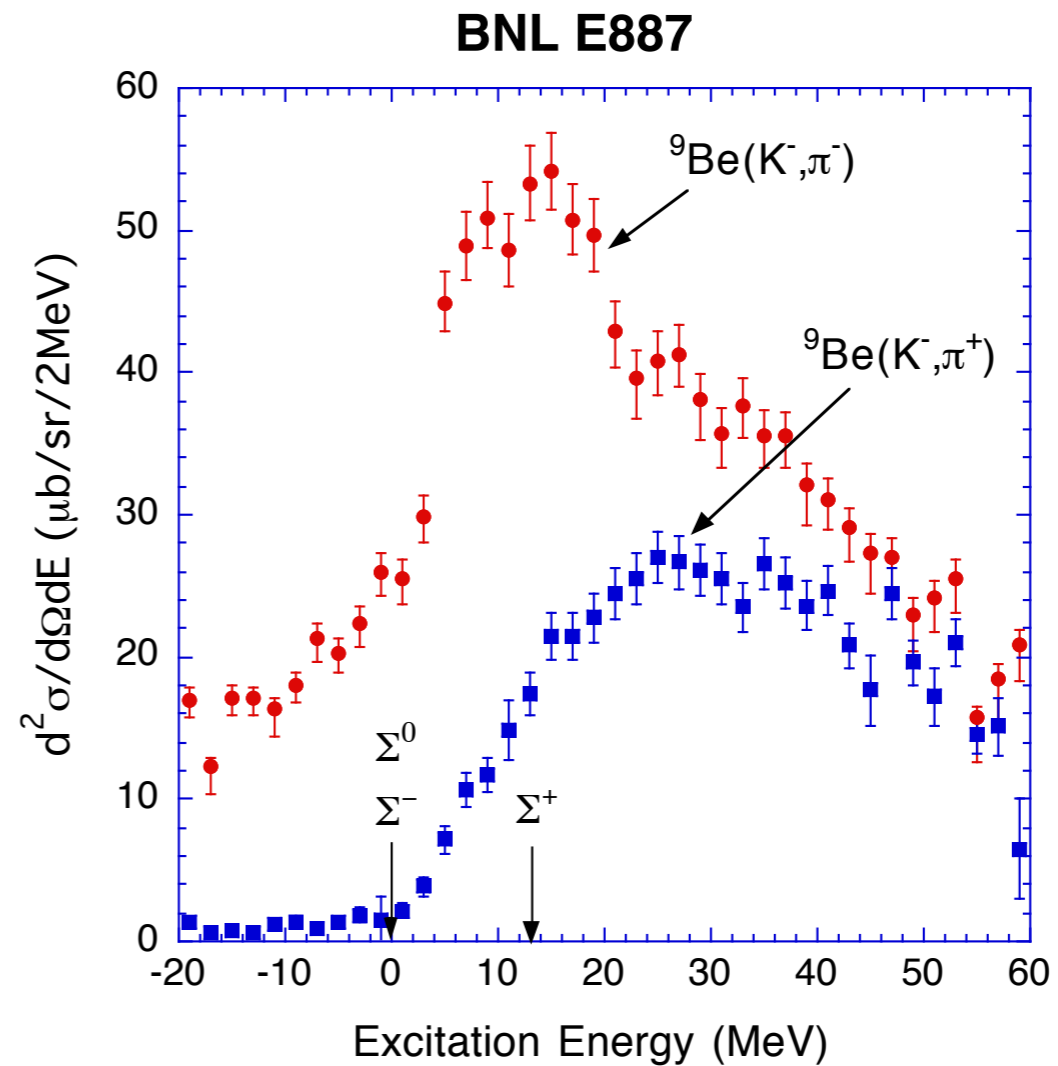
Narrow width problem in 1980s

- ✓ ${}^9\text{Be}(\text{K}^-, \pi^-)$ at CERN(1980)
 - Narrow peak ($\sim 7 \text{ MeV}$) in unbound region
 - BNL, KEK

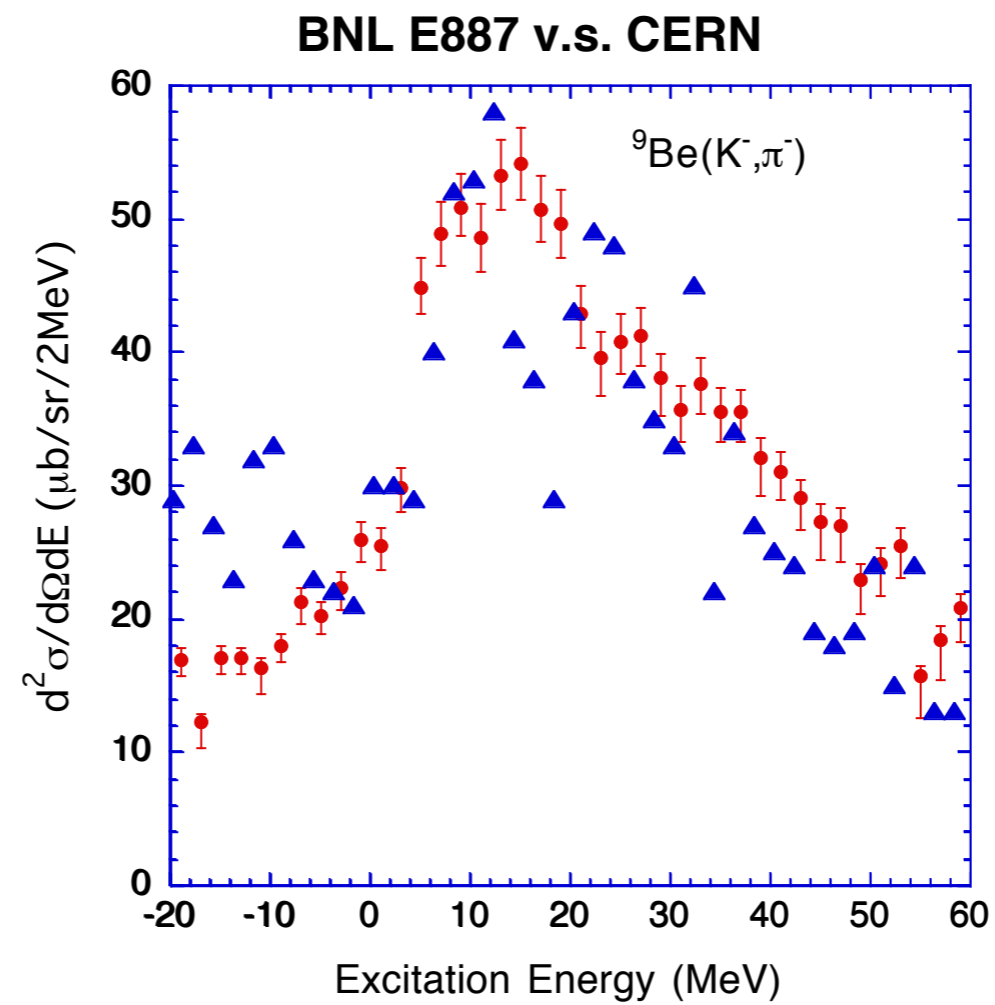


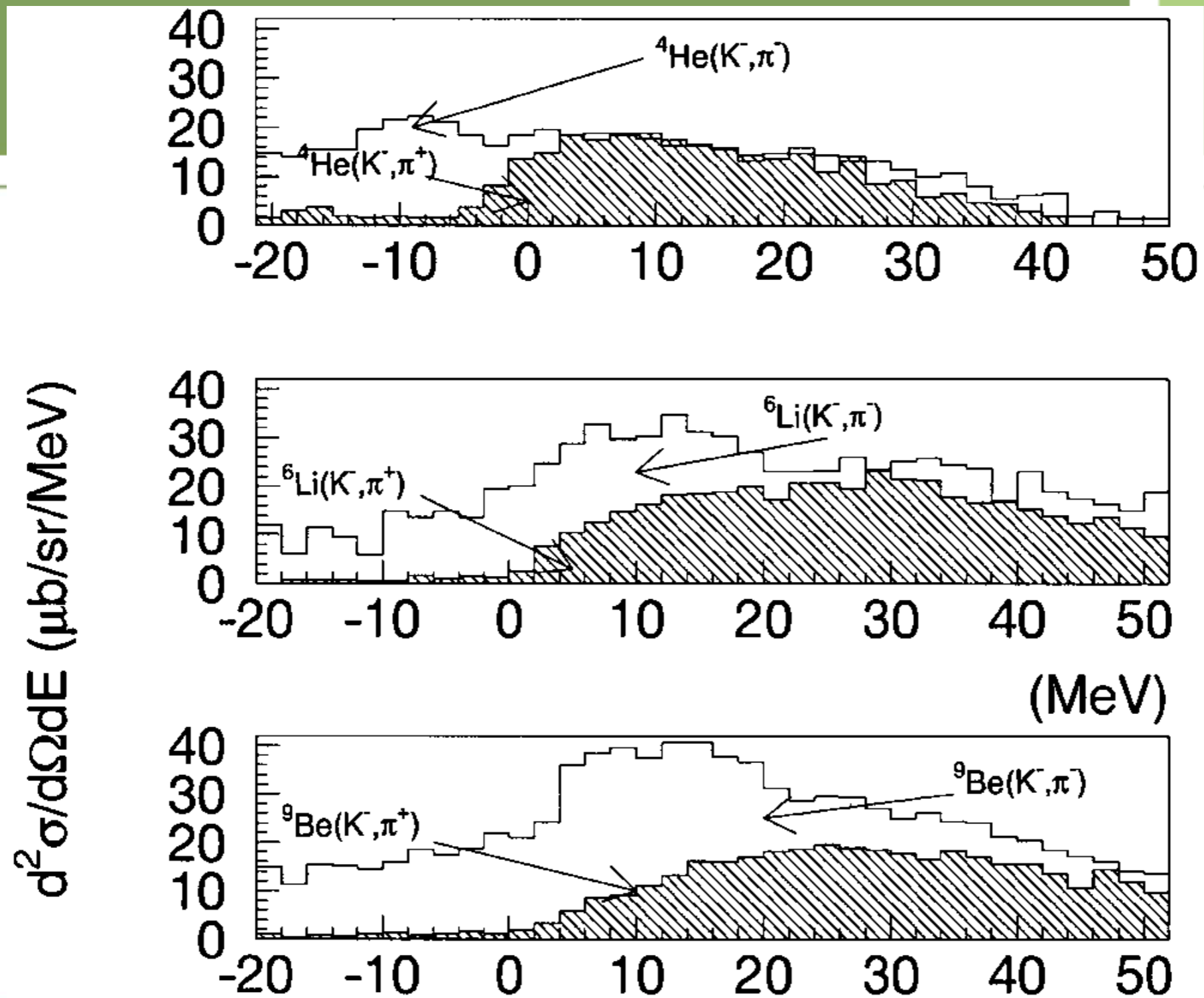
BNL E887

- ✓ 600 MeV/c
- ✓ 4 degrees
- ✓ No Peaks !!



E887 vs. CERN Data





束縛状態の問題

✓ ポテンシャルの実部の深さ？

– Σ 原子のX線データの密度依存型ポテンシヤ

ルによる再解析

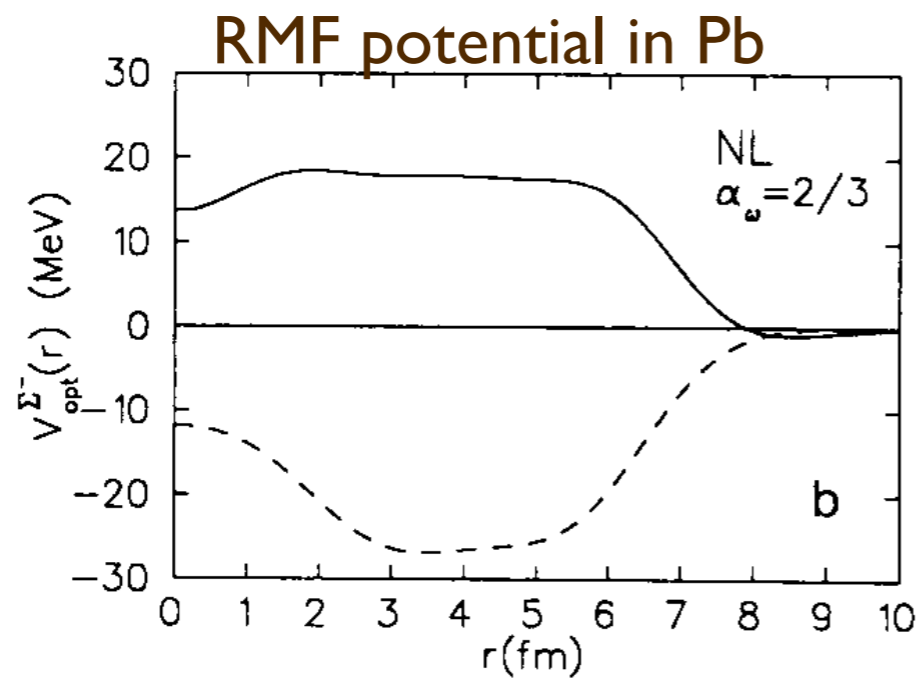
- 弱い引力：原子核外部の長距離
- 強い斥力：原子核内部

$$2\mu V_{opt}(r) = -4\pi \left(1 + \frac{\mu}{m_n}\right) \left\{ \left[b_0 + B_0 \left(\frac{\rho(r)}{\rho(0)} \right)^\alpha \right] \rho(r) + \left[b_1 + B_1 \left(\frac{\rho(r)}{\rho(0)} \right)^\alpha \right] \delta\rho(r) \right\}$$

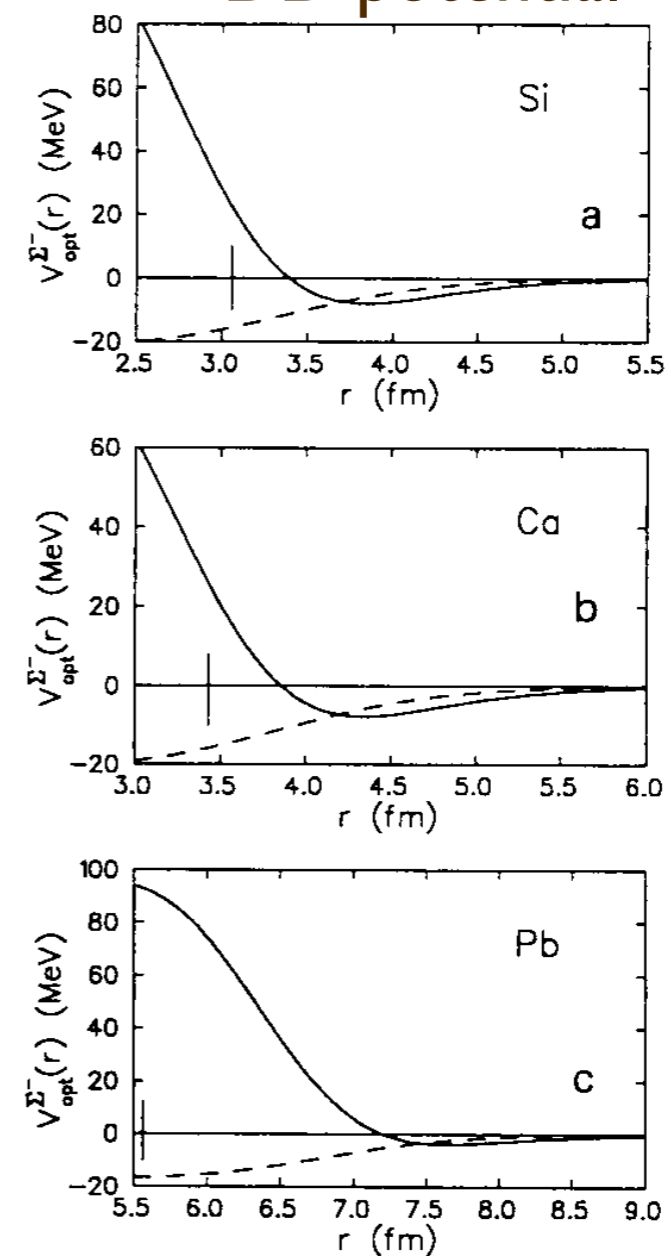
- 軽い核を除いて、束縛状態は存在しない!?

Repulsive ??

- ✓ C.J.Batty,E.Friedman,A.Gal,
Phys.Lett.B335(94)273;
PTP Suppl.117(94)227.
- ✓ J.Mares et al., NP A594(95)311.



DD potential



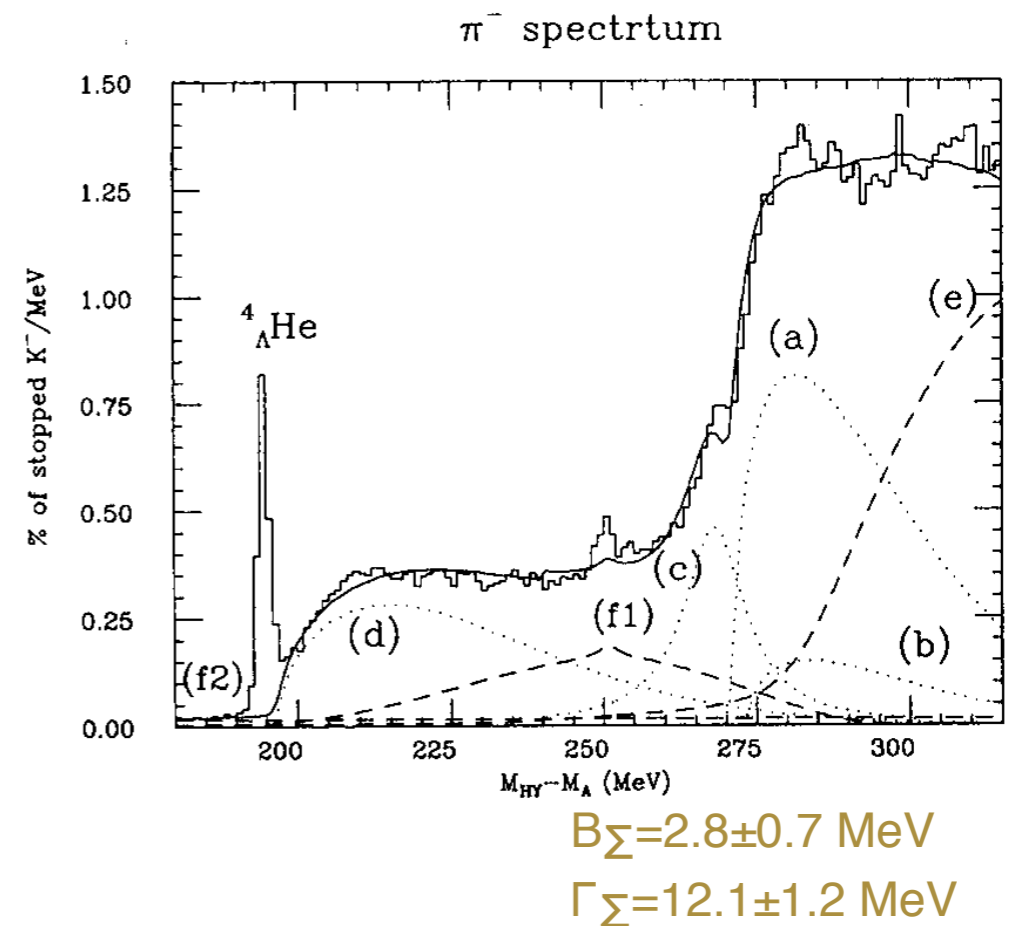
Existence of any bound states ?

✓ Only candidate

- ${}^4\text{He}(\text{K}^-_{\text{stop}}, \pi^-)$: R.S.Hayano et al.
- predicted by Harada and Akaishi

✓ Definitive evidence ?

- Large background
- K^- orbit
 - *S or P ?*



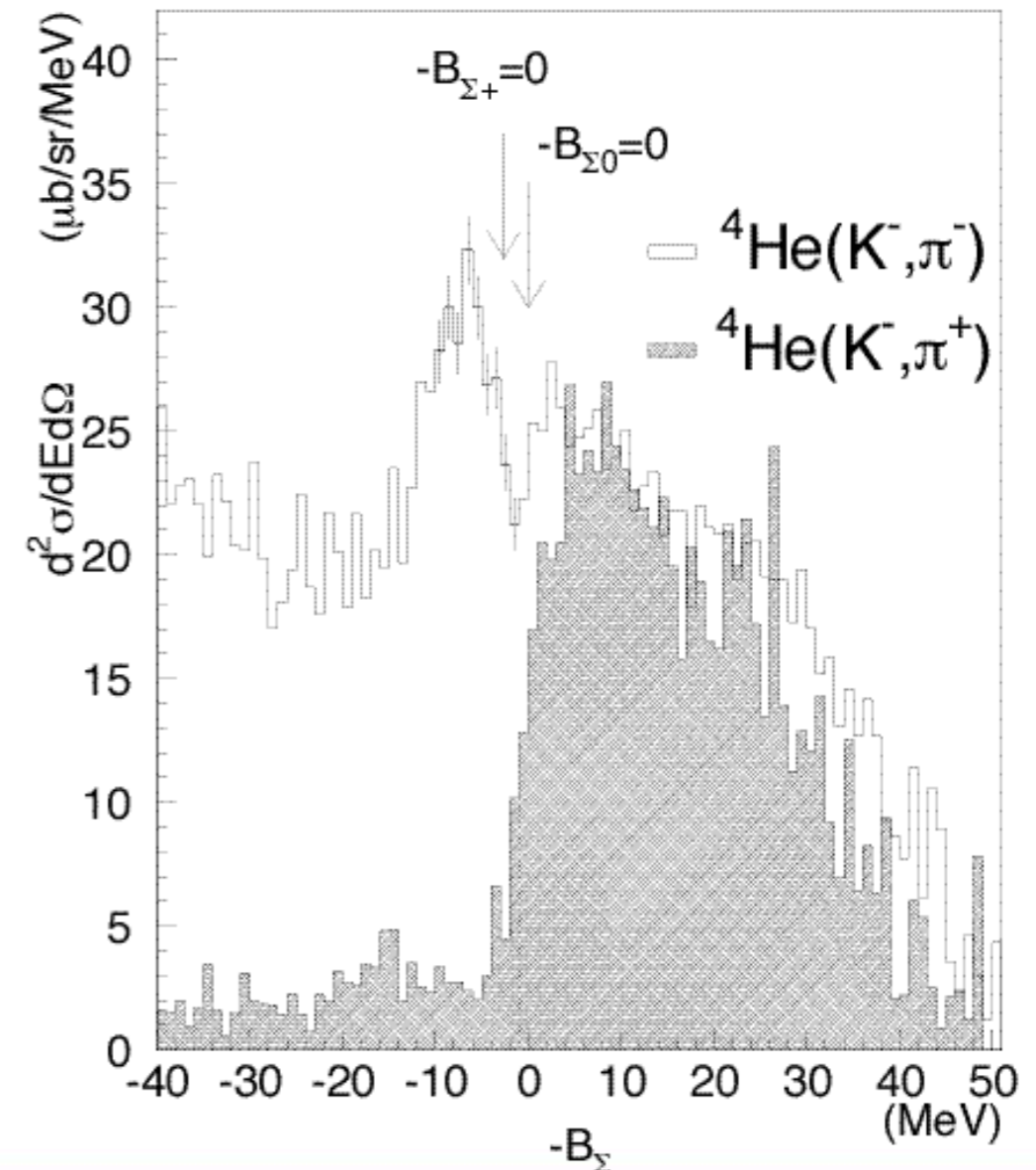
R.S. Hayano et al., PL B231 (1989).

H.Outa et al., Prog. Theor. Phys. Suppl. 117 (1994) 177.

BNL E905: In-flight (K^- , π^-)

- ✓ 600 MeV/c, 4 deg.
- ✓ Simple analysis: DWIA
- ✓ Established the existence of a bound state
 - B_Σ : $4.4 \pm 0.3 \pm 1$ MeV
 - Width : $7 \pm 0.7 + 1.2 / - 0.0$ MeV (FWHM)

T. Nagaie et al., PRL 80 (1998) 1605.



Harada and Akaishi

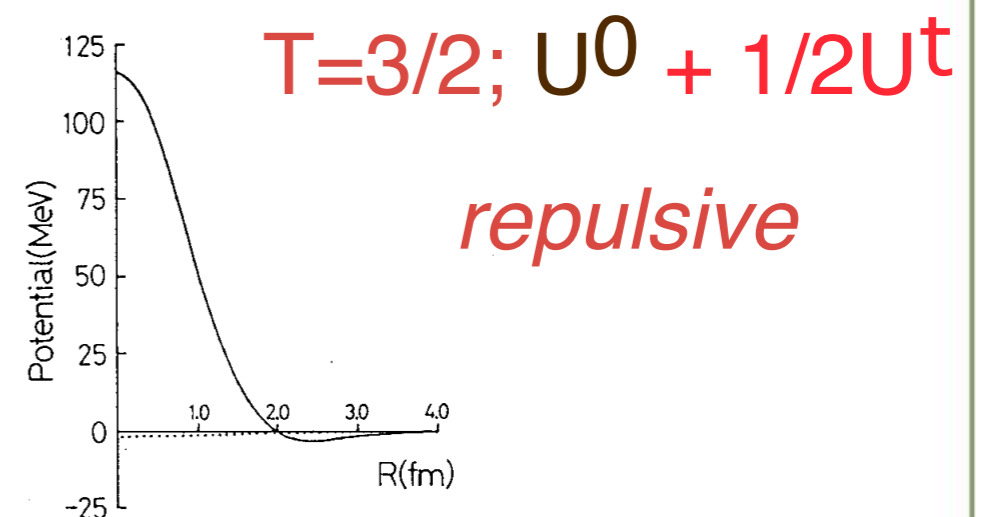
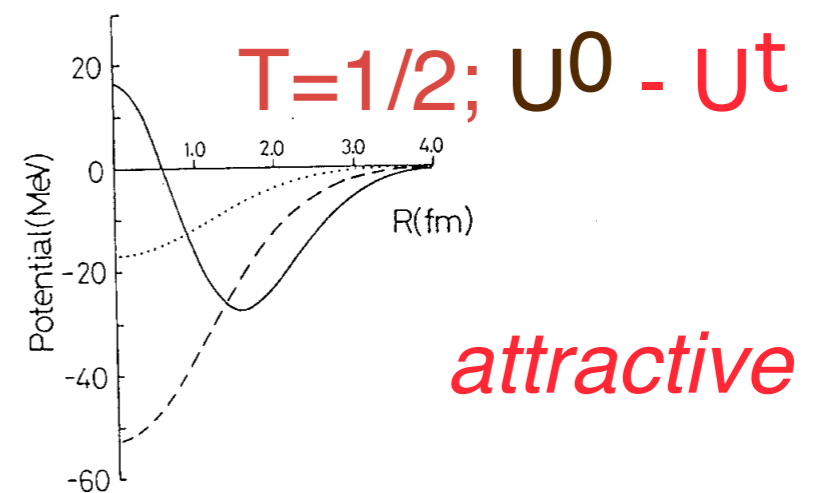
✓ Strong Isospin dependence

– Lane term

$$- U_{C\Sigma} = U^0 + U^t T_C \cdot t_\Sigma / A$$

– T. Harada et al., Nucl. Phys. A507(1990) 715.

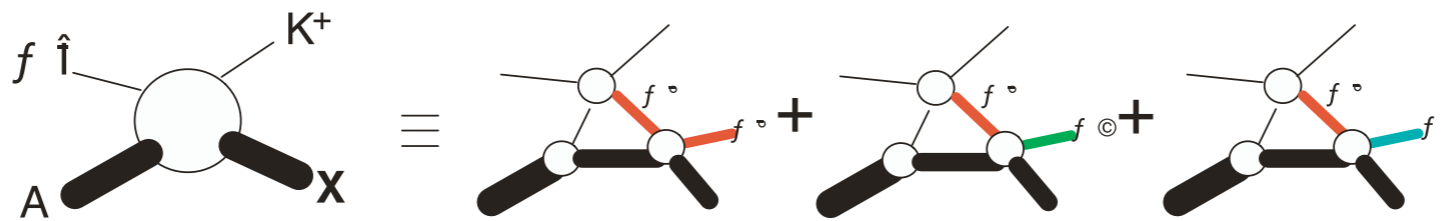
– T. Harada, PRL 81 (1998) 5287.



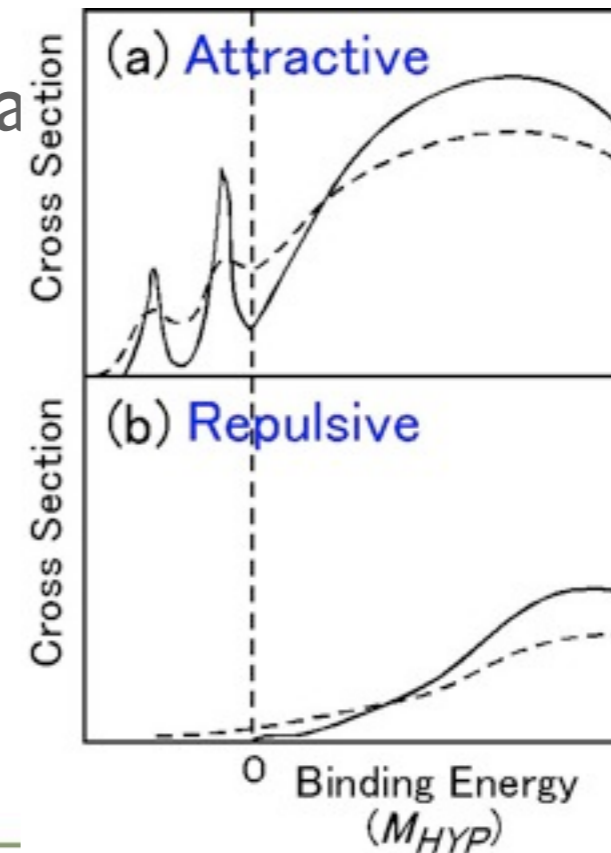
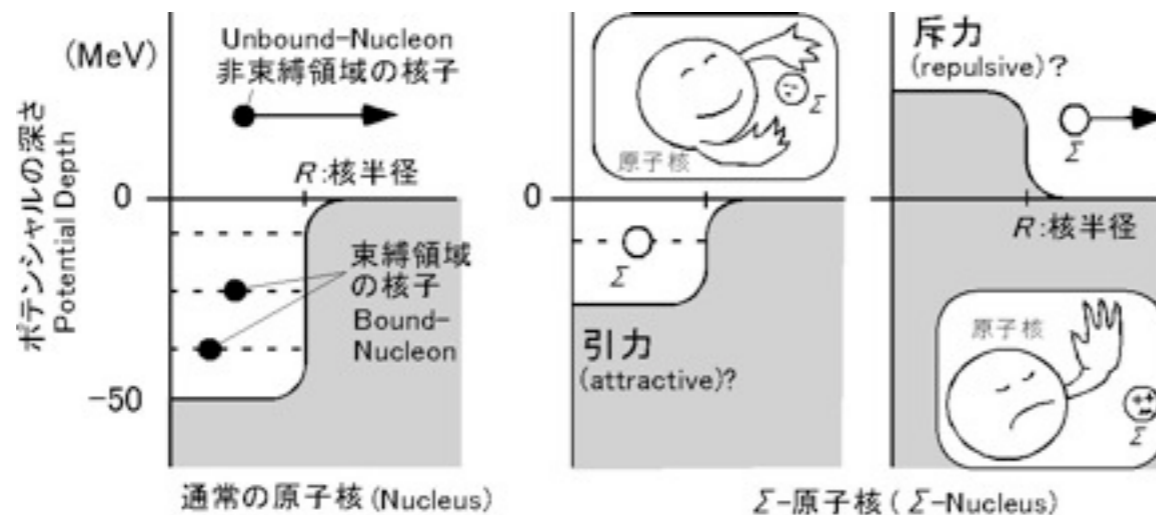
E438: Study of Σ -nucleus potential by the (π^-, K^+) reaction on heavy nuclei

$$U_{\Sigma} = V_{\Sigma} + iW_{\Sigma}$$

No Σ -hypernuclear bound states, but ${}^4_{\Sigma}\text{He}$



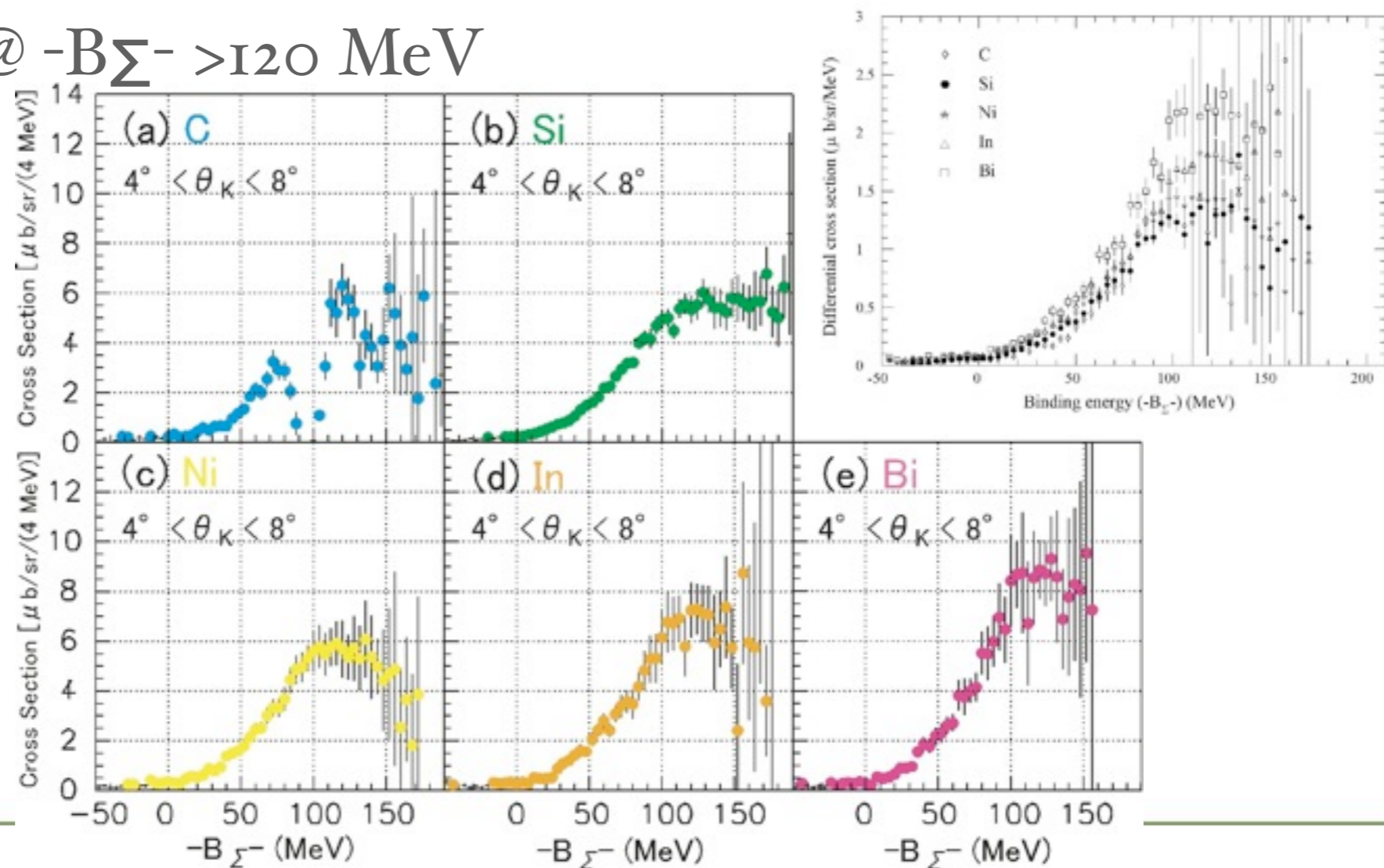
Inclusive spectrum tells the Σ potential

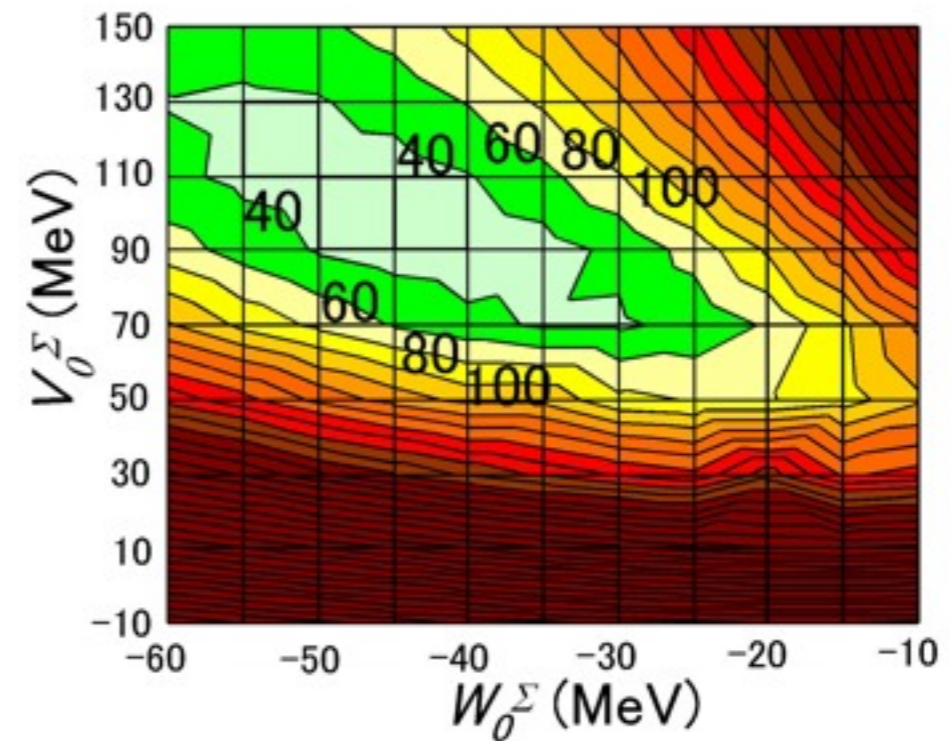
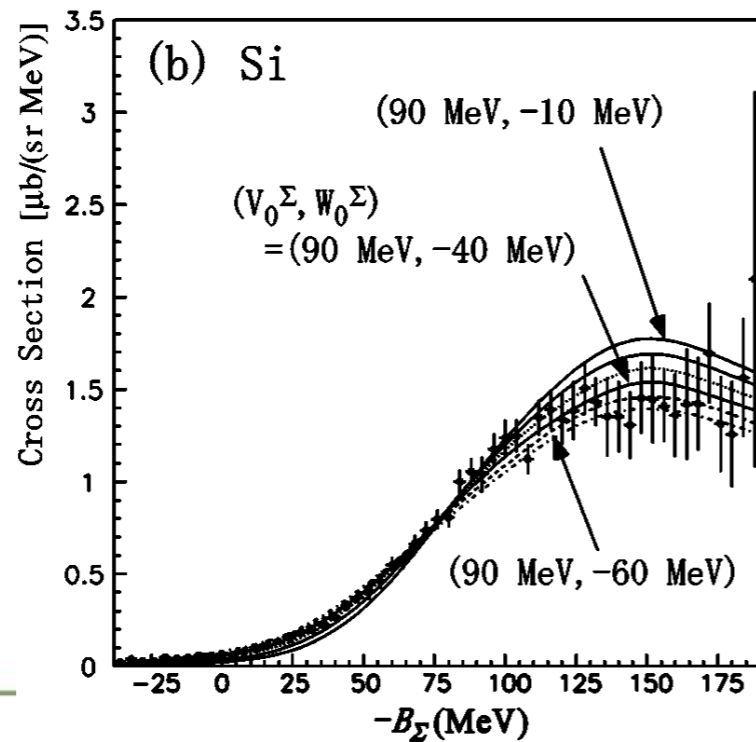
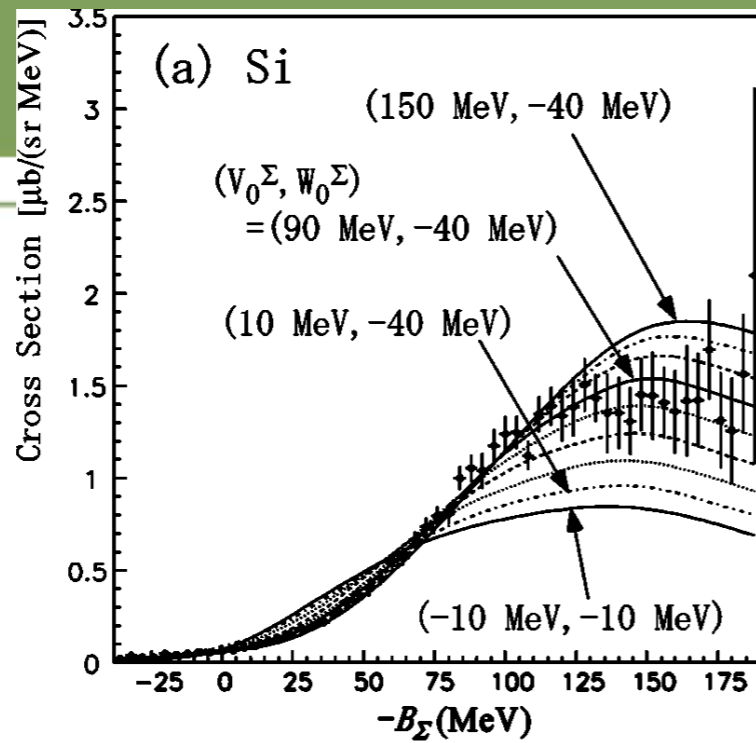


Measured Inclusive (π^- , K^+) Spectra on C, Si, Ni, In, & Bi

- Similar Shape
- No peak in $-B_{\Sigma^-} < 0$ MeV
- Maximum @ $-B_{\Sigma^-} > 120$ MeV

P.K. Saha et al., Phys. Rev. C 70 (2004) 044613.



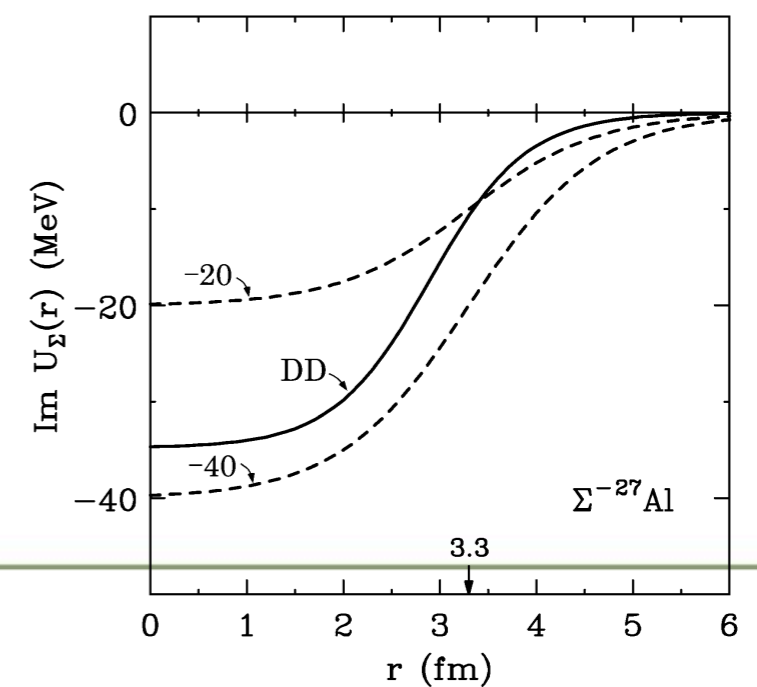
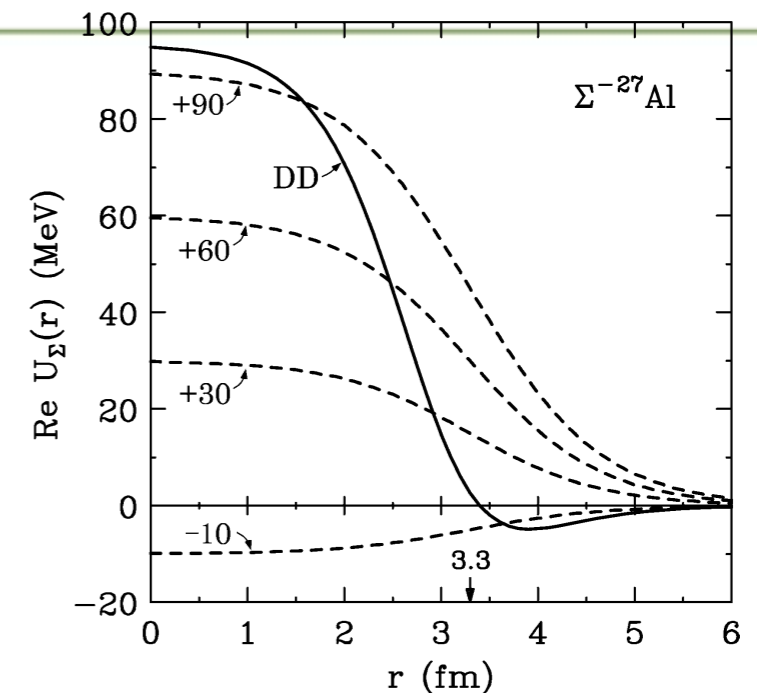
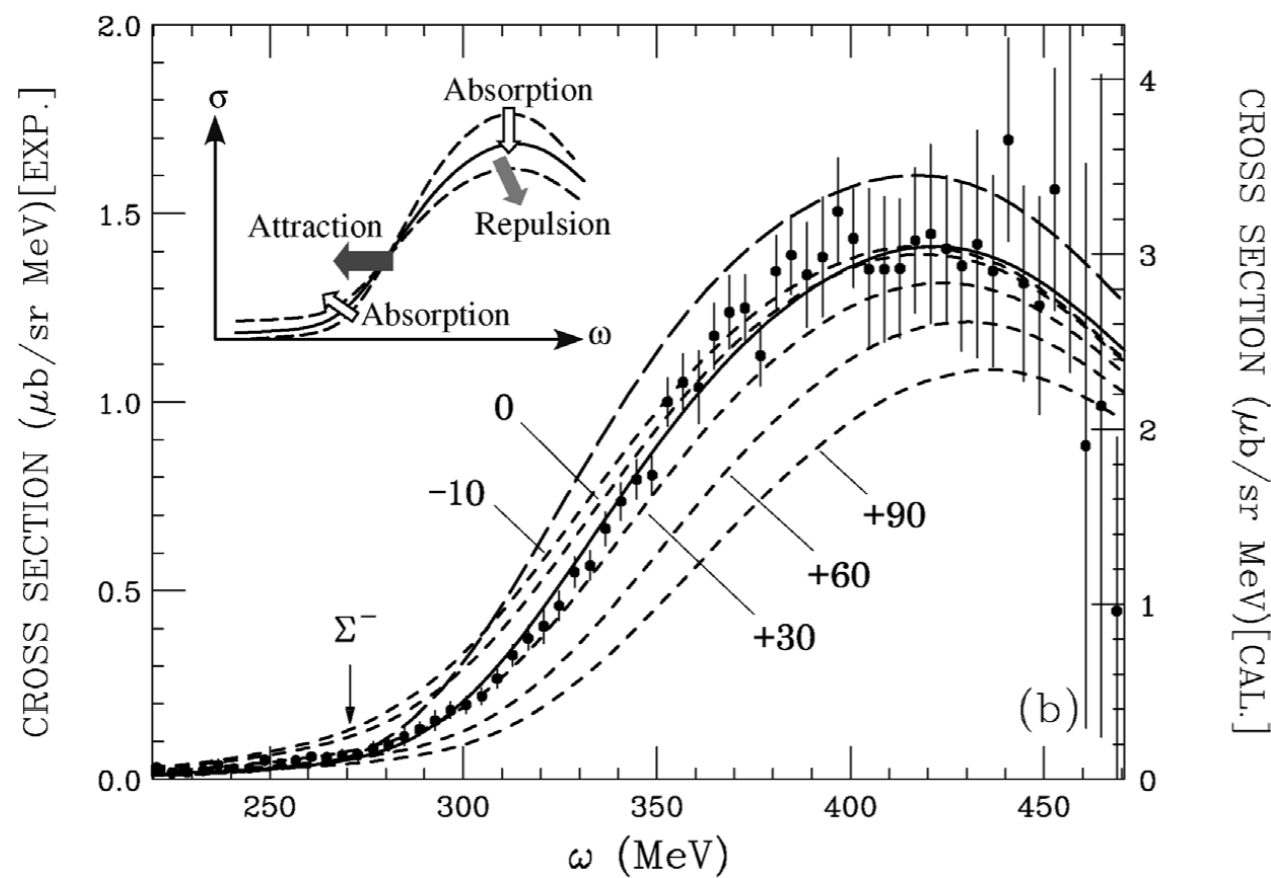


$V_0 = +90 \text{ MeV}, W_0 = -40 \text{ MeV}$

Theoretical analysis by Harada & Hirabayashi

T. Harada, Y. Hirabayashi / Nuclear Physics A 759 (2005) 143–169

► $V_0 = +30$ MeV, $W_0 = -40$ MeV



Summary on Σ hypernuclei

- ▶ No narrow states in unbound region
- ▶ One bound state in ${}^4_{\Sigma}\text{He}$
 - ▶ ${}^7_{\Sigma}\text{Li}$? Nucl. Phys. A 547 (1992) 175c.
- ▶ Σ -Nucleus potential is repulsive in medium-heavy system.

Weak decay of Hypernuclei

W. M. Alberico and G. G., Phys. Rep. **369**, 1 (2002);
Hadron Physics, IOS Press, Amsterdam, 2005, p. 125 [nucl-th/0410059].
E. Oset and A. Ramos, Prog. Part. Nucl. Phys. 41, 191 (1998).

Λ の崩壊

$$\begin{array}{ll} \Lambda \rightarrow \pi^- p & (\text{B.R.} = 63.9 \times 10^{-2}) \\ & \pi^0 n \quad (\text{B.R.} = 35.8 \times 10^{-2}) \end{array}$$

with a lifetime $\tau_{\Lambda}^{\text{free}} \equiv \hbar/\Gamma_{\Lambda}^{\text{free}} = 2.632 \times 10^{-10}$ sec.

$$\begin{array}{ll} \Lambda \rightarrow n\gamma & (\text{B.R.} = 1.75 \times 10^{-3}) \\ & p\pi^- \gamma \quad (\text{B.R.} = 8.4 \times 10^{-4}) \\ & pe^- \bar{\nu}_e \quad (\text{B.R.} = 8.32 \times 10^{-4}) \\ & p\mu^- \bar{\nu}_\mu \quad (\text{B.R.} = 1.57 \times 10^{-4}) \end{array}$$

$\Delta I = 1/2$ 則

$$|\pi^- p\rangle = \sqrt{\frac{1}{3}} \left| \frac{3}{2}, -\frac{1}{2} \right\rangle - \sqrt{\frac{2}{3}} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle,$$
$$|\pi^0 n\rangle = \sqrt{\frac{2}{3}} \left| \frac{3}{2}, -\frac{1}{2} \right\rangle + \sqrt{\frac{1}{3}} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle.$$

Hence the ratio of amplitudes for $\Delta I = 1/2$ transitions yields:

$$\frac{\Gamma_{\Lambda \rightarrow \pi^- p}^{\text{free}}}{\Gamma_{\Lambda \rightarrow \pi^0 n}^{\text{free}}} \simeq \frac{|\langle \pi^- p | T_{1/2, -1/2} | \Lambda \rangle|^2}{|\langle \pi^0 n | T_{1/2, -1/2} | \Lambda \rangle|^2} = \left| \frac{\sqrt{2/3}}{\sqrt{1/3}} \right|^2 = 2,$$

while a $\Delta I = 3/2$ process should give:

$$\frac{\Gamma_{\Lambda \rightarrow \pi^- p}^{\text{free}}}{\Gamma_{\Lambda \rightarrow \pi^0 n}^{\text{free}}} \simeq \frac{|\langle \pi^- p | T_{3/2, -1/2} | \Lambda \rangle|^2}{|\langle \pi^0 n | T_{3/2, -1/2} | \Lambda \rangle|^2} = \left| \frac{\sqrt{1/3}}{\sqrt{2/3}} \right|^2 = \frac{1}{2}.$$

$$\left\{ \frac{\Gamma_{\Lambda \rightarrow \pi^- p}^{\text{free}}}{\Gamma_{\Lambda \rightarrow \pi^0 n}^{\text{free}}} \right\}^{\text{Exp}} \simeq 1.78,$$

$$\left| \frac{A_{1/2}}{A_{3/2}} \right| \simeq 30.$$

ハイパー核の弱崩壊

▶ 中間子崩壊モード

▶ $\Lambda \rightarrow \pi N$ ($Q \sim 37$ MeV)



$p_N(90 \text{ MeV}/c) < p_F$

Pauli Suppressed

▶ 非中間子崩壊モード

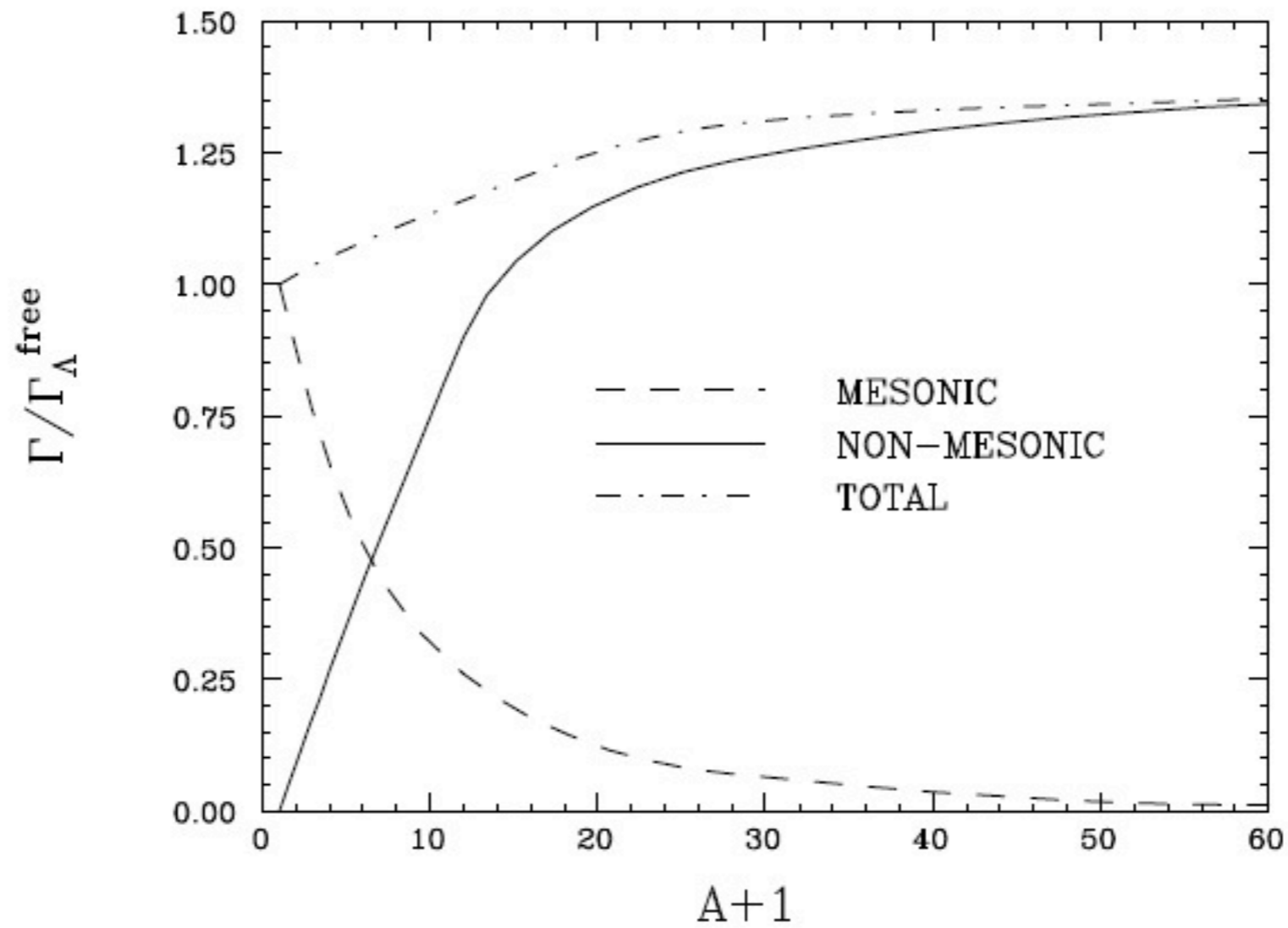
▶ $\Lambda N \rightarrow NN$ ($Q \sim 176$ MeV)



$p_N(400 \text{ MeV}/c) > p_F$

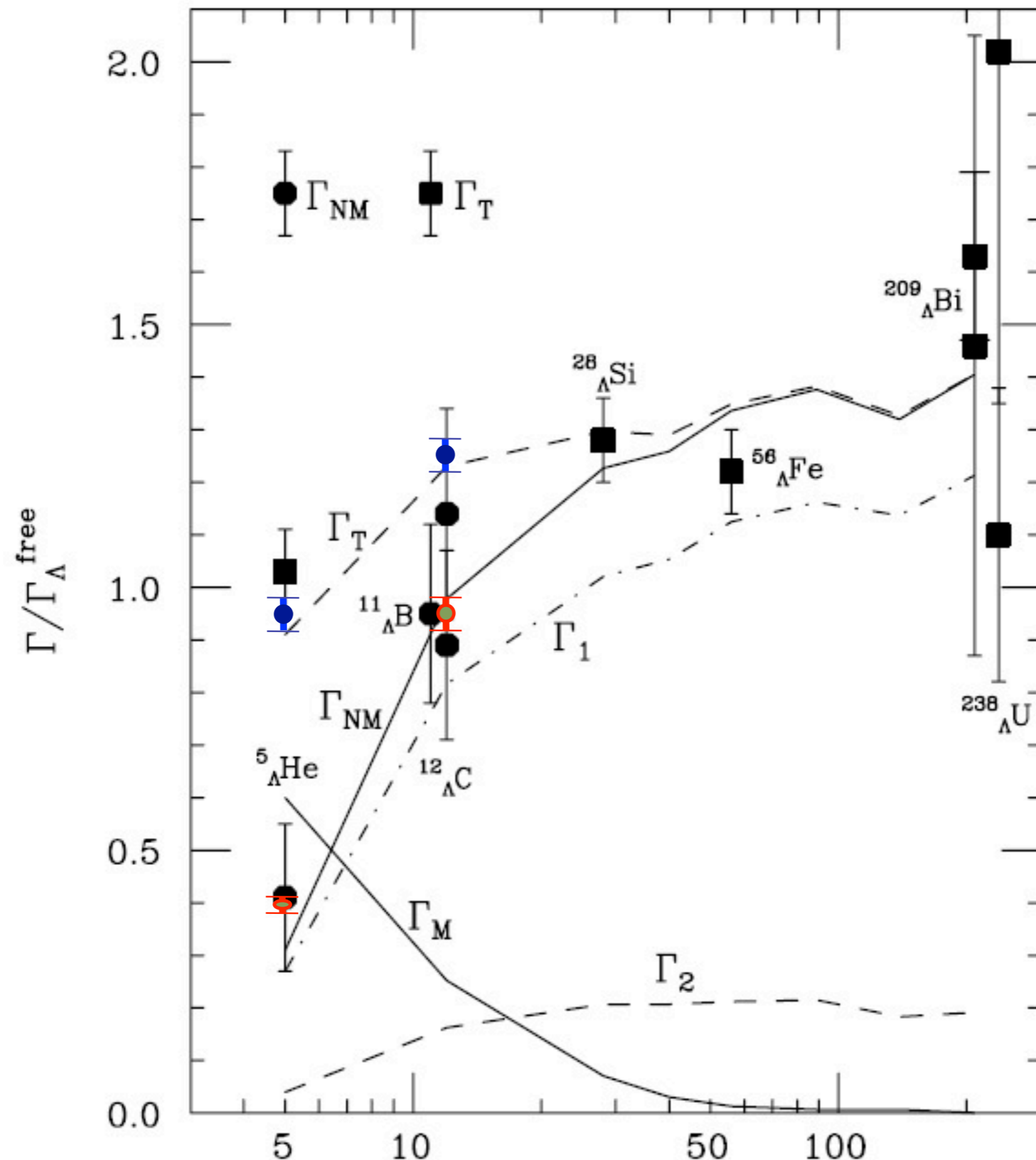
$$\Gamma_T = \Gamma_M + \Gamma_{NM},$$

$$\Gamma_M = \Gamma_{\pi^-} + \Gamma_{\pi^0}, \quad \Gamma_{NM} = \Gamma_1 + \Gamma_2, \quad \Gamma_1 = \Gamma_n + \Gamma_p,$$



$$\Gamma_1(A) \propto \int d\vec{r} |\psi_{\Lambda}(\vec{r})|^2 \rho_A(\vec{r}),$$

Mass number dependence of Γ_{NM}



NON-MESONIC WEAK DECAY OF HYPERNUCLEI

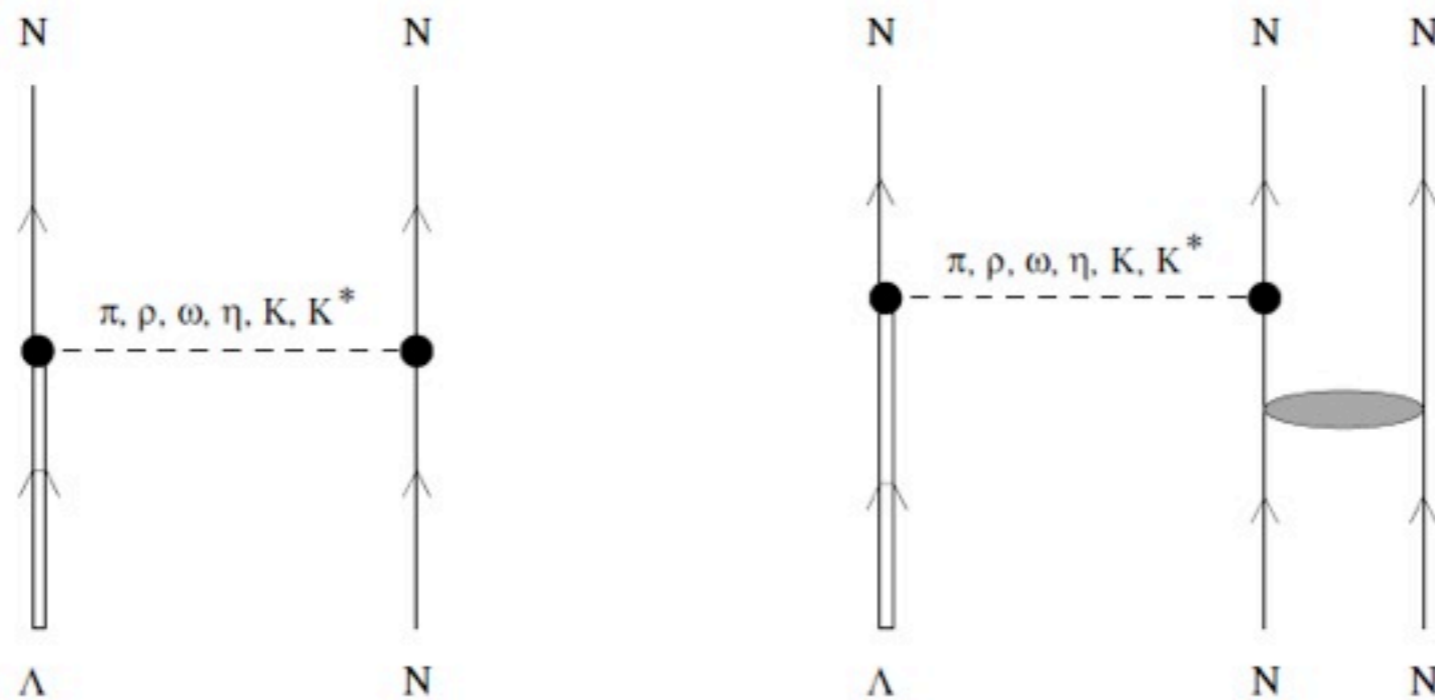
One-nucleon induced

$$\Lambda n \rightarrow nn \quad \Gamma_n$$

$$\Lambda p \rightarrow np \quad \Gamma_p$$

Two-nucleon induced

$$\Lambda NN \rightarrow nNN \quad \Gamma_2$$

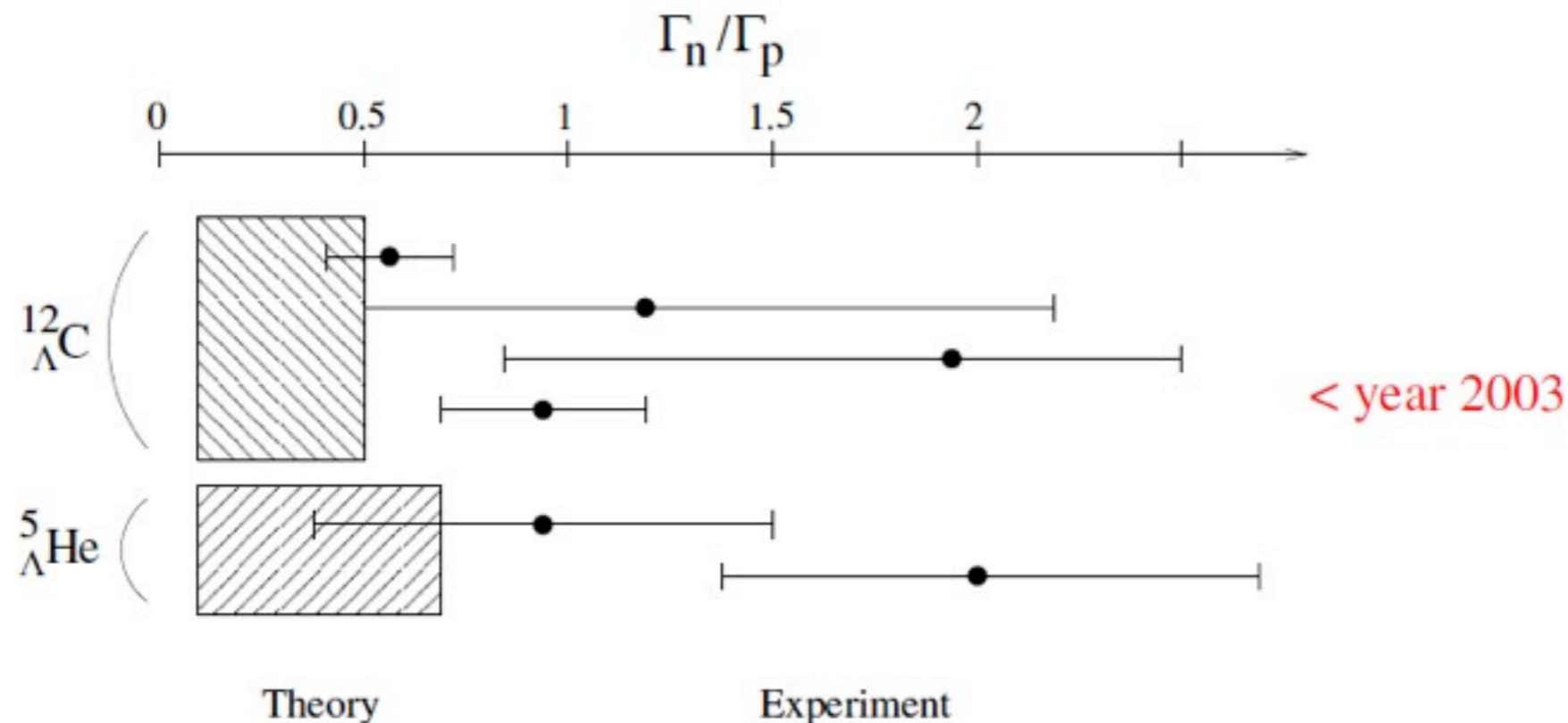


$$\Gamma_T = \Gamma_M + \Gamma_{NM} = \Gamma_{\pi^0} + \Gamma_{\pi^-} + \Gamma_n + \Gamma_p + \Gamma_2$$

Γ_n/Γ_p パズル

THE RATIO Γ_n/Γ_p

For many years, a sound theoretical explanation of the large experimental values of $\frac{\Gamma_n}{\Gamma_p} \equiv \frac{\Gamma(\Lambda n \rightarrow nn)}{\Gamma(\Lambda p \rightarrow np)}$ has been missing



Theory strongly underestimated Experiment!

[W. M. Alberico and G. G., Phys. Rep. 369, 1 (2002)]

[E. Oset and A. Ramos, Prog. Part. Nucl. Phys. 41, 191 (1998)]

Experiment

◆ Large uncertainties in the extraction of Γ_n/Γ_p from “old” data (< year 2002)

– only Single-Proton Spectra measured

– very indirect determination of the decay rates, probable overestimation of

$$\frac{\Gamma_n}{\Gamma_p} = \frac{\Gamma_T - \Gamma_M - \Gamma_2 - \Gamma_p}{\Gamma_p} \iff \Gamma_p \text{ underestimated, } \Gamma_2 \text{ neglected}$$

$$\left(\Gamma_2 = 0, \Gamma_p = 0.8[\Gamma_p]^{\text{th}} : \frac{\Gamma_n}{\Gamma_p} = 1 \iff \left[\frac{\Gamma_n}{\Gamma_p} \right]^{\text{th}} = 0.3 \right)$$

◆ KEK-E462/E508: simultaneous measurement of Single-Proton and Single-Neutron Spectra (year 2003) [1]

– improved determination of $\frac{\Gamma_n}{\Gamma_p}$ from $\frac{N_n}{N_p}$ ratio

◆ KEK-E462/E508: Nucleon-Nucleon Coincidence Spectra (years 2003–2006) [2]

– more direct determination of $\frac{\Gamma_n}{\Gamma_p}$ from $\frac{N_{nn}}{N_{np}}$ ratio

◆ First data from FINUDA@DAΦNE, experiments planned at J-PARC and HypHI@GSI

[1] S. Okada et al., PLB 597, 249 (2004)

[2] B. H. Kang et al., PRL 96, 062301 (2006); M. J. Kim et al., PLB 641, 28 (2006)

Theory

- ◆ The One-Pion-Exchange (OPE) model predicts very small ratios:

$$\left[\frac{\Gamma_n}{\Gamma_p} \right]^{\text{OPE}} \left({}^5_{\Lambda}\text{He}, {}^{12}_{\Lambda}\text{C} \right) = 0.1 \div 0.2$$

$[\Delta I = 1/2 \text{ rule} + \text{strong tensor component } \Lambda N({}^3S_1) \rightarrow nN({}^3D_1) \text{ requiring } I_{nN} = 0 \iff N = p]$

- ◆ but the OPE reproduces the observed total non-mesonic rates,
 $\Gamma_{\text{NM}} = \Gamma_n + \Gamma_p(+\Gamma_2)$.

Other **interaction mechanisms beyond the OPE** should then be responsible for the **overestimation of Γ_p** and the **underestimation of Γ_n**

- ◆ Heavier Mesons ($\rho, K, K^*, \omega, \eta, 2\pi, 2\pi/\rho, 2\pi/\sigma$) [Parreño et al., Itonaga et al., Jido et al.]
- ◆ Direct Quark Mechanism [Oka et al.]
- ◆ Two-Nucleon Induced Mechanism [Alberico et al., Ramos et al.]
- ◆ Nucleon Final State Interactions [Ramos et al., Garbarino et al.]

History of hypernuclear weak decay experiments...

Year	Method	<ul style="list-style-type: none"> * Clean decay identification → ground state spin assignment * Low energy threshold for p 	<div style="border: 1px solid black; padding: 5px; text-align: center;"> Merit/ Demerit </div>
~1960	Emulsion and Bubble chamber	<ul style="list-style-type: none"> * Hypernuclear formation is not identified * Blind for neutral particles * No timing information 	
1985	Counter experiment start @BNL/KEK w/ (K,π)	<ul style="list-style-type: none"> * Hypernuclear formation tagged → branching ratio ! * Direct lifetime meas. w/TOF counter 	
1995	SKS experiments w/ (π,K) reaction	<ul style="list-style-type: none"> * Still hard to see neutral particles * High energy threshold for p ($E_p > 30 \sim 40 \text{ MeV}$) 	
2000~2002	n+p/n+n coincidence	<ul style="list-style-type: none"> * Heavy Λ hypernuclear production * Neutral particle detection * Asymmetry of p from NMWD * Improved statistics 	$\Gamma_m \left\{ \begin{array}{l} \Gamma_{\pi^-} (\Lambda \rightarrow p + \pi^-) \\ \Gamma_n (\Lambda \rightarrow n + \pi^0) \end{array} \right.$
2004~	<p style="text-align: center;">New era started!</p> <p style="text-align: center;">→ FINUDA@DAFNE / J-PARC</p>	<ul style="list-style-type: none"> → n+p/n+n double coincidence 	$\Gamma_{nm} \left\{ \begin{array}{l} \Gamma_p (\Lambda + \text{"p"} \rightarrow n + p) \\ \Gamma_n (\Lambda + \text{"n"} \rightarrow n + n) \end{array} \right.$

Γ_n/Γ_p ratio

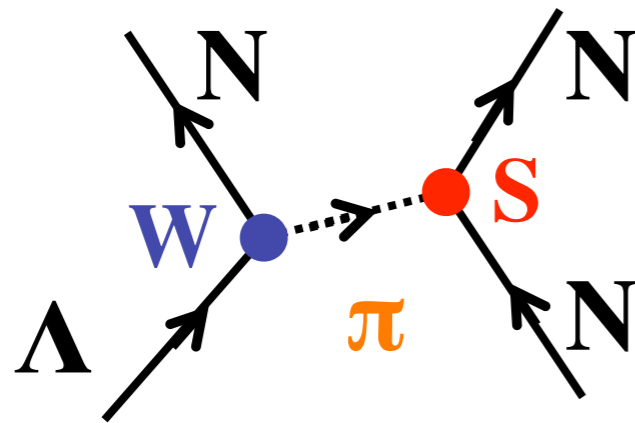
: The most important observable used to study the isospin structure of the NMWD.

Simple theoretical model

$$\Gamma_p (\Lambda + \text{“p”} \rightarrow n + p)$$
$$\Gamma_n (\Lambda + \text{“n”} \rightarrow n + n)$$

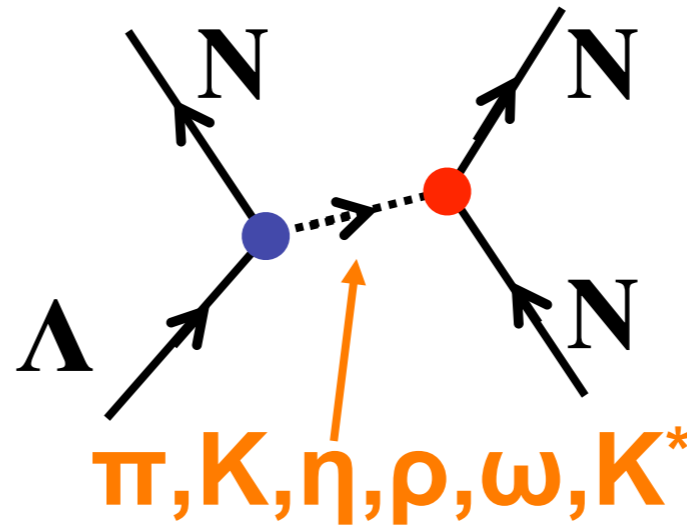
$$\Rightarrow \Gamma_n / \Gamma_p \sim 0.1$$

One Pion Exchange (OPE)

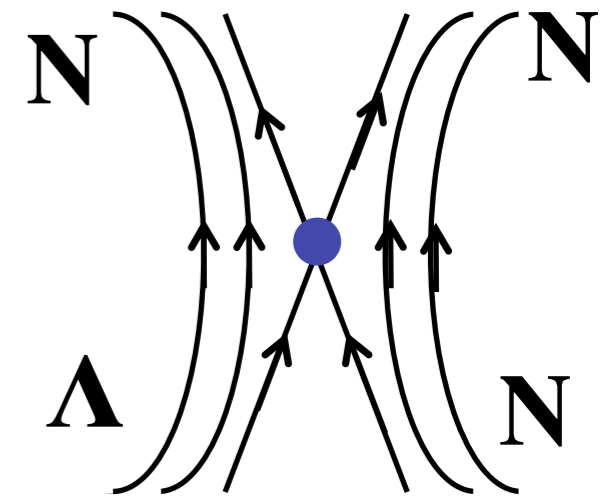


Tensor-dominant
→ requires the **final Nn** pair to have isospin 0.

Meson Exchange mechanism



Direct Quark mechanism



Theoretical

Γ_n / Γ_p

0

0.5

1

1.5

Exp. (for $^5_\Lambda\text{He}$)

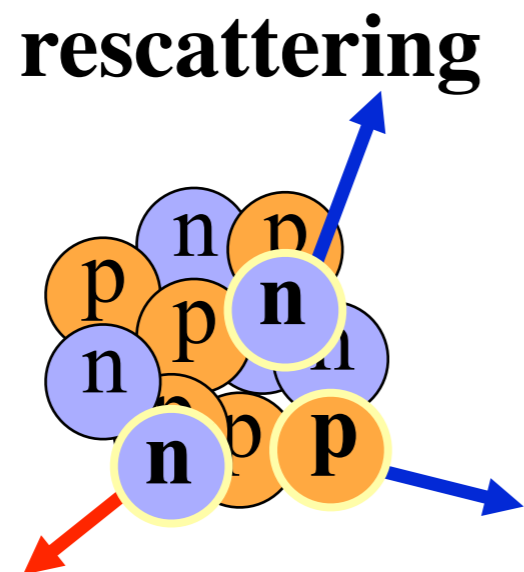
0.93 ± 0.55 (Szymanski et al.)

Γ_n / Γ_p ratio puzzle

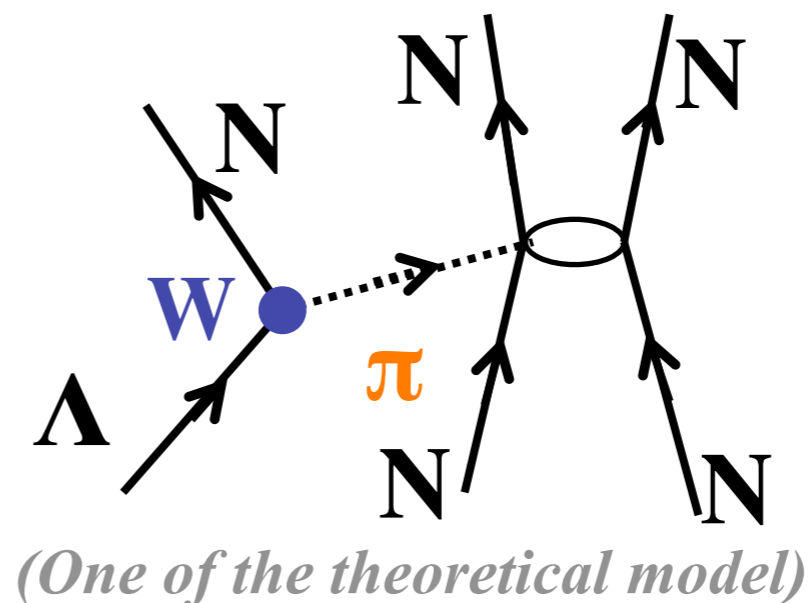
Experimental difficulties in single nucleon measurement

- ✓ **Difficulty in detecting neutrons.**
→ There is no experiment to observe both of the protons and neutrons simultaneously with high statistics.
- ✓ **Final state interaction (FSI) effect**
→ not well established
- ✓ Distinguish between the FSI and " **$\Lambda NN \rightarrow nNN$** " process

Final state interaction (FSI) effect



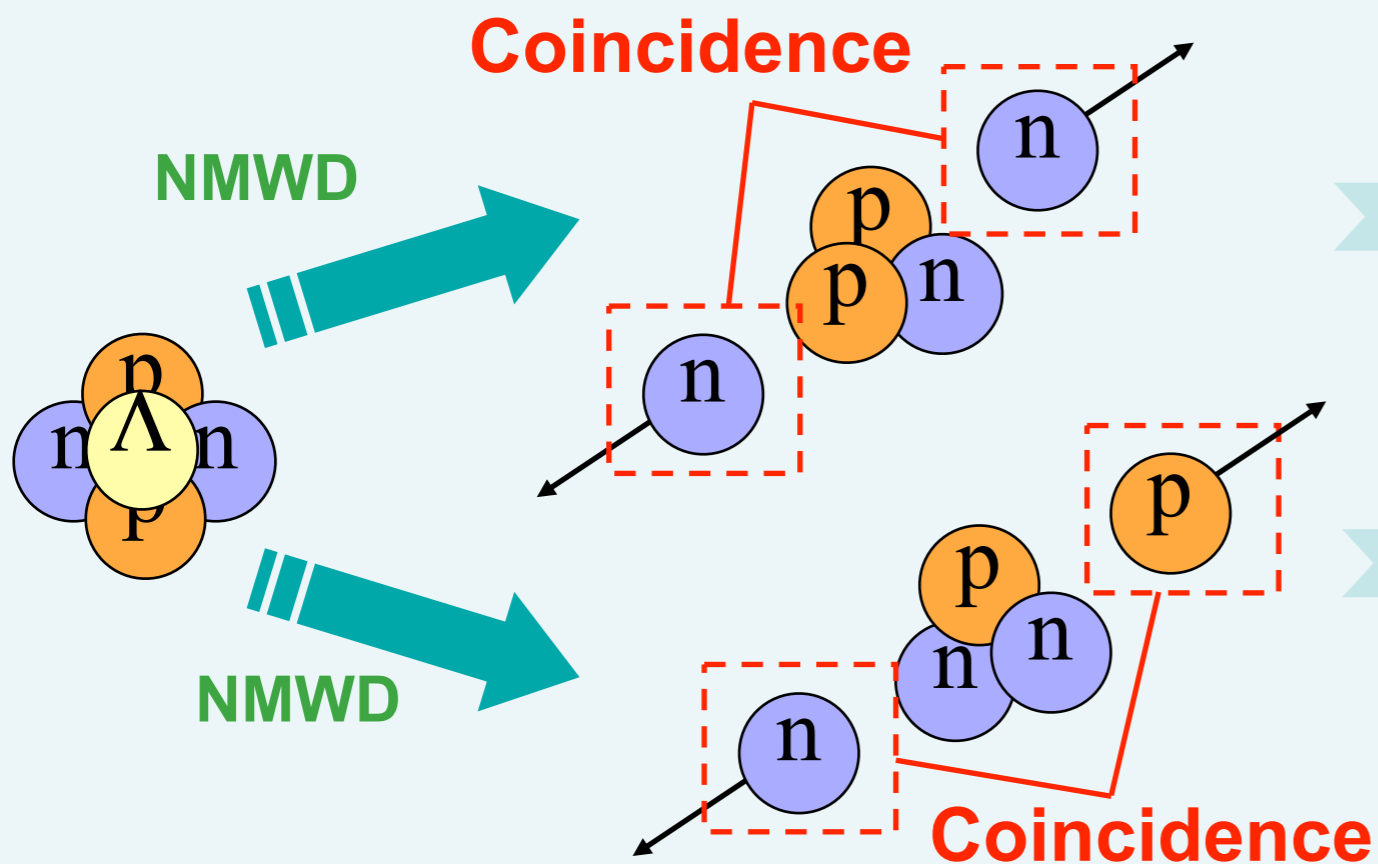
$\Lambda NN \rightarrow NNN$
(2N-induced process)



The present experiment

KEK-PS E462/E508

NMWD : $\Lambda N \rightarrow NN$



Direct measurement
of the Γ_n / Γ_p ratio

⇒ Select $\Lambda N \rightarrow NN$ events
w/o FSI effect & $\Lambda NN \rightarrow NNN$.

$$N(\Lambda n \rightarrow nn) \times (\Omega_n \times \Omega_n)_{av.} \times \varepsilon_n^2 \times (1 - R_{FSI})$$

$$N(\Lambda p \rightarrow np) \times (\Omega_n \times \Omega_p)_{av.} \times \varepsilon_n \times \varepsilon_p \times (1 - R_{FSI})$$

* $\cos\theta < -0.8$

* $E(N1) + E(N2)$ cut

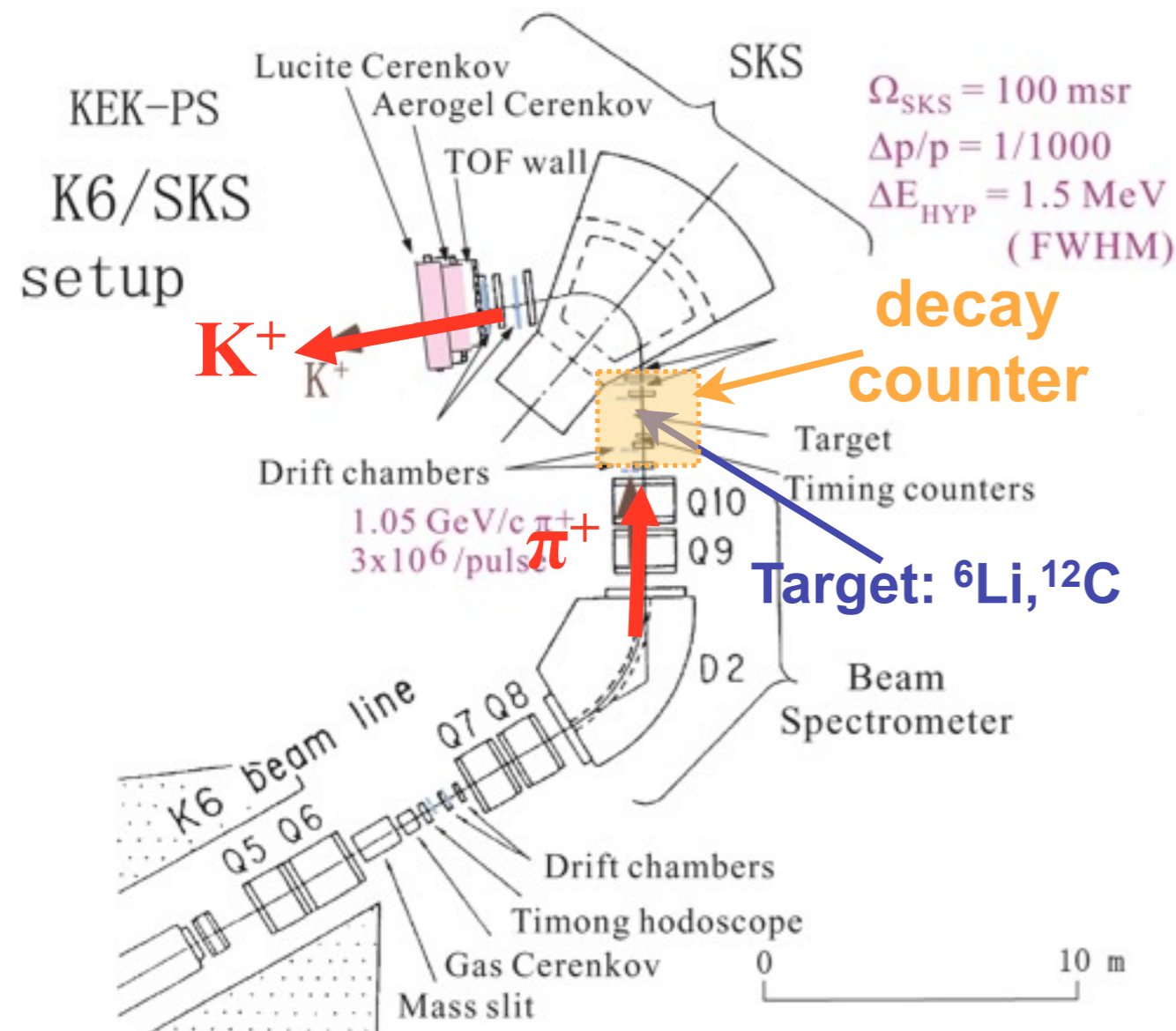
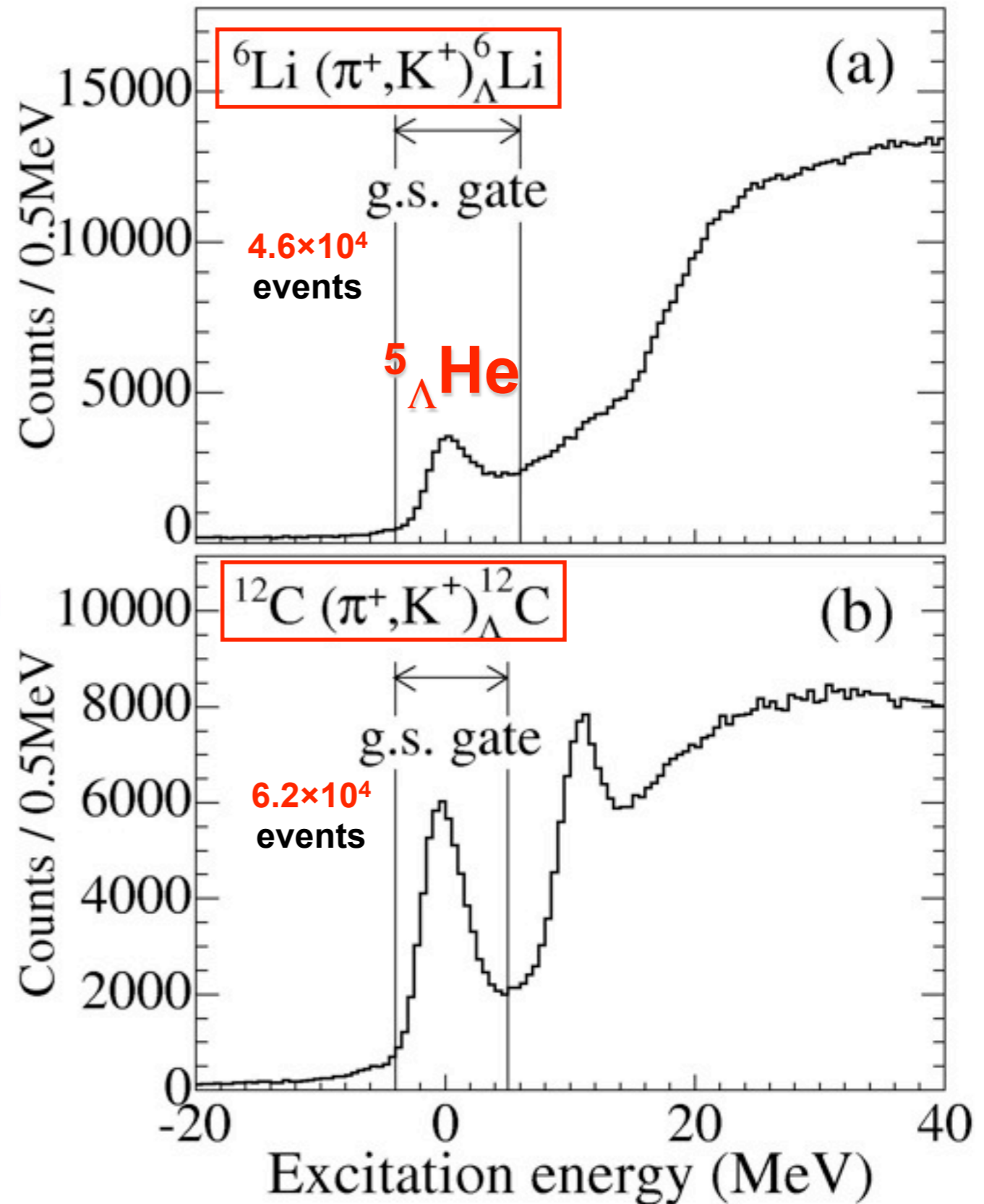
$$\frac{\Gamma_n}{\Gamma_p} = \frac{N(nn - \text{pair coin})}{N(np - \text{pair coin})} \times \frac{\varepsilon_p}{\varepsilon_n}$$

- 1) Angular correlation
(back-to-back, $\cos\theta < -0.8$)
- 2) Energy correlation
($Q \sim E(N1) + E(N2) \sim 152\text{MeV}$)

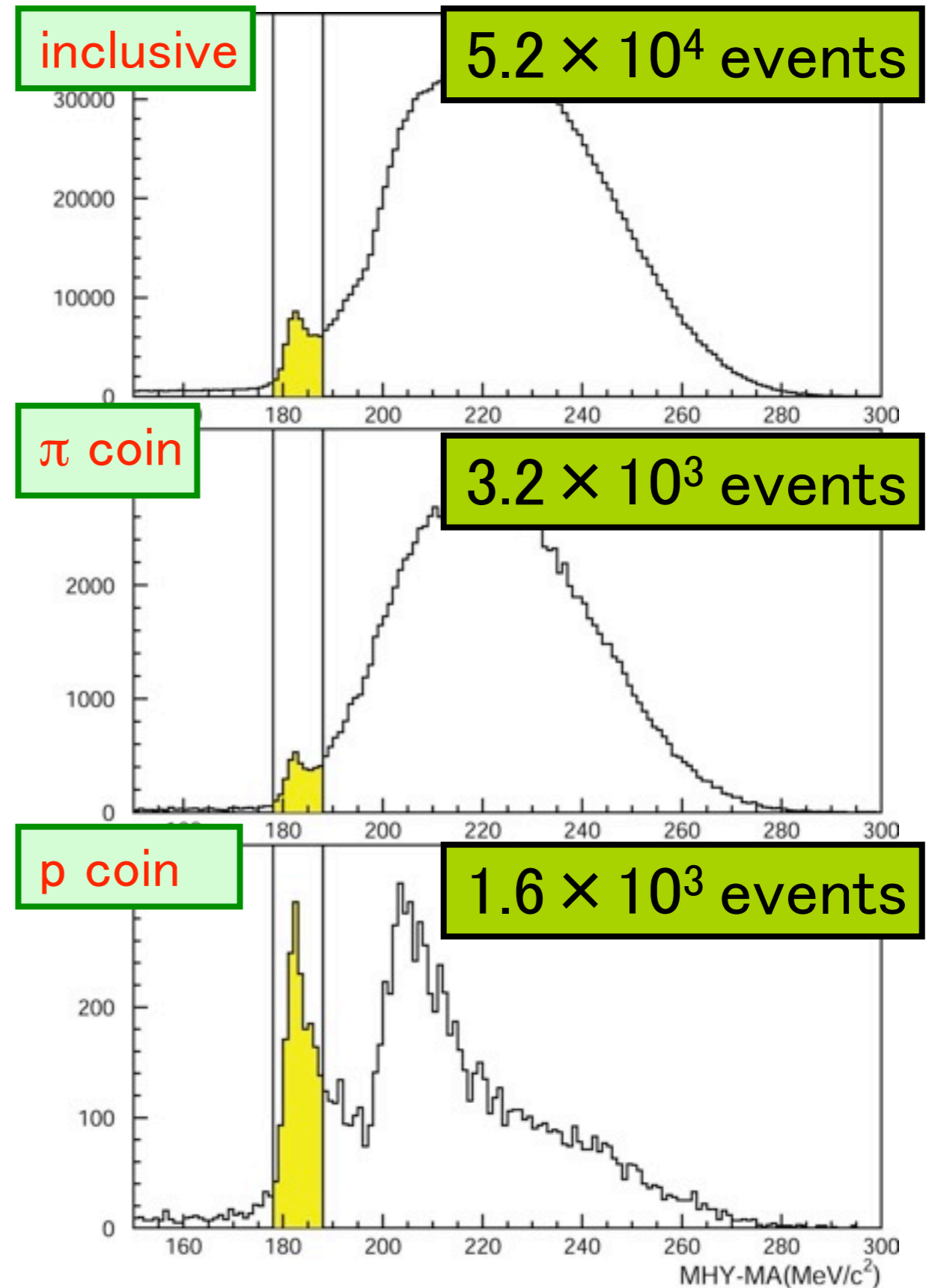
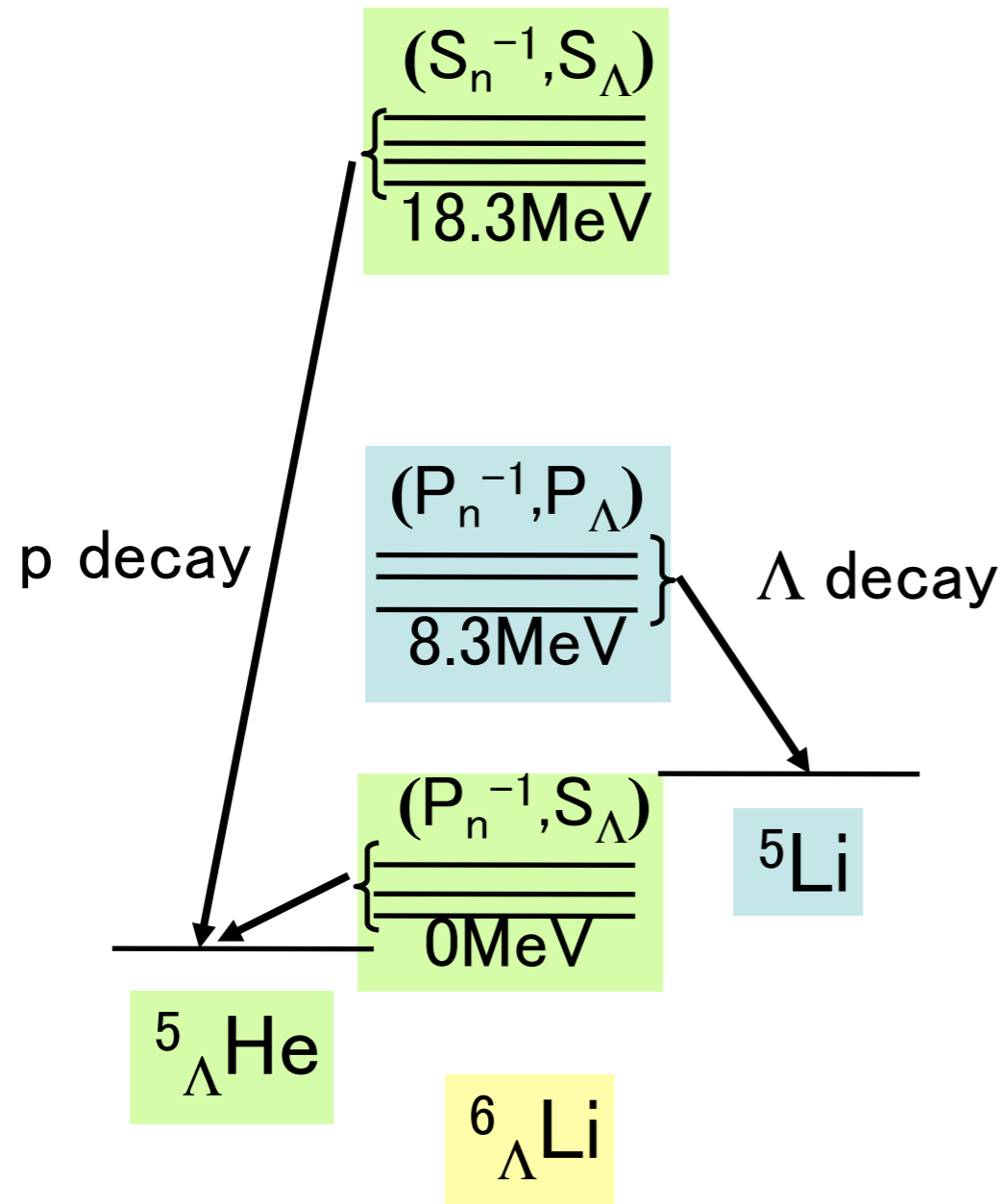
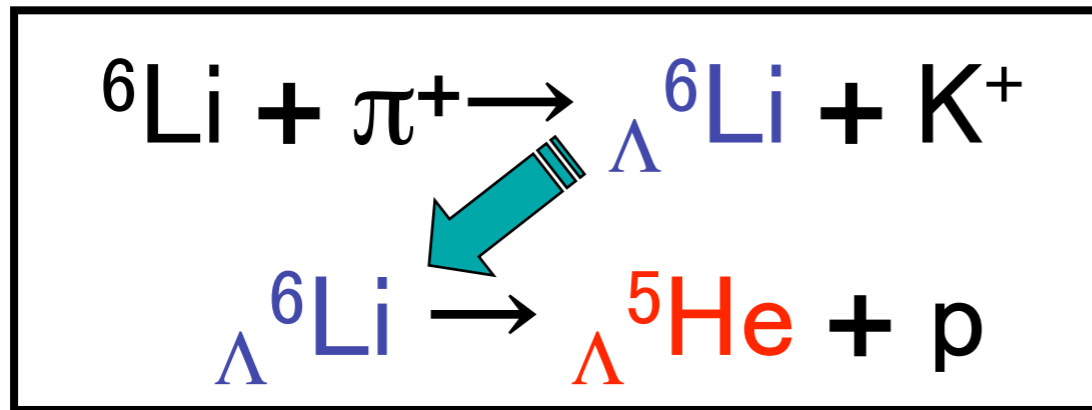
Select light hypernuclei to minimize FSI effect, ${}^5_{\Lambda}\text{He}$ and ${}^{12}_{\Lambda}\text{C}$

Excitation-energy spectra for ${}^6_{\Lambda}\text{Li}$ and ${}^{12}_{\Lambda}\text{C}$

The ground state of ${}^6_{\Lambda}\text{Li}$ is **above** the threshold of ${}^5_{\Lambda}\text{He} + p$.



${}^6_{\Lambda}\text{Li}$ Hypernuclear mass spectra

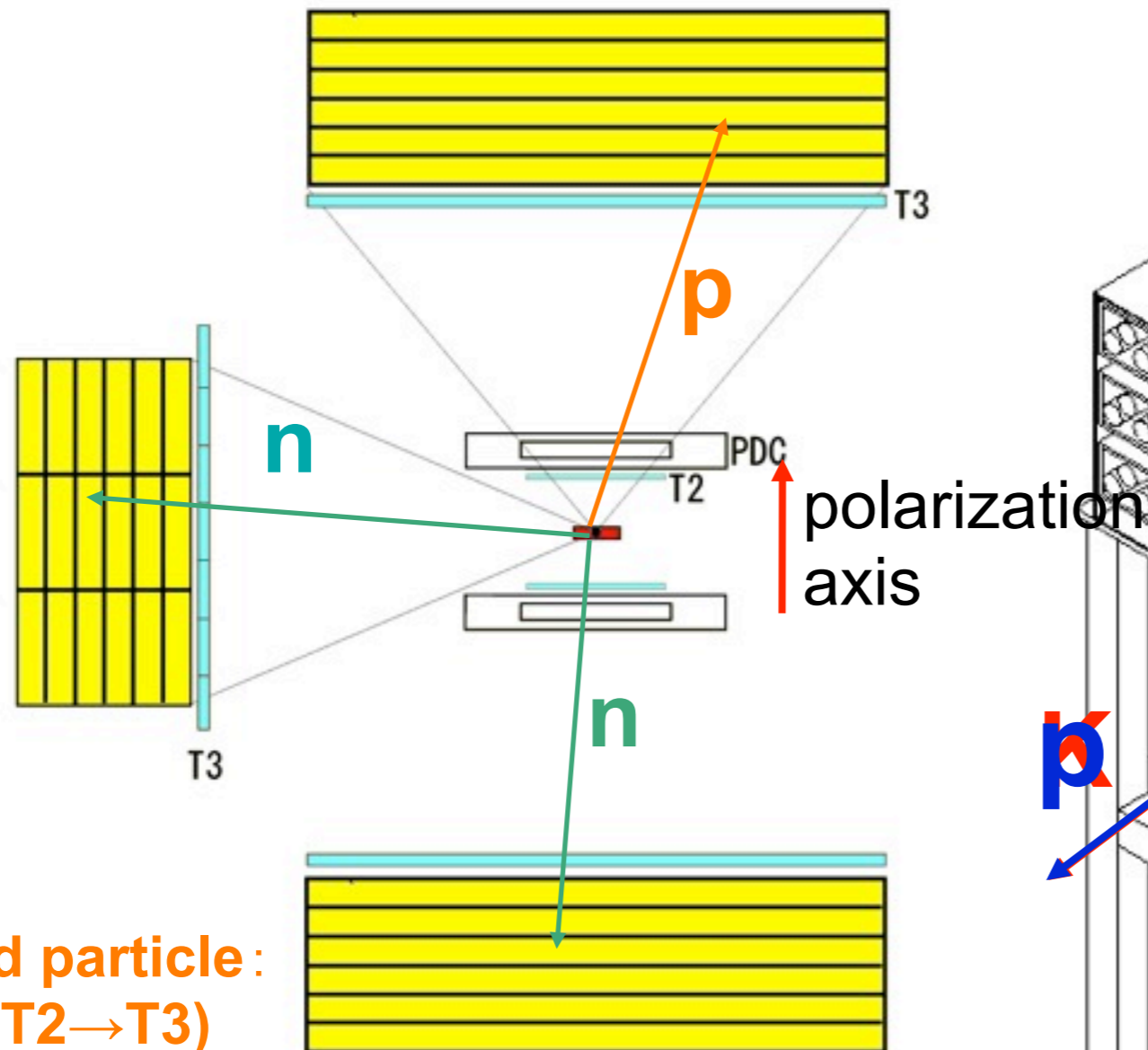


Decay counter Setup

(KEK-PS K6 & SKS)

Solid angle: 26%
9(T)+9(B)+8(S)%

Decay arm



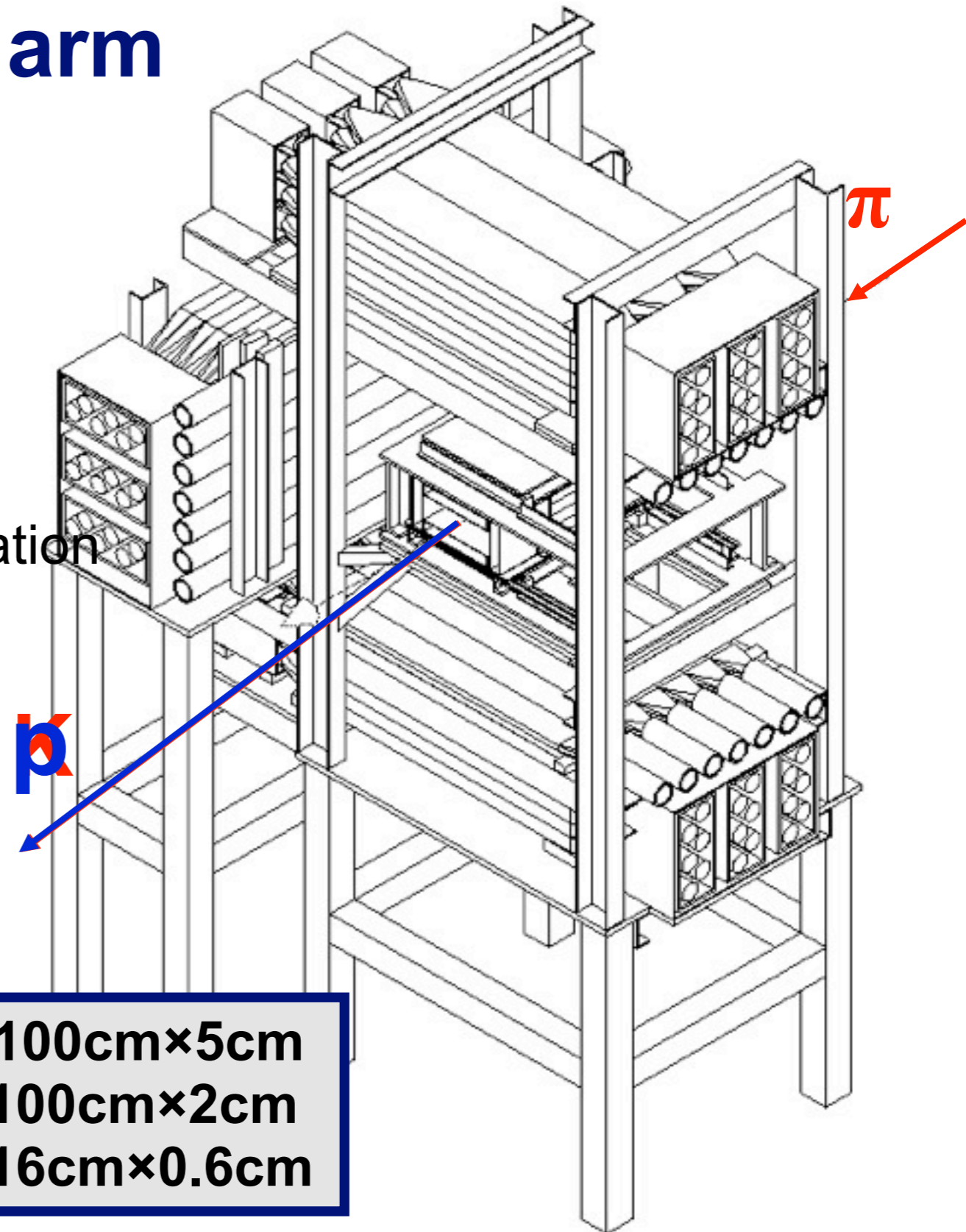
Charged particle:

- TOF (T2→T3)
- tracking (PDC)

Neutral particle:

- TOF (target→NT)
- T3 VETO

N: 20cm×100cm×5cm
T3: 10cm×100cm×2cm
T2: 4cm×16cm×0.6cm



Excitation spectra w/ coincident decay particles for $^{12}_{\Lambda}C$

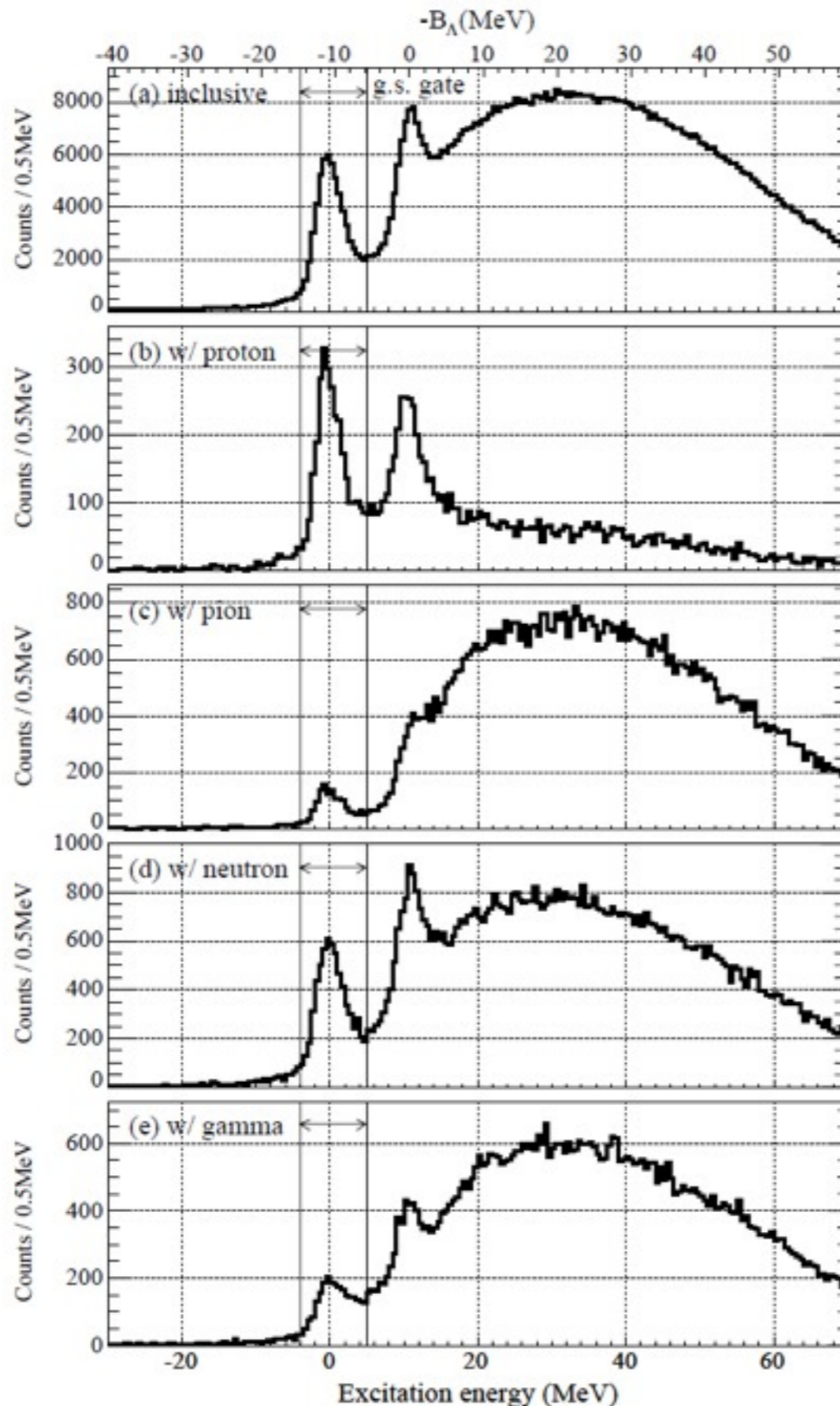
inclusive

w/ proton

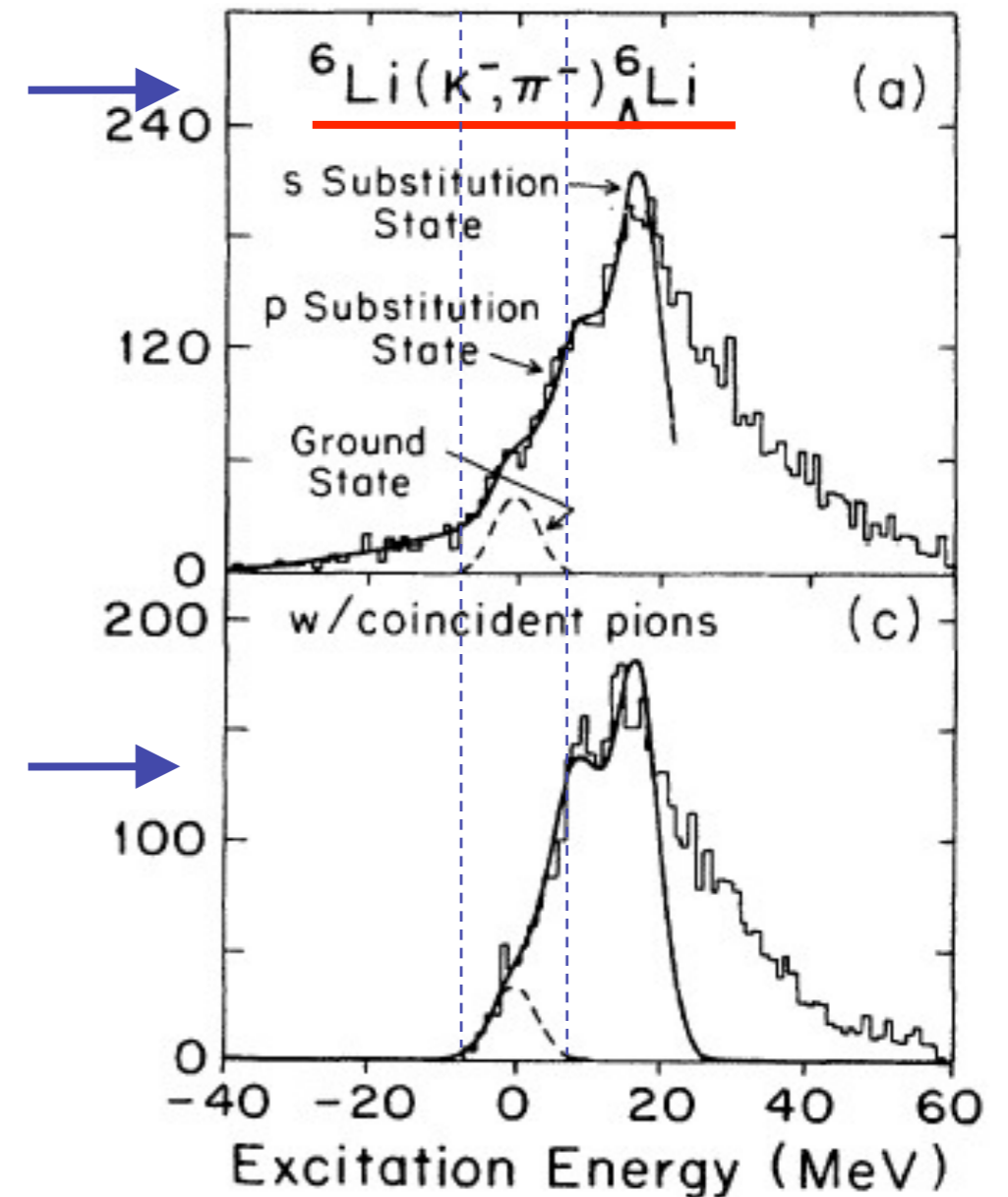
w/ π^{\pm}

w/ neutron

w/ gamma



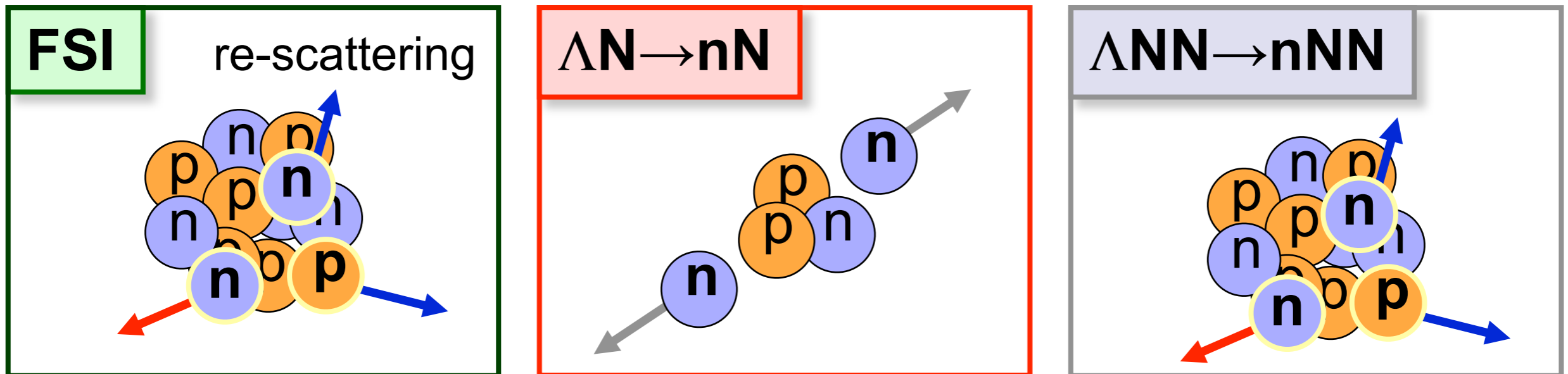
previous experiment at BNL



The **g.s. peak** is clearly seen in all spectra with coincident decay particles.

- . Kameoka *et al.* Nucl. Phys. A754 (2005) 173c
- . Okada *et al.* Nucl. Phys. A754 (2005) 178c

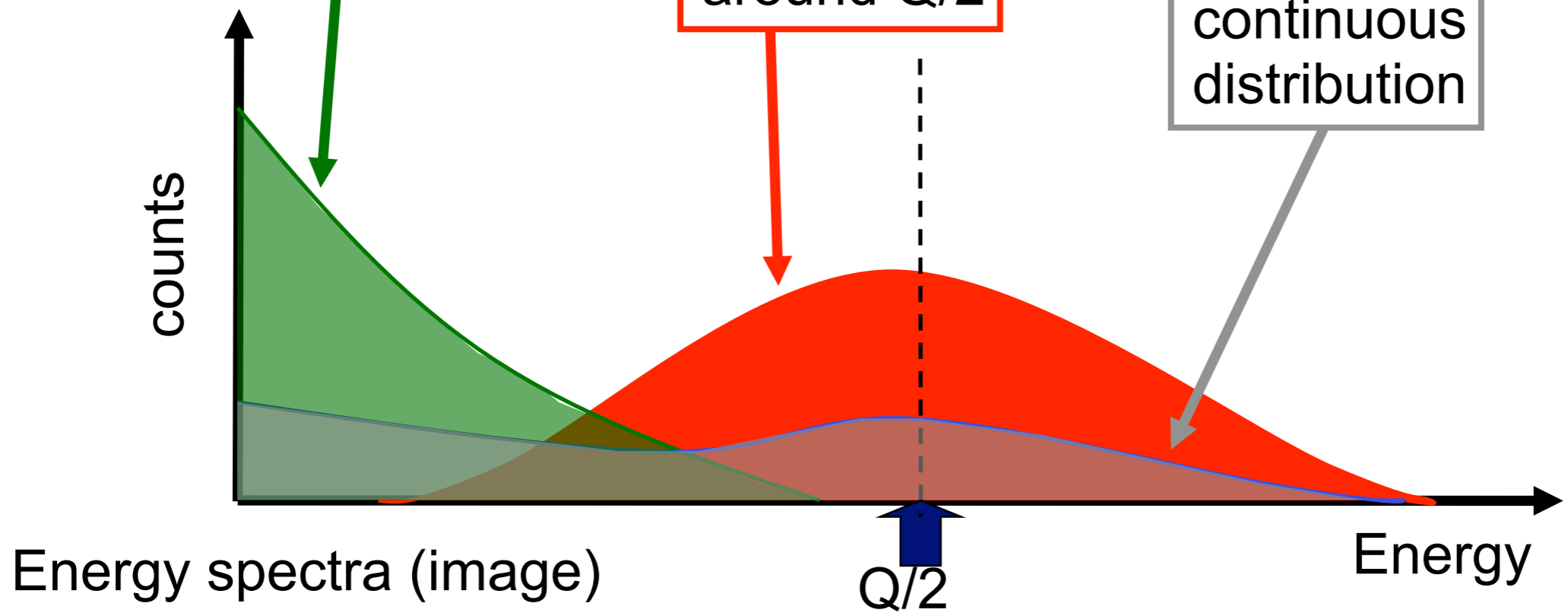
Expected Spectrum



distribute low energy region up to $Q/2$

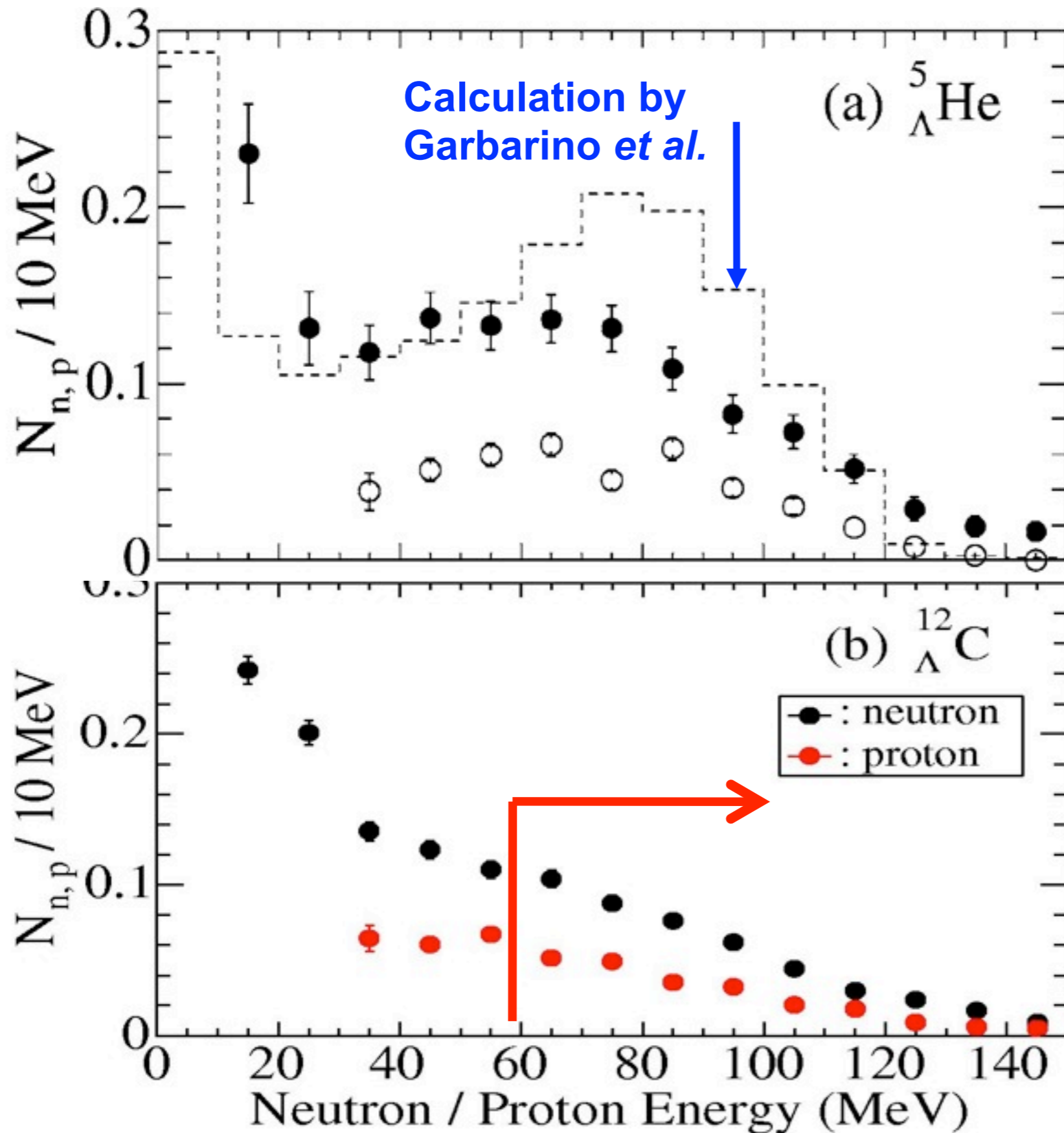
broad peak around $Q/2$

continuous distribution



Energy spectra (image)

Single proton/neutron spectra from ${}^5_{\Lambda}\text{He}$ and ${}^{12}_{\Lambda}\text{C}$



$$N_n \sim 2N_p$$

$$N_n/N_p \cong 2 \times (\Gamma_n/\Gamma_p) + 1.$$

$$N_n/N_p({}^5_{\Lambda}\text{He}) = 2.17 \pm 0.15(\text{stat}) \pm 0.16(\text{sys})$$

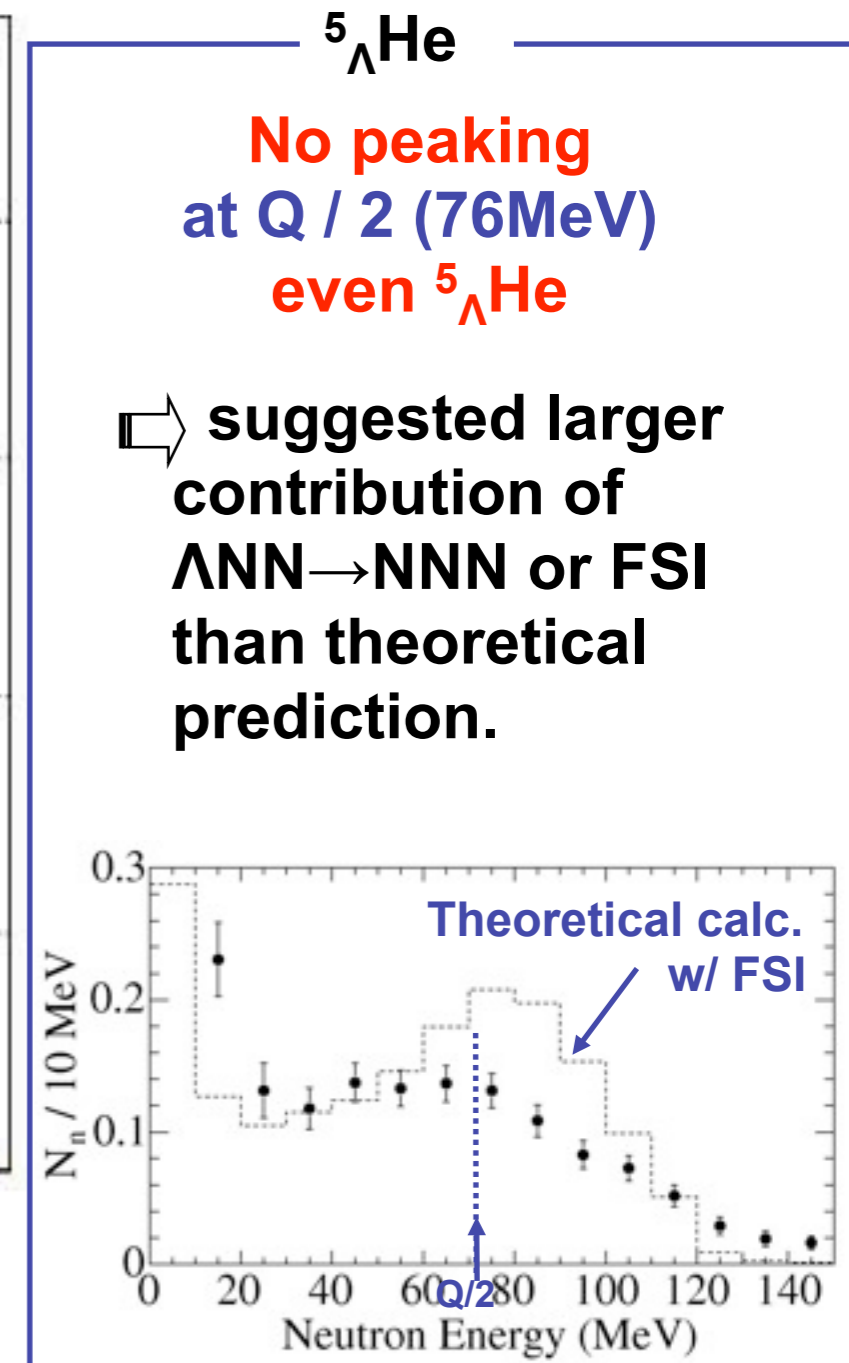
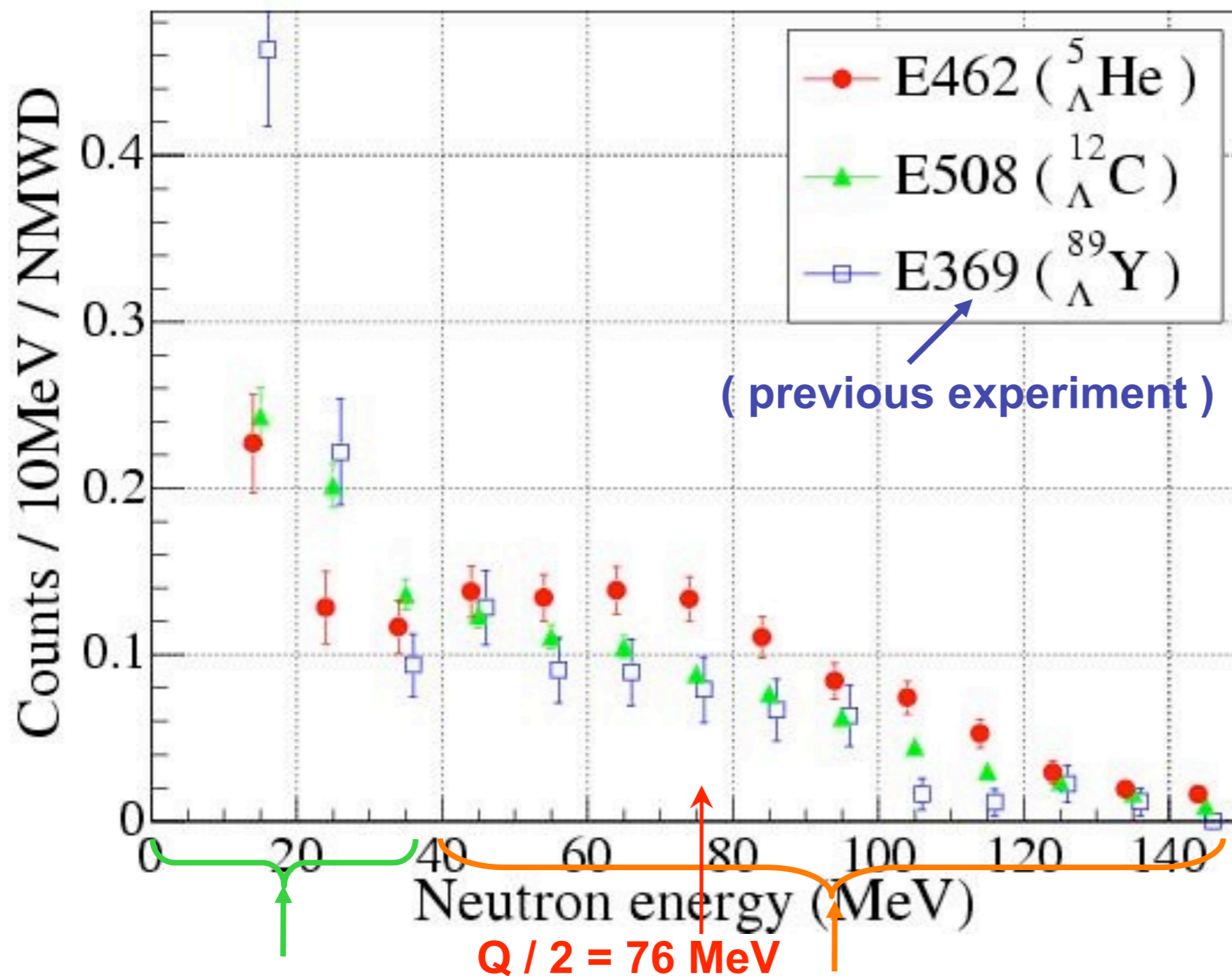
(60 < E < 110 MeV),

$$N_n/N_p({}^{12}_{\Lambda}\text{C}) = 2.00 \pm 0.09(\text{stat}) \pm 0.14(\text{sys})$$

(E > 60 MeV),

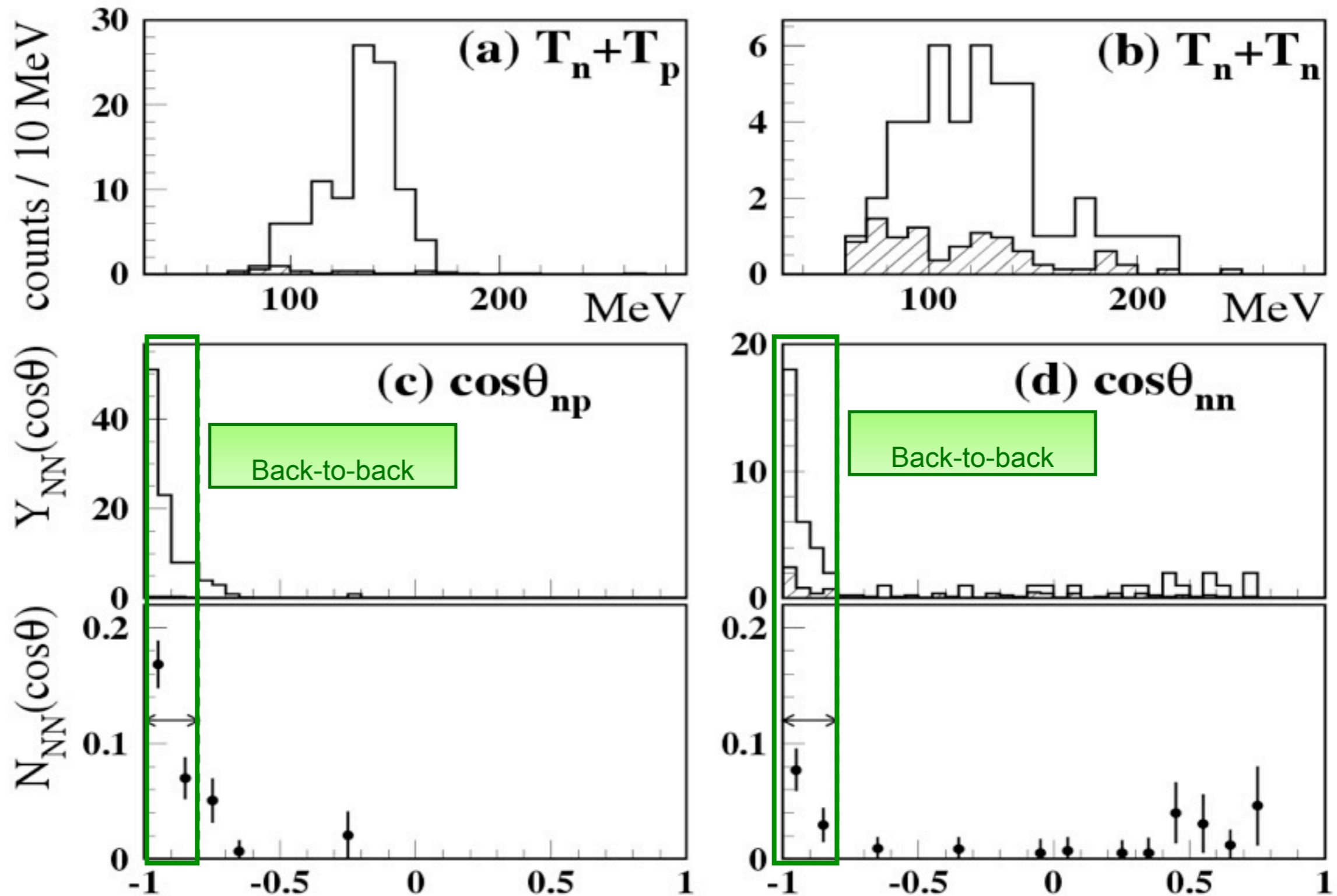
S.Okada *et al.*,
PLB 597 (2004) 249

Mass number dependence of neutron energy spectra ($A=5,12,89$)



As the mass number become larger, the number of neutron become larger in the low energy part, and smaller in the high energy part.

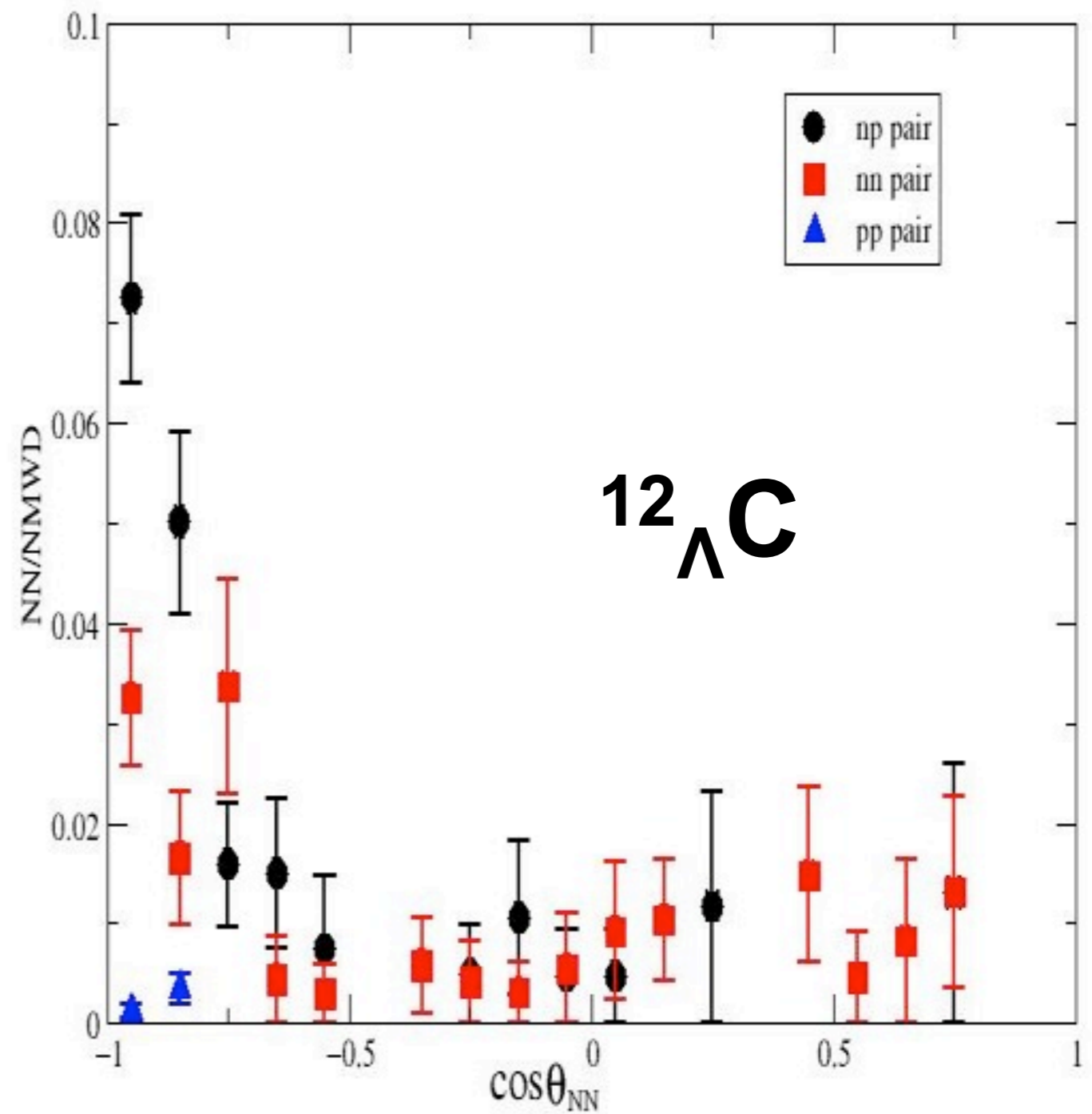
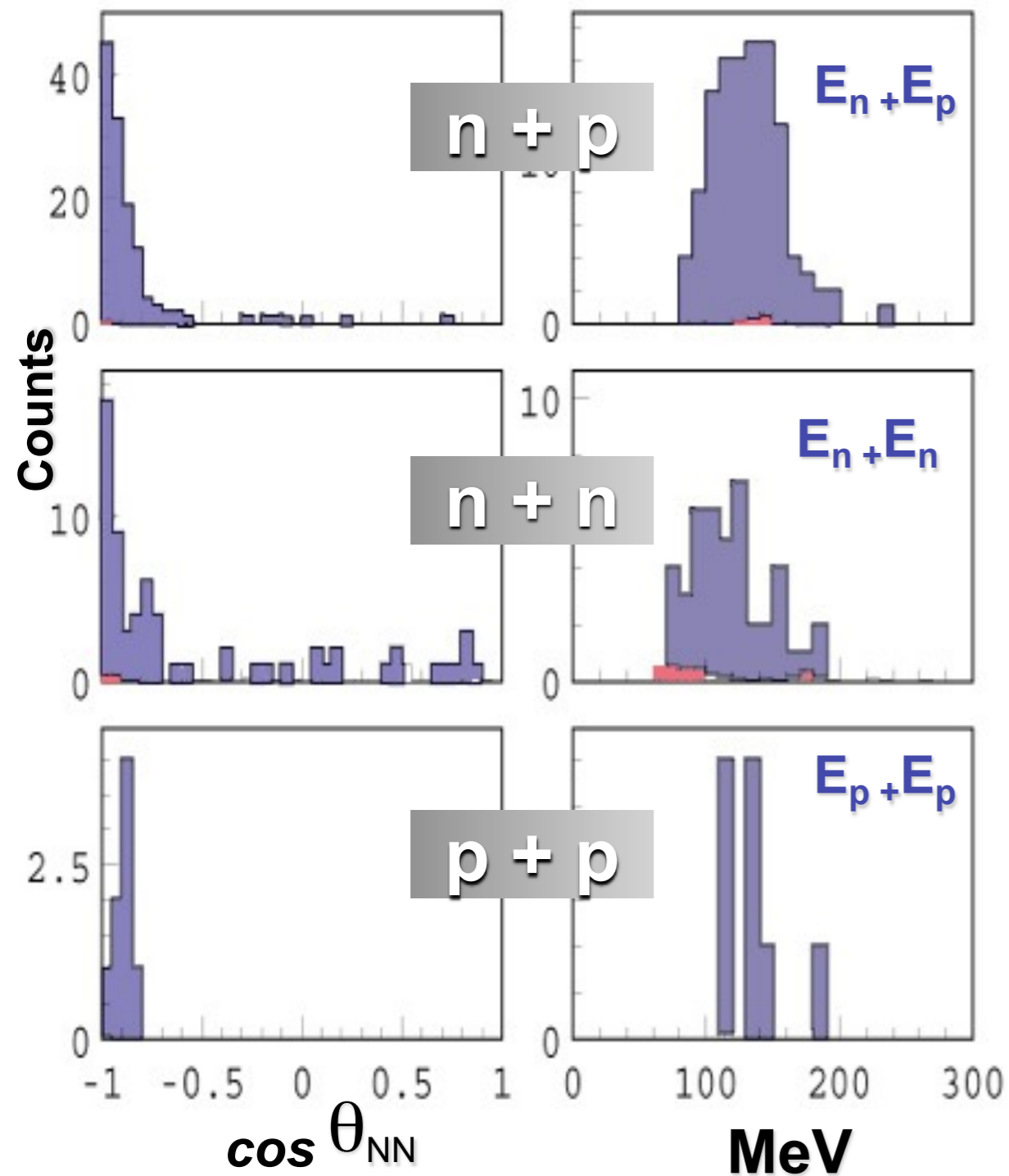
np- & nn- angular distribution ($^5_\Lambda\text{He}$)



$$\Gamma_n / \Gamma_p \sim N_{nn} / N_{np} = 0.45 \pm 0.11 \pm 0.03$$

systematic error is mainly come from efficiency for neutron (6%) + acceptance(3%)

Coincidence Measurement ($A=12$)

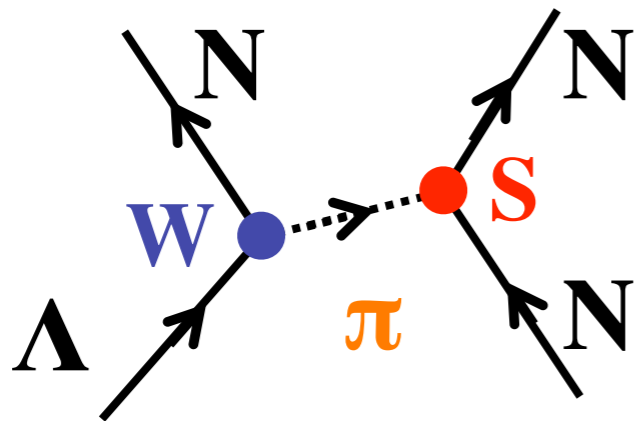


$$\Gamma_n/\Gamma_p \sim N_{nn} / N_{np} = 0.51 \pm 0.13 \pm 0.05$$

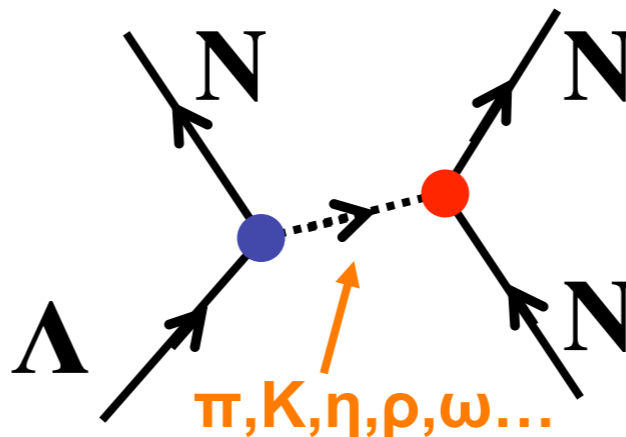
Γ_n / Γ_p ratio

Theo.

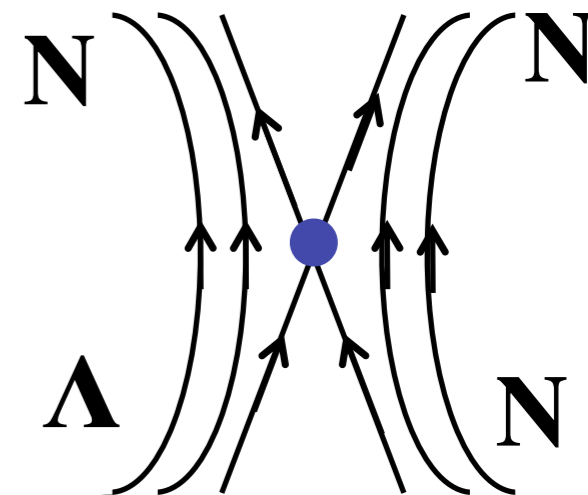
One Pion Exchange (OPE)



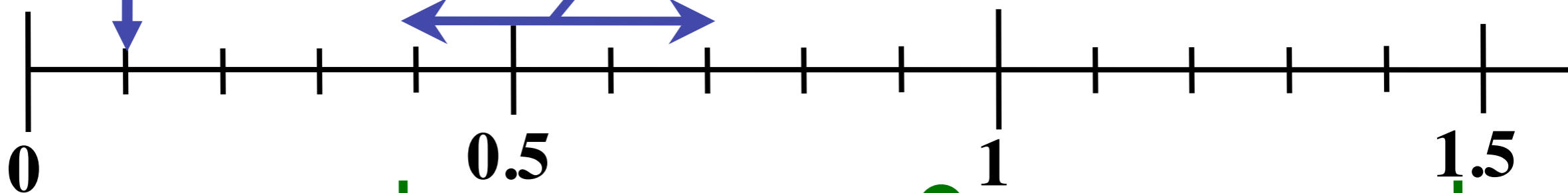
Meson Exchange mechanism



Direct Quark mechanism



Γ_n / Γ_p



Previous exp. (at BNL) 0.93 ± 0.55 (Szymanski et al.) for ${}^5_{\Lambda}\text{He}$

Exp.

${}^5_{\Lambda}\text{He}$ (E462)



$$N_{nn} / N_{np} ({}^5_{\Lambda}\text{He}) = 0.45 \pm 0.11 \pm 0.03$$

Kang et al. PRL 96 (2006) 062301

${}^{12}_{\Lambda}\text{C}$ (E508)



$$\Gamma_n / \Gamma_p ({}^{12}_{\Lambda}\text{C}) = 0.51 \pm 0.13 \pm 0.05$$

Kim et al. PLB641 (2006) 28

偏極と非対 称度

偏極ハイパー核の生成

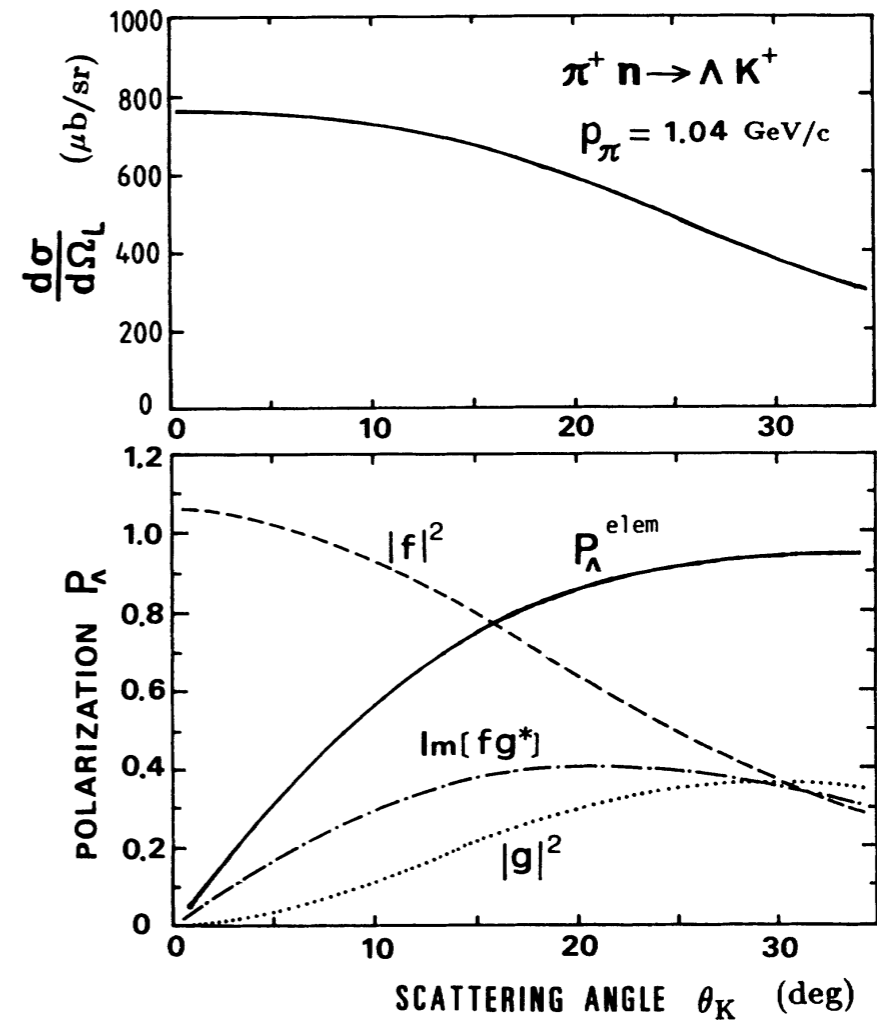
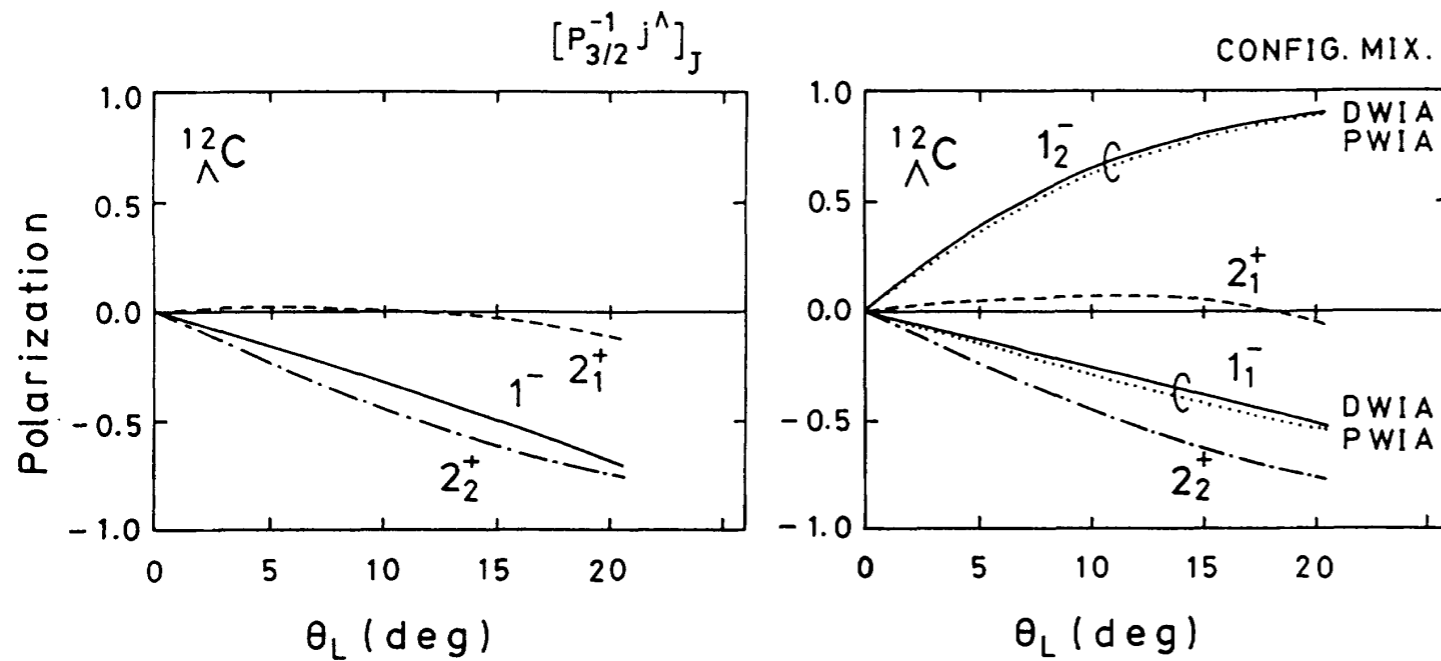


FIG. 8. The spin-nonflip amplitude (f), spin-flip one (g), differential cross section, and polarization calculated as a function of the laboratory scattering angle for $\pi^+ n \rightarrow \Lambda K^+$ at $p_\pi = 1.04$ GeV/c. See Eq. (1) for the definition of the amplitudes and Eq. (11) for the Λ polarization in the free space. The two-body laboratory cross section is given by $d\sigma/d\Omega = C(|f|^2 + |g|^2)$ where C is a proportionality coefficient [7].

Asymmetry measurement of decay proton

Asymmetry : Volume of the asymmetric emission from NMWD

$$N(\theta) = N_0(1 + \underline{A} \cos\theta)$$

Asymmetry

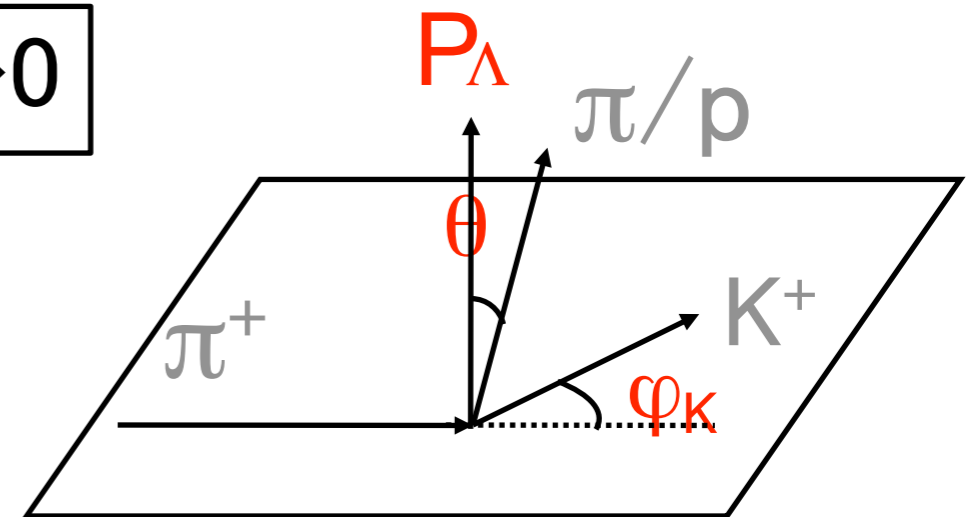
$$= N_0(1 + \alpha \underline{P}_\Lambda \cos\theta)$$

Asymmetry parameter

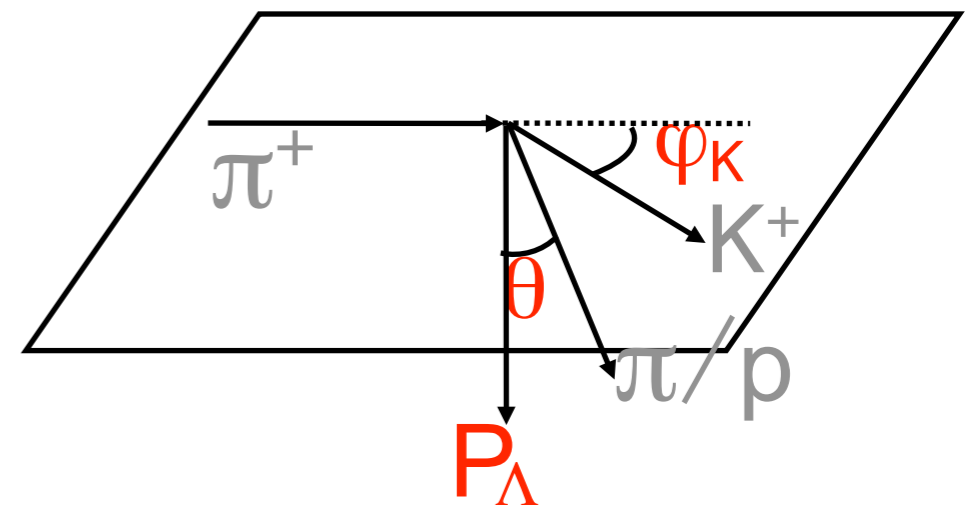
$$A = \frac{(R + 1)}{(R - 1)}, \quad R = \frac{N(\theta^+)}{N(\theta^-)}$$

$$R = \left\{ \frac{N(\theta^+(+\varphi)) \times N(\theta^-(-\varphi))}{N(\theta^+(-\varphi)) \times N(\theta^-(+\varphi))} \right\}^{1/2}$$

$$\varphi_K > 0$$



$$\varphi_K < 0$$



Difference of acceptance & efficiency → canceled out !!

Importance of α_{nm} measurement

If assuming
initial S state

Initial state	Final state	Amplitude	Isospin	Parity
1S_0	1S_0	a	1	No
	3P_0	b	1	Yes
3S_1	3S_1	c	0	No
	3D_1	d	0	No
	1P_1	e	0	Yes
	3P_1	f	1	Yes

$$\alpha_p^{NM} = \frac{\sqrt{3}/2[-ae + b(c - \sqrt{2}d)/\sqrt{3} + (\sqrt{2}c + d)f]}{1/4\{a^2 + b^2 + 3(c^2 + d^2 + e^2 + f^2)\}}$$



We can know the interference between states with different **Isospin** and **Parity**.

$$\Gamma_n / \Gamma_p = \frac{2(a^2 + b^2 + f^2)}{a^2 + b^2 + c^2 + d^2 + e^2 + f^2} \quad (\text{Applying } \Delta I = 1/2 \text{ rule})$$

α_{NM} for ${}^5_{\Lambda}\text{He}$ NMWD

- Polarization of Λ \longrightarrow Estimated from mesonic decay

$$A_{\pi} = \alpha_{\pi} P_{\Lambda} \varepsilon$$

- A_{π} : Asymmetry of Pion
- α_{π} : Asymmetry Parameter of Pion
($= -0.642 \pm 0.013$)
- P_{Λ} : Polarization of Lambda
- ε : Attenuation factor

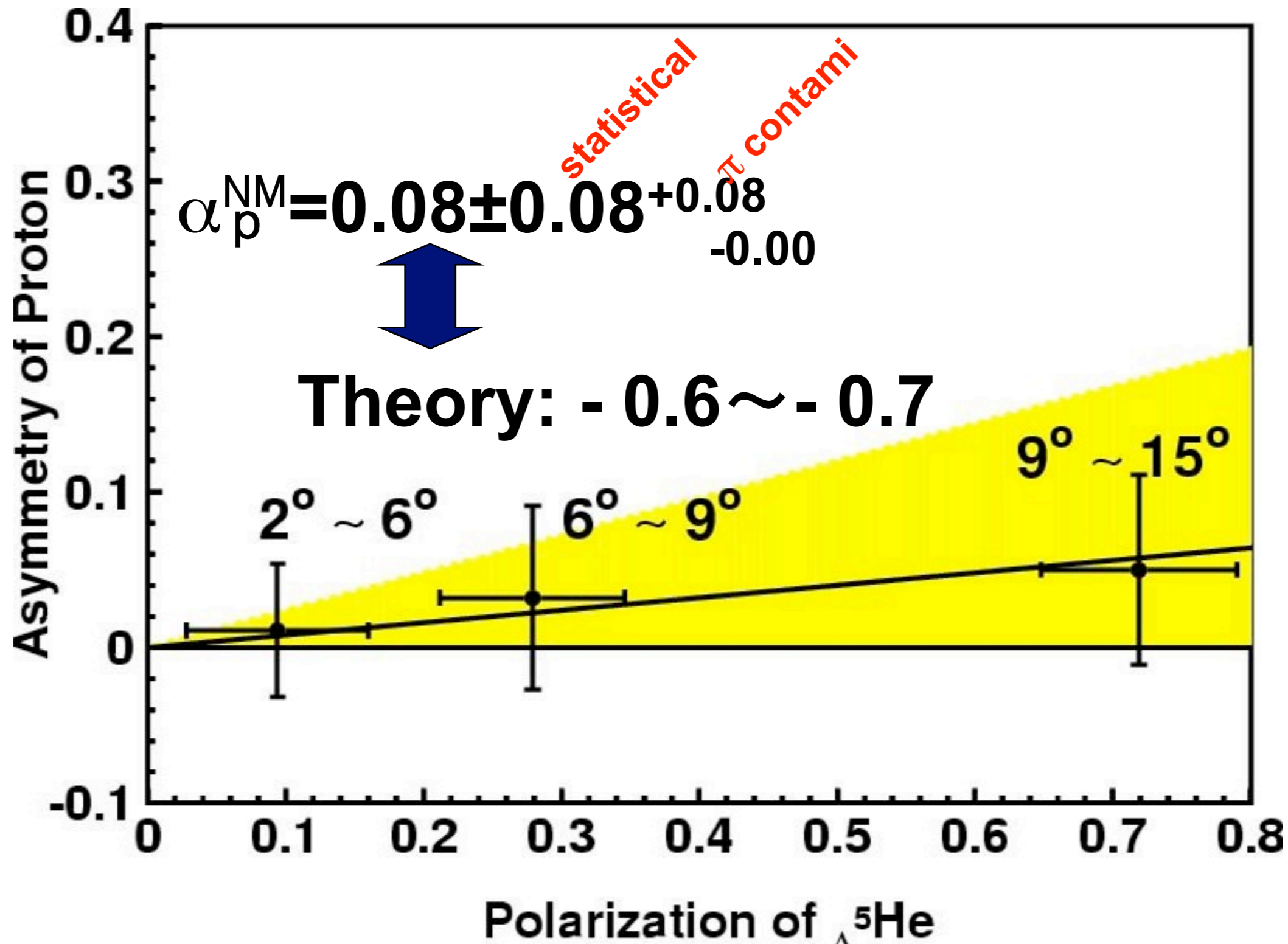
- Asymmetry Parameter of Proton

$$A_{\text{p}} = \alpha_{\text{p}}^{\text{NM}} P_{\Lambda} \varepsilon$$

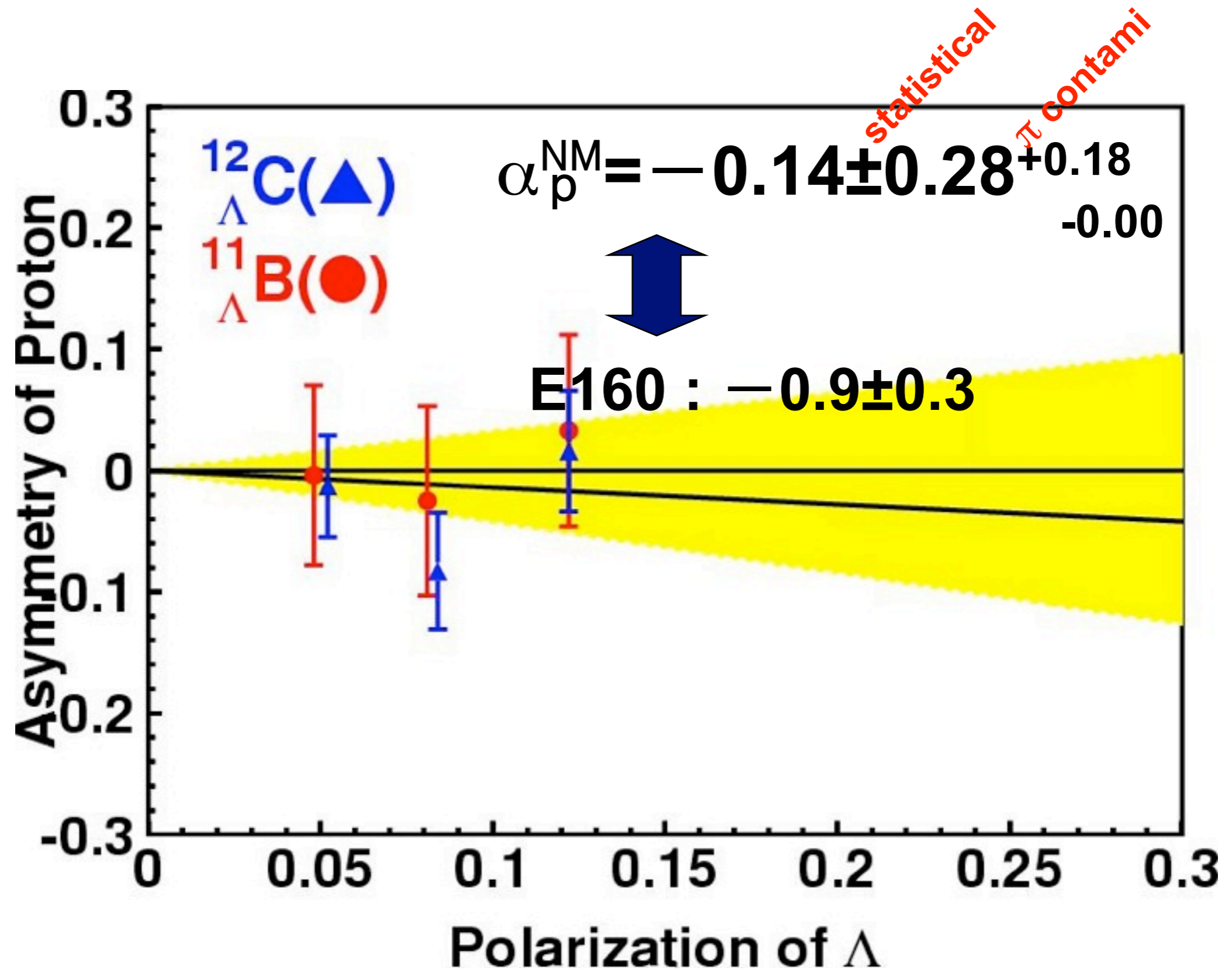
We can calculate $\alpha_{\text{p}}^{\text{NM}}$ without theoretical help !

Asymmetry parameter of ${}^5_{\Lambda}\text{He}$

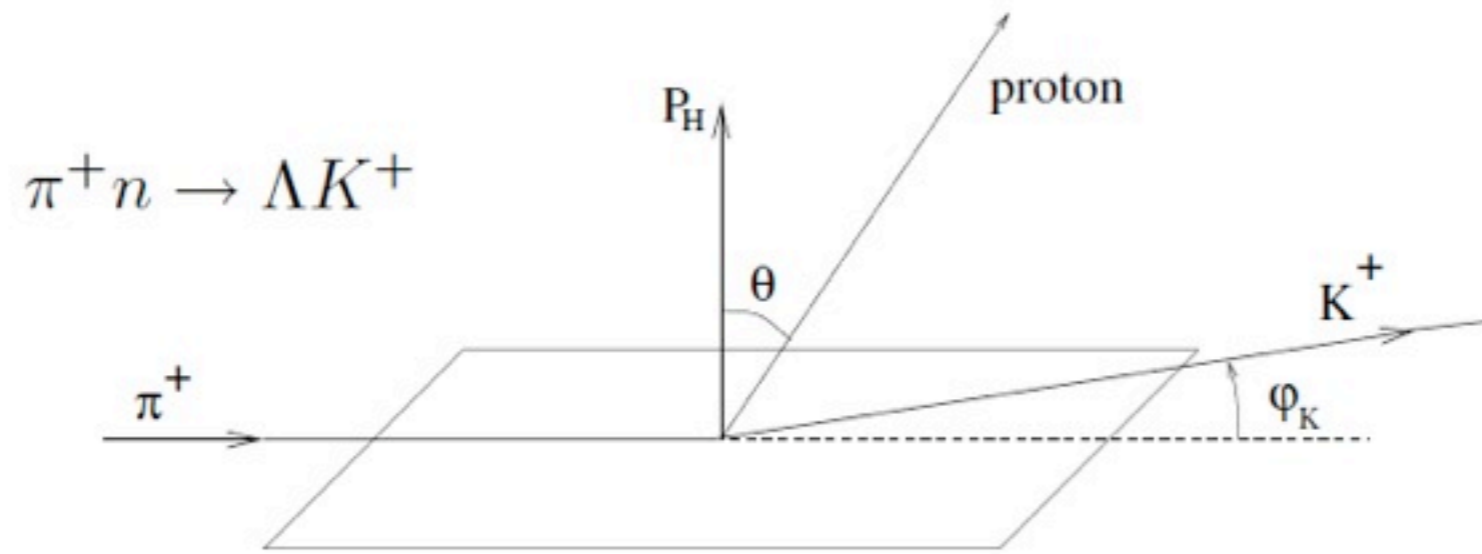
Nucl.Phys.A754 (2005) 168c
nucl-ex/050916



Asymmetry parameter of ${}_{\Lambda}^{12}\text{C}$, ${}_{\Lambda}^{11}\text{B}$



POLARIZED HYPERNUCLEI: THE DECAY ASYMMETRY



◆ Weak decay proton intensity from $\vec{\Lambda}p \rightarrow np$: $I(\theta) = I_0 [1 + p_\Lambda a_\Lambda \cos \theta]$

$p_\Lambda = \Lambda$ polarization

$a_\Lambda =$ intrinsic Λ asymmetry parameter

$a_\Lambda \iff$ interference among PC and PV $\vec{\Lambda}p \rightarrow np$ channels

\implies information on strengths and relative phases of the decay amplitudes

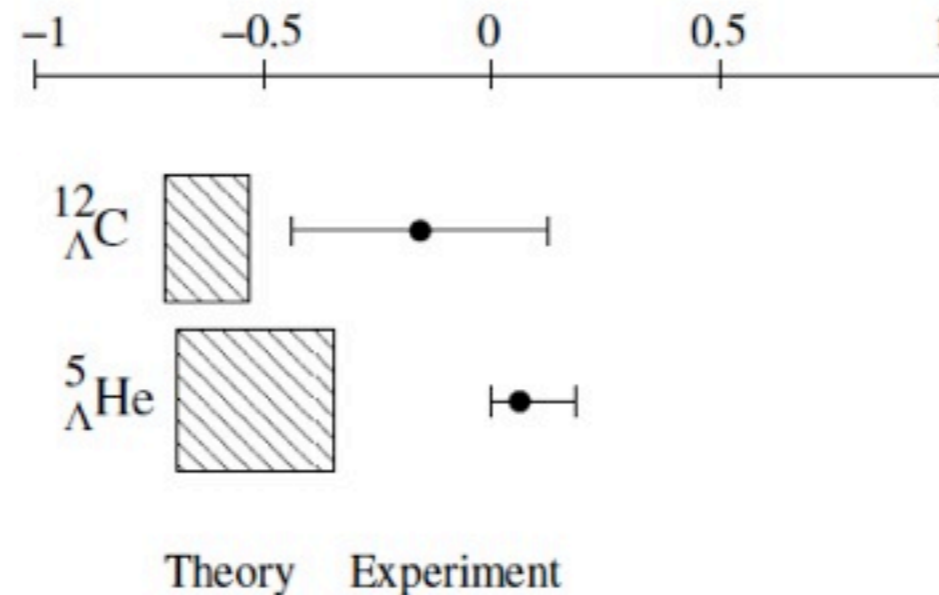
◆ Nucleon FSI modify the weak decay proton intensity $I(\theta)$

Experimentally one measures $I^M(\theta) = I_0^M [1 + p_\Lambda a_\Lambda^M \cos \theta]$

\implies observable Λ asymmetry parameter $a_\Lambda^M = \frac{1}{p_\Lambda} \frac{I^M(0^\circ) - I^M(180^\circ)}{I^M(0^\circ) + I^M(180^\circ)}$

		${}^5_{\Lambda}\text{He}$	${}^{12}_{\Lambda}\text{C}$
Sasaki et al.	a_{Λ}		
$\pi + K + \text{DQ}$		-0.68	
Parreño et al.			
$\pi + \rho + K + K^* + \omega + \eta$		-0.68	-0.73
Itonaga et al.			
$\pi + K + \omega + 2\pi/\rho + 2\pi/\sigma$		-0.33	
Barbero et al.			
$\pi + \rho + K + K^* + \omega + \eta$		-0.54	-0.53
KEK-E508	a_{Λ}^M		$-0.16 \pm 0.28^{+0.18}_{-0.00}$
KEK-E462		$+0.07 \pm 0.08^{+0.08}_{-0.00}$	

KEK-E508/E462: T. Maruta et al., EPJA 33, 255 (2007)



FSI prevent establishing direct comparisons between a_{Λ} and a_{Λ}^M
 \implies a theoretical evaluation of a_{Λ}^M is required

OME + Nucleon FSI

[W. M. Alberico, G.G., A. Parreño and A. Ramos, PRL 94, 082501 (2005)]

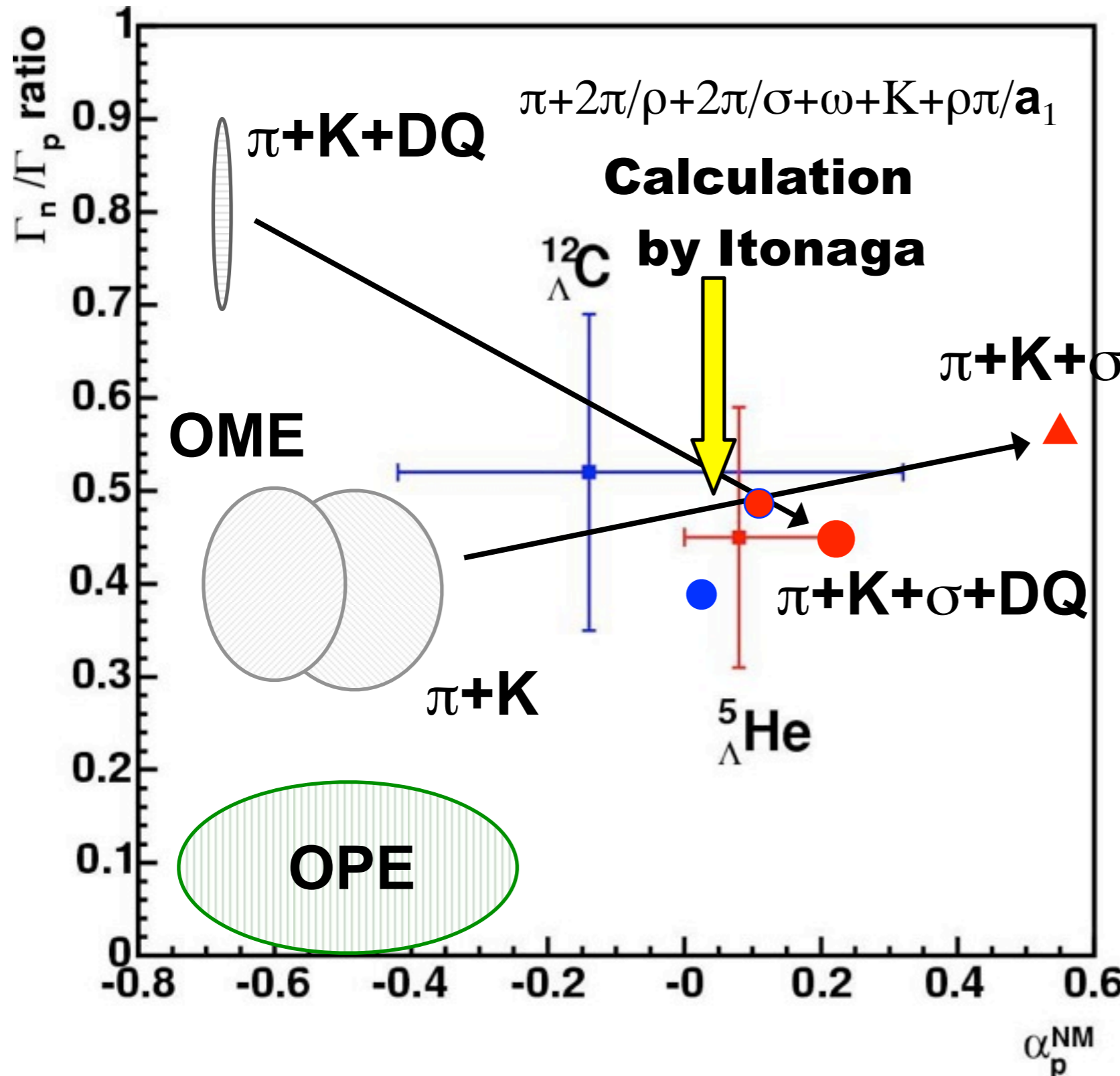
$$\text{OME} = \pi + \rho + K + K^* + \eta + \omega$$

$$I(\theta) = I_0 [1 + p_\Lambda a_\Lambda \cos \theta] \quad I^M(\theta) = I_0^M [1 + p_\Lambda a_\Lambda^M \cos \theta]$$

	${}^5_\Lambda\text{He}$	${}^{11}_\Lambda\text{B}$	${}^{12}_\Lambda\text{C}$
a_Λ	-0.68	-0.81	-0.73
$a_\Lambda^M (T_p \geq 30 \text{ MeV})$	-0.46	-0.39	-0.37
$a_\Lambda^M (T_p \geq 50 \text{ MeV})$	-0.52	-0.55	-0.51
$a_\Lambda^M (T_p \geq 70 \text{ MeV})$	-0.55	-0.70	-0.65
KEK-E462	$0.07 \pm 0.08^{+0.08}_{-0.00}$		
KEK-E508	$-0.16 \pm 0.28^{+0.18}_{-0.00}$		

Data from [T. Maruta et al., EPJA 33, 255 (2007)]

Comparison with recent calculations



$\pi+K, OME$ can reproduce Γ_n/Γ_p ratio but predict large negative α^{NM}

Γ_n/Γ_p and α^{NM} can be reproduced by $\pi+K+\sigma+DQ$ model

Sasaki *et al.*

PRC71 (2005)035502

- (1) Large $b(^1S_0 \rightarrow ^3P_0)$ and $f(^3S_0 \rightarrow ^3P_1)$ amplitude
- (2) Violation of $\Delta I=1/2$ rule considered

$$\frac{\sqrt{3}/2[-ae + b(c - \sqrt{2}d)/\sqrt{3} + (\sqrt{2}c + d)f]}{1/4\{a^2 + b^2 + 3(c^2 + d^2 + e^2 + f^2)\}}$$

◆ Effective Field Theory: $\pi + K +$ Leading-Order Contact Interactions

[A. Parreño, C. Bennhold and B. R. Holstein, PRC 70, 051601 (2004)]

- LOCI coefficients fixed to reproduce experimental Γ_{NM} and Γ_n/Γ_p for ${}^5_{\Lambda}\text{He}$, ${}^{11}_{\Lambda}\text{B}$ and ${}^{12}_{\Lambda}\text{C}$ and $a_{\Lambda}({}^5_{\Lambda}\text{He})$
- Predicted a dominating central, spin- and isospin-independent contact term

◆ $\pi + K + \sigma +$ Direct Quark

[K. Sasaki, M. Izaki, M. Oka, PRC 71, 035502 (2005)]

- Decay data for s -shell hypernuclei fitted to obtain the weak couplings of the scalar-isoscalar σ -meson, $\mathcal{H}_{\Lambda\sigma N}^{\text{W}} = g_{\text{W}} \bar{\psi}_N (A_{\sigma} + B_{\sigma} \gamma_5) \phi_{\sigma} \psi_{\Lambda}$
- All ${}^5_{\Lambda}\text{He}$ decay observables reasonably reproduced. No calculation for ${}^{12}_{\Lambda}\text{C}$

◆ OME + σ , OME = $\pi + \rho + K + K^* + \eta + \omega$

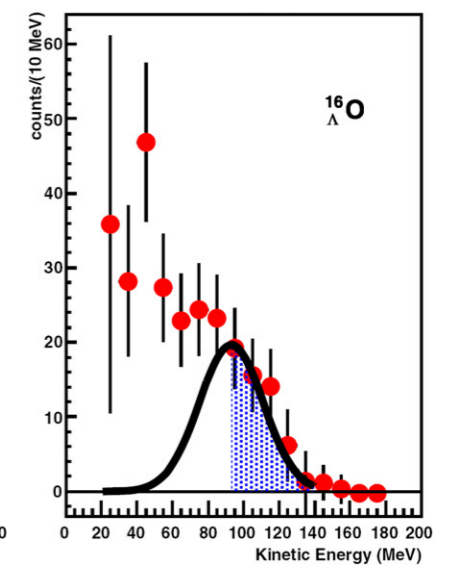
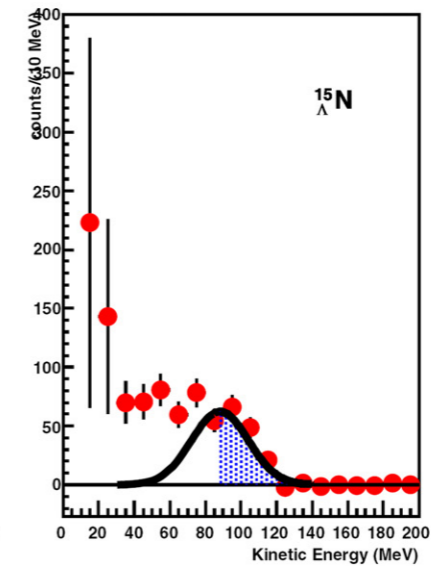
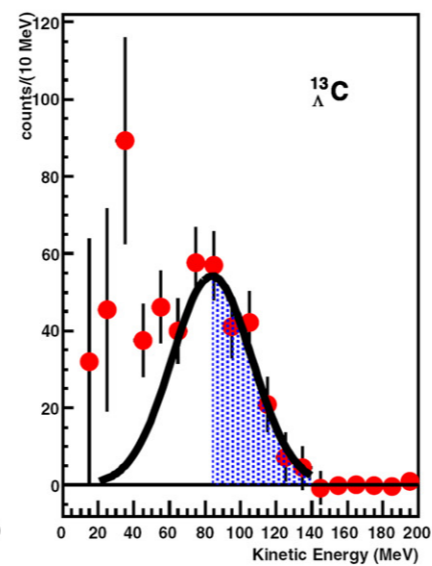
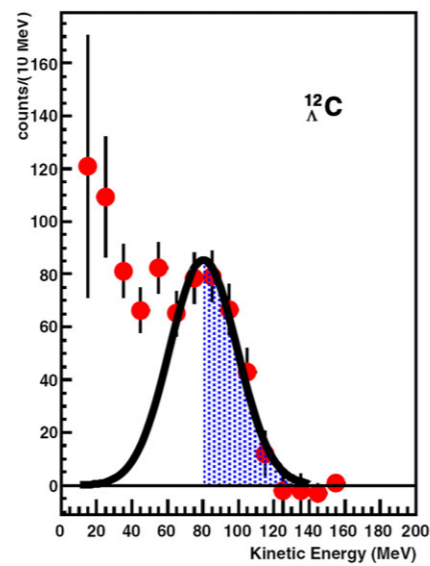
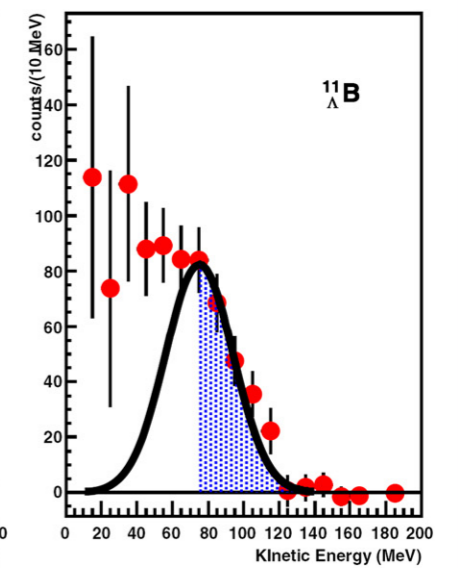
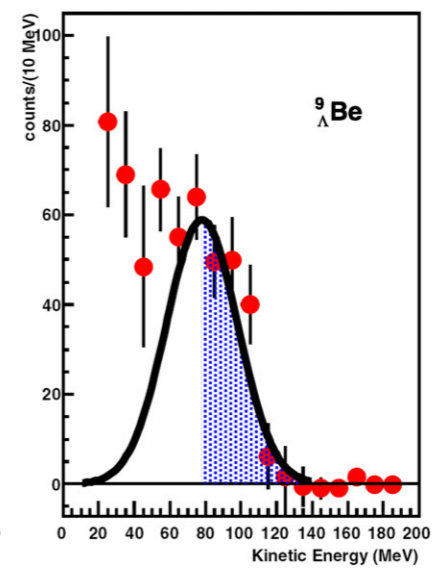
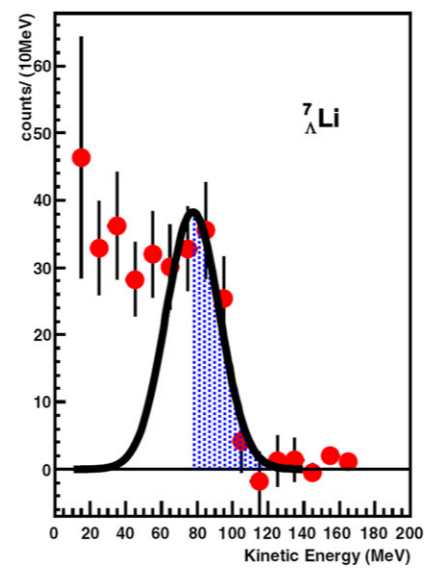
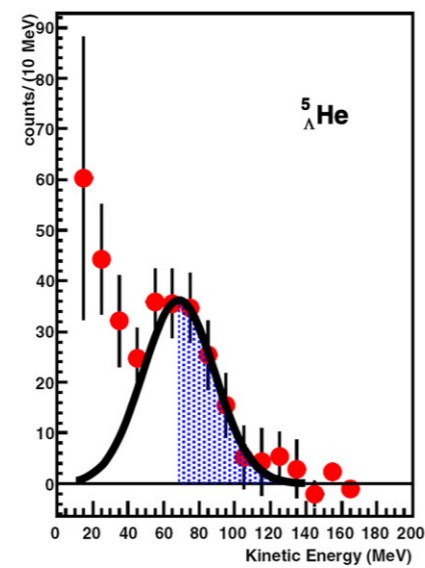
[C. Barbero and A. Mariano, PRC 73, 024309 (2006)]

- Unknown σ couplings fixed to reproduce measured $\Gamma_{\text{NM}}({}^5_{\Lambda}\text{He})$ and $\Gamma_n/\Gamma_p({}^5_{\Lambda}\text{He})$
- Improved overall agreement with experiment for ${}^{12}_{\Lambda}\text{C}$ and ${}^5_{\Lambda}\text{He}$ but data for $a_{\Lambda}({}^5_{\Lambda}\text{He})$ could not be reproduced

◆ \Rightarrow Importance of the Scalar-Isoscalar channel in Asymmetry calculations

Γ_{2N} ?

► FINUDA



$$R(A) = \frac{0.5 + \frac{\Gamma_2}{\Gamma_p}}{1 + \frac{\Gamma_2}{\Gamma_p}} + bA.$$

$$\frac{\Gamma_2}{\Gamma_{\text{NMWD}}} = \frac{\Gamma_2/\Gamma_p}{(\Gamma_n/\Gamma_p) + 1 + (\Gamma_2/\Gamma_p)}.$$

$$\frac{\Gamma_2}{\Gamma_{\text{NMWD}}} = 0.24 \pm 0.10.$$

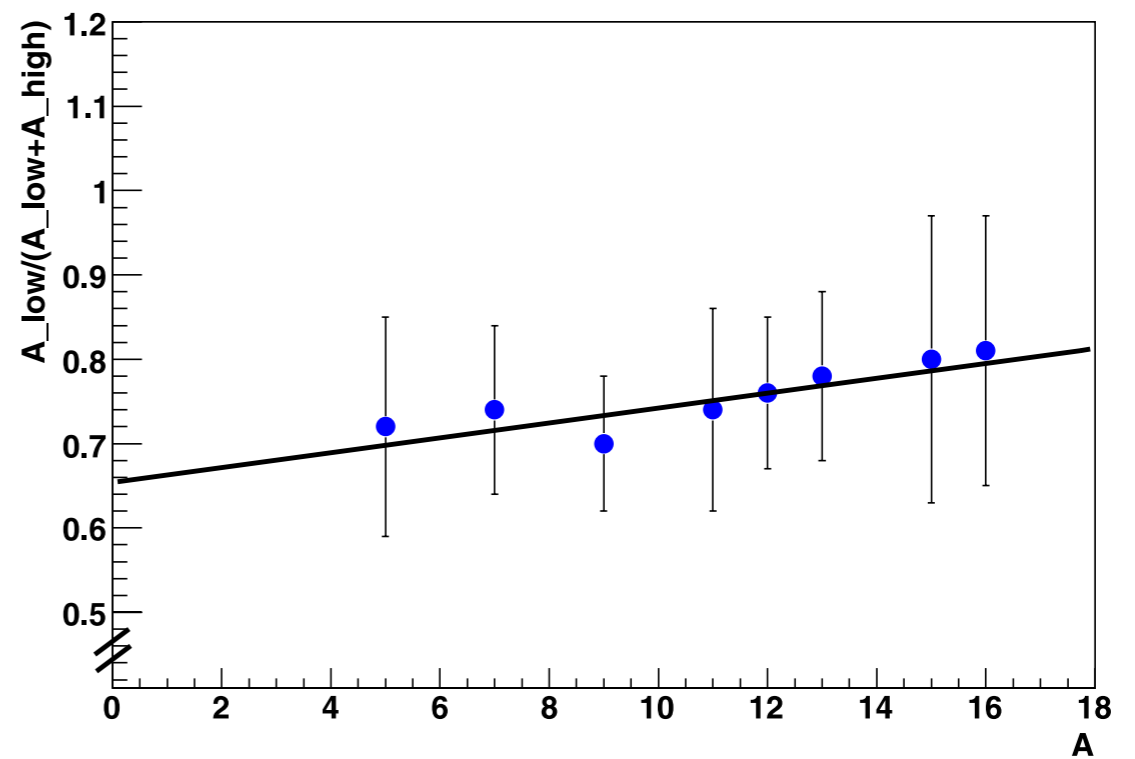


Fig. 2. The ratio $A_{\text{low}}/(A_{\text{low}} + A_{\text{high}})$ as a function of the hypernuclear mass number.

► KEK E502: PRL 103(2009) 182502.

► $\Gamma_{2N}/\Gamma_{NMWD}=0.29\pm 0.13$

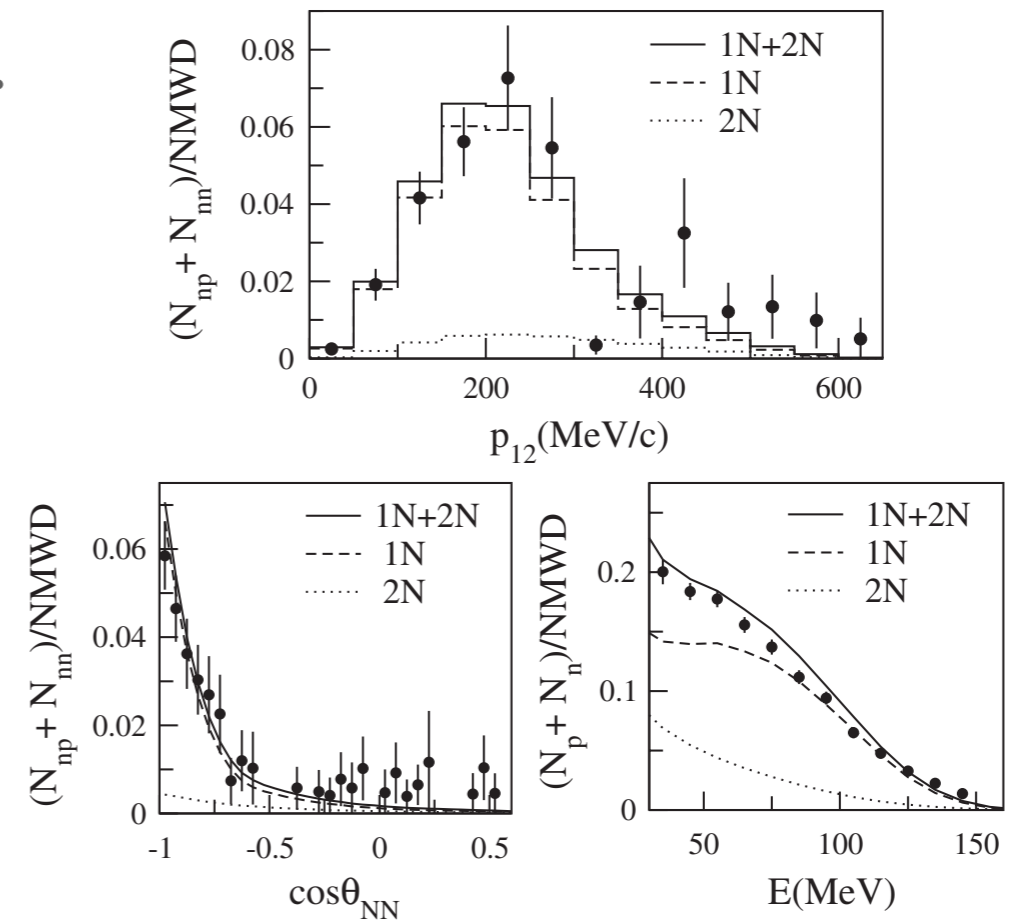


FIG. 4. The momentum sum (upper) and the angular (lower left) correlation of the pair sum $N_{np} + N_{nn}$ and the normalized nucleon yields $N_N(E)$ are compared with those of INC(1N + 2N) (solid lines) with $b_{2N} = 0.29$. The decomposed 1N- (dashed lines) and 2N-NMWD (dotted lines) contribution also are shown.

$\Delta I = 1/2$ 則の
検証

s -shell Hypernuclei $\iff \Delta I = 1/2$ Rule

- ◆ Block-Dalitz Phenomenological Model \implies Spin-Isospin structure of $\Lambda N \rightarrow nN$
- ◆ Introducing the rates R_{NJ} for the spin-singlet (R_{n0}, R_{p0}) and spin-triplet (R_{n1}, R_{p1}) elementary $\Lambda N \rightarrow nN$ interactions:

$$\Gamma_{\text{NM}}({}_{\Lambda}^3\text{H}) = (3R_{n0} + R_{n1} + 3R_{p0} + R_{p1}) \frac{\rho_2}{8}$$

$$\Gamma_{\text{NM}}({}_{\Lambda}^4\text{H}) = (R_{n0} + 3R_{n1} + 2R_{p0}) \frac{\rho_3}{6}$$

$$\Gamma_{\text{NM}}({}_{\Lambda}^4\text{He}) = (2R_{n0} + R_{p0} + 3R_{p1}) \frac{\rho_3}{6}$$

$$\Gamma_{\text{NM}}({}_{\Lambda}^5\text{He}) = (R_{n0} + 3R_{n1} + R_{p0} + 3R_{p1}) \frac{\rho_4}{8}$$

- ◆ Relations which test the $\Delta I = 1/2$ Rule

$$\frac{\Gamma_n({}_{\Lambda}^4\text{He})}{\Gamma_p({}_{\Lambda}^4\text{H})} = \frac{\frac{\Gamma_n({}_{\Lambda}^4\text{H})}{\Gamma_p({}_{\Lambda}^4\text{H})} \frac{\Gamma_n({}_{\Lambda}^4\text{He})}{\Gamma_p({}_{\Lambda}^4\text{He})}}{\frac{\Gamma_n({}_{\Lambda}^5\text{He})}{\Gamma_p({}_{\Lambda}^5\text{He})}} = \frac{R_{n0}}{R_{p0}} \iff \Delta I = 1/2 \text{ Rule: } \frac{R_{n1}}{R_{p1}} \leq \frac{R_{n0}}{R_{p0}} = 2$$

TABLE XI. – *Experimental data for the non-mesonic weak decay of s-shell hypernuclei.*

	$\Gamma_n/\Gamma_\Lambda^{\text{free}}$	$\Gamma_p/\Gamma_\Lambda^{\text{free}}$	$\Gamma_{\text{NM}}/\Gamma_\Lambda^{\text{free}}$	Γ_n/Γ_p	Ref.
${}^4_\Lambda\text{H}$			0.22 ± 0.09		reference value
			0.17 ± 0.11		KEK [11]
			0.29 ± 0.14		[73]
${}^4_\Lambda\text{He}$	0.04 ± 0.02	0.16 ± 0.02	0.20 ± 0.03	0.25 ± 0.13	BNL [74]
${}^5_\Lambda\text{He}$	0.20 ± 0.11	0.21 ± 0.07	0.41 ± 0.14	0.93 ± 0.55	BNL [37]

► $\Delta I = 1/2$

$$R_n(^1S_0) = 2R_p(^1S_0), \quad R_n(^3P_0) = 2R_p(^3P_0), \quad R_n(^3P_1) = 2R_p(^3P_1).$$

$$\frac{R_{n1}}{R_{p1}} \leq \frac{R_{n0}}{R_{p0}} = 2.$$

$$\frac{R_{n0}}{R_{p0}} = \frac{4r^2 - 4r + 1}{2r^2 + 4r + 2}$$

$$r = \frac{\langle I_f = 1 || A_{1/2} || I_i = 1/2 \rangle}{\langle I_f = 1 || A_{3/2} || I_i = 1/2 \rangle}$$

To J-PARC

Non-mesonic weak decay of ${}^4_{\Lambda}\text{He}$ and ${}^4_{\Lambda}\text{H}$

see S.Ajimura : J-PARC LOI 21

Spin / isospin dependence

$$\Gamma_{\text{nm}}({}^4_{\Lambda}\text{H}) = (3R_{n1} + R_{n0} + 2R_{p0}) \times \rho_4 / 6$$

$$\Gamma_{\text{nm}}({}^4_{\Lambda}\text{He}) = (2R_{n0} + 3R_{p1} + R_{p0}) \times \rho_4 / 6$$

$$\Gamma_{\text{nm}}({}^5_{\Lambda}\text{He}) = (3R_{n1} + R_{n0} + 3R_{p1} + R_{p0}) \times \rho_5 / 8$$

$R_{NS} \dots N : \Lambda n \rightarrow nn, \Lambda p \rightarrow np$
 $S : \text{spin} = 0 \text{ or } 1$

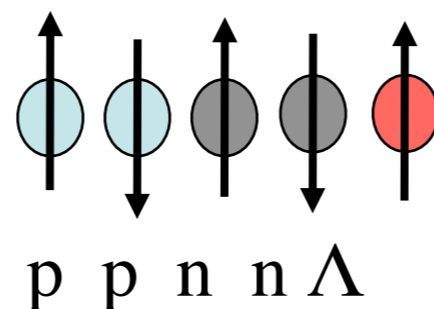
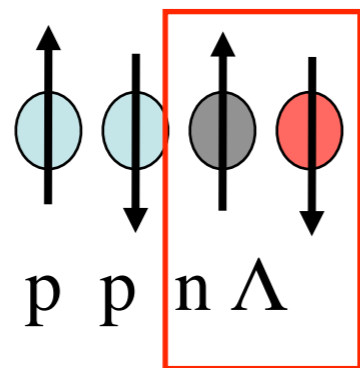
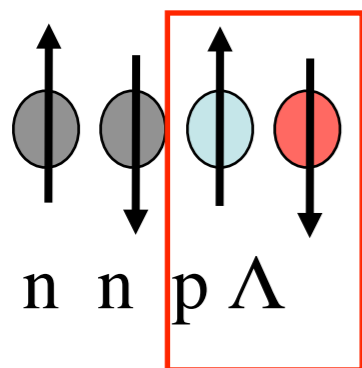
${}^4\text{He} (\text{K}^-, \pi^-) {}^4_{\Lambda}\text{He}$ or
 ${}^4\text{He} (\pi^+, \text{K}^+) {}^4_{\Lambda}\text{He}$

\rightarrow **n+n back-to-back**

${}^4_{\Lambda}\text{H}$

${}^4_{\Lambda}\text{He}$

${}^5_{\Lambda}\text{He}$



${}^4\text{He} (\text{K}^-, \pi^0) {}^4_{\Lambda}\text{H}$

\rightarrow **p+n back-to-back**
 (π^0 spectrometer)

\rightarrow *Need one-order higher statistics.* \rightarrow **J-PARC**



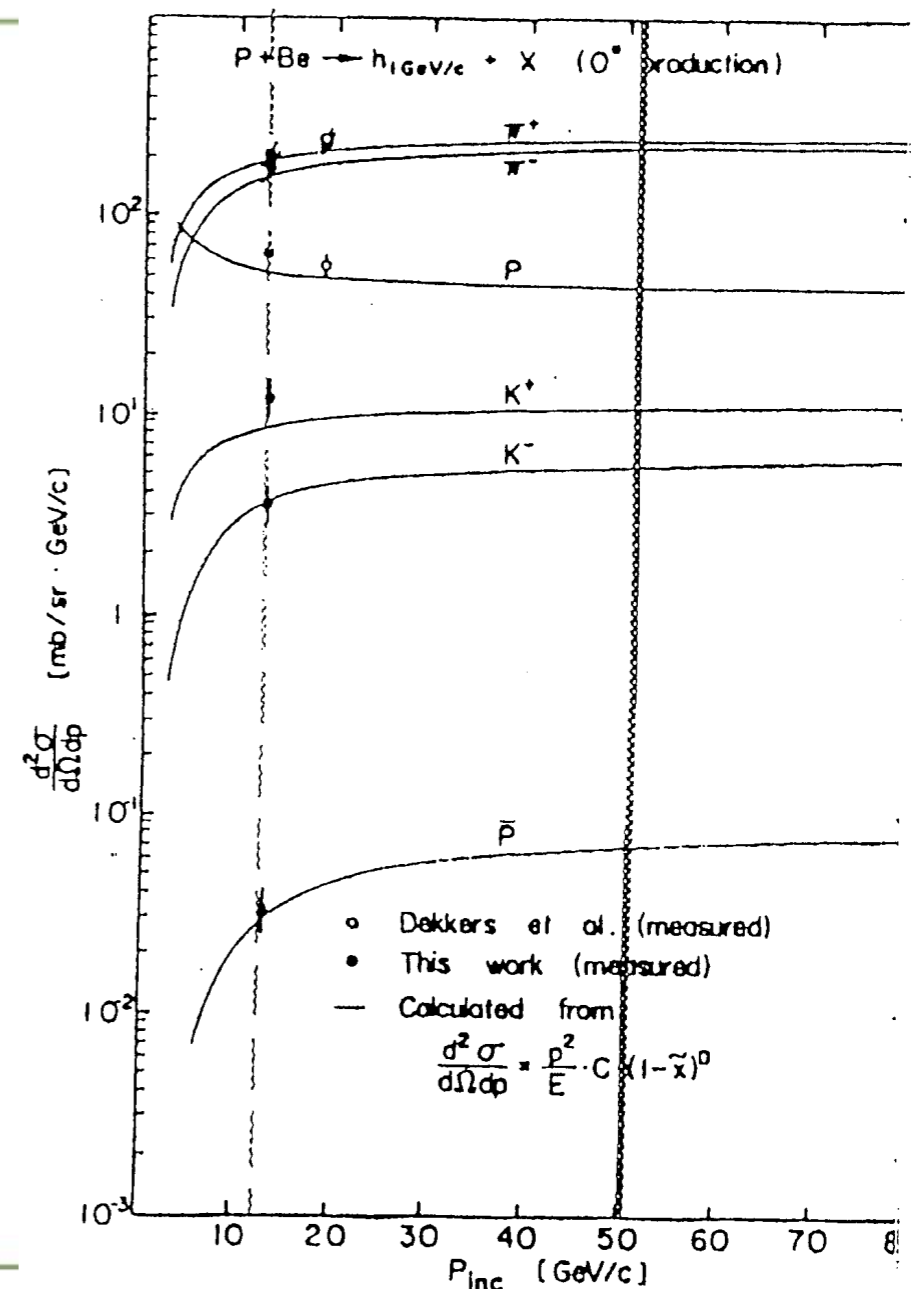
Third day in UT



Production of Secondary Meson Beams

- ▶ $p+A \rightarrow \pi, K, + X$ at forward angles
 - ▶ $E_{cm} = (m_1^2 + m_2^2 + 2E_1^{lab} m_2)^{1/2}$
 $\sim (2E_1^{lab} m_2)^{1/2}$
 - ▶ $\pi^+ > \pi^-$ ← charge conservation
 - ▶ $K^+ > K^-$ ← threshold difference
 - ▶ $\pi > K \gg$ anti-p

$s\bar{s}$: $K^+ \Lambda (500+175)$, $K^- K^+ (500+500)$



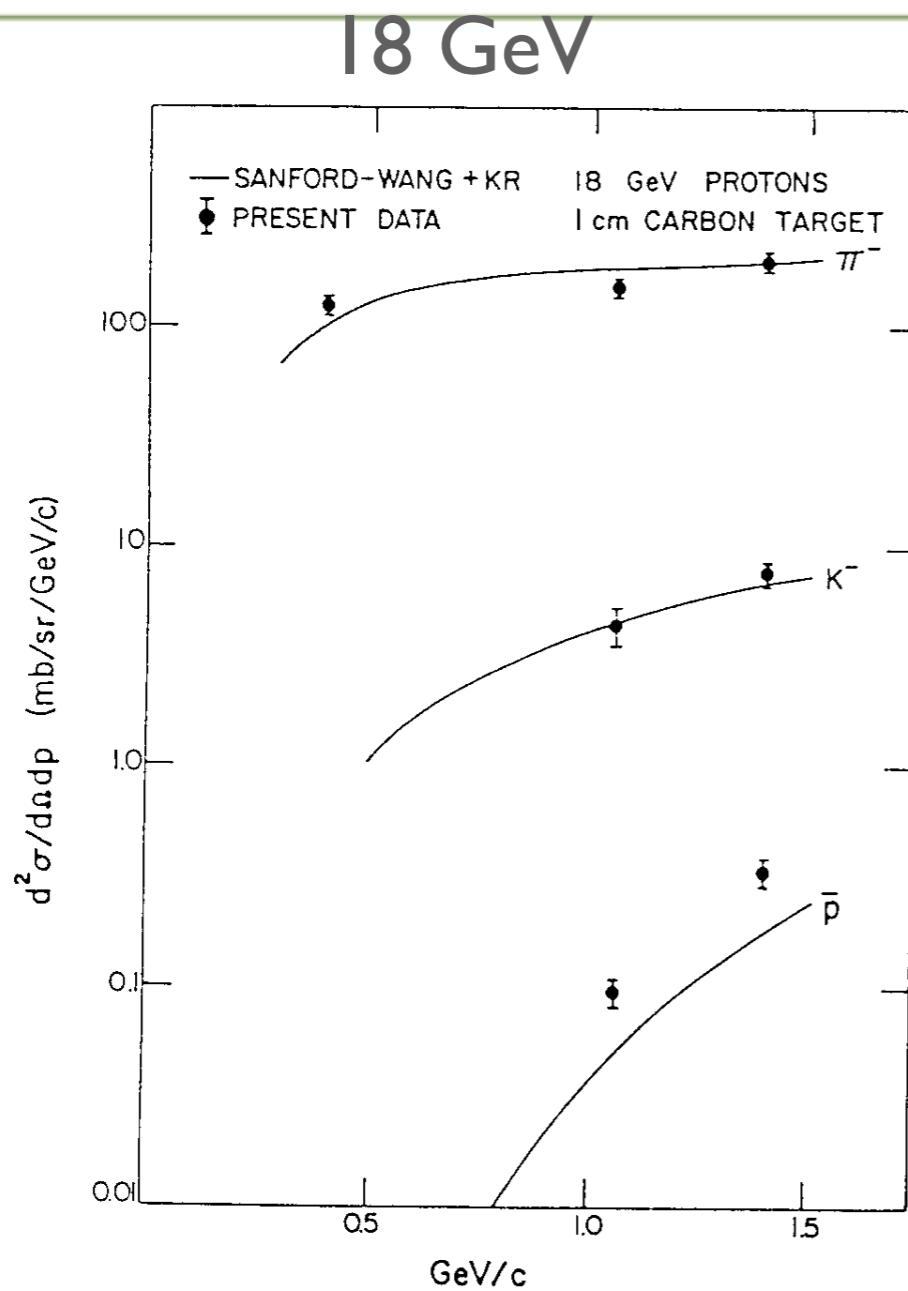
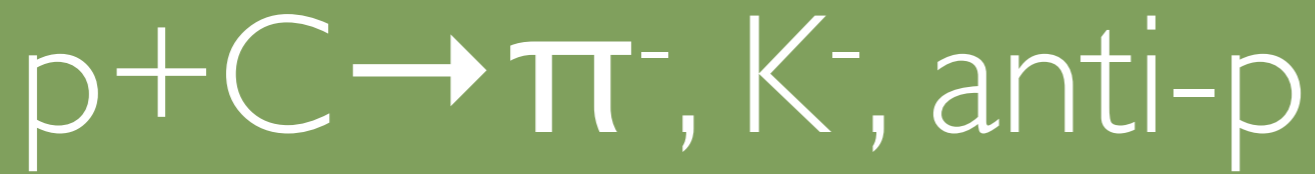


Fig. 5. 18-GeV production cross sections on 1-cm carbon target.

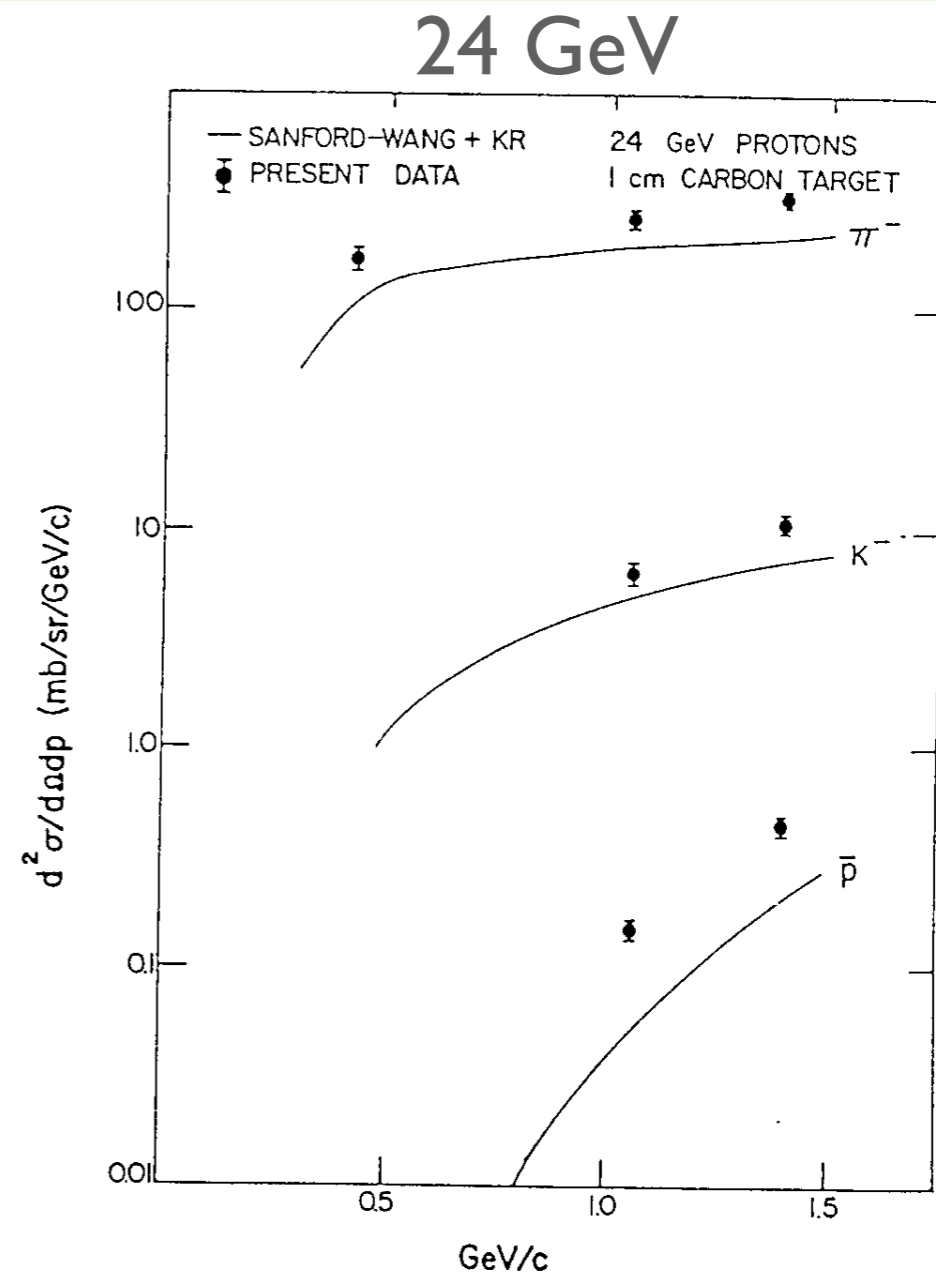
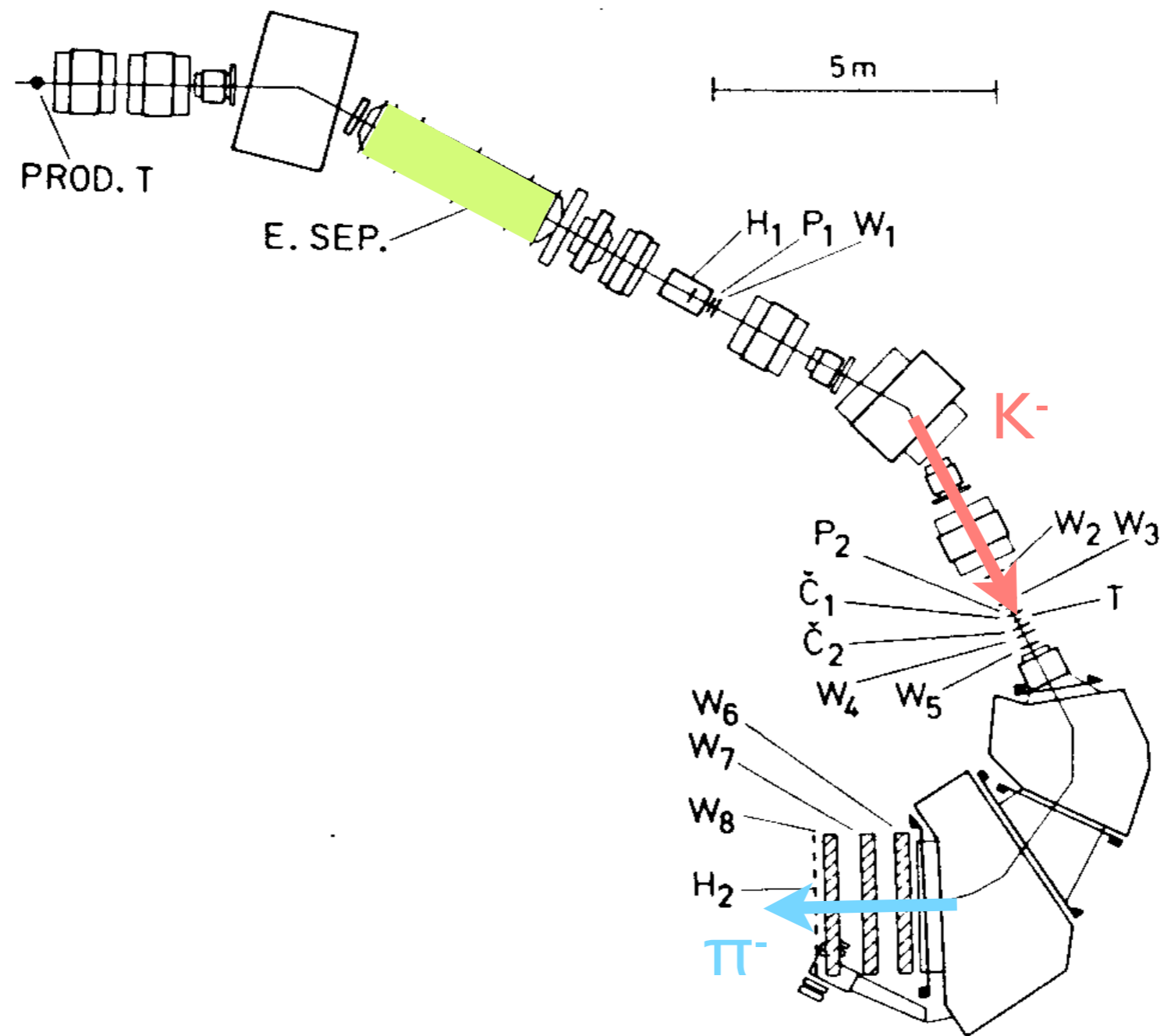
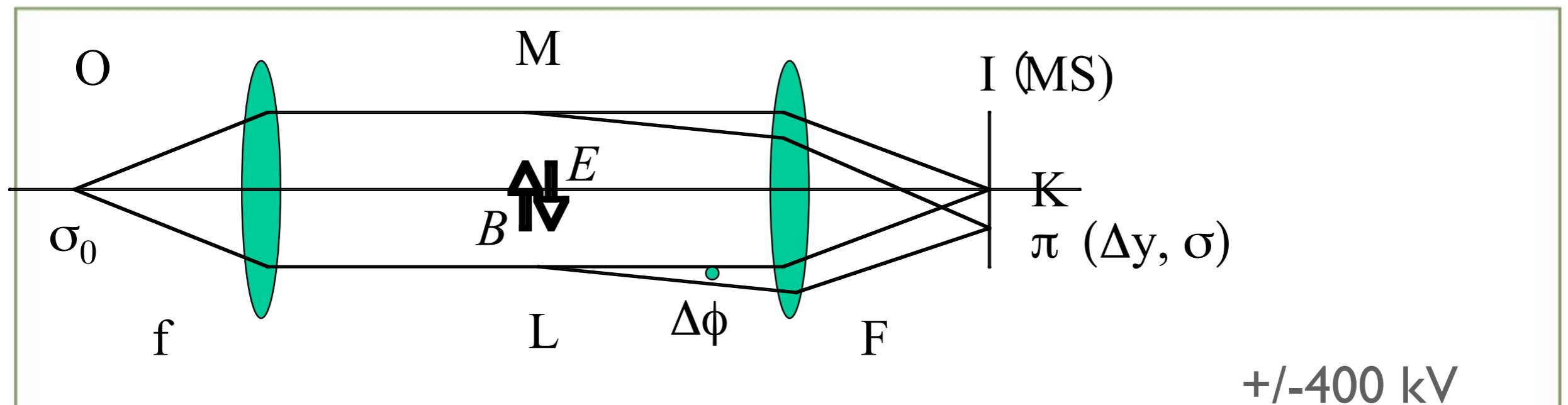


Fig. 6. 24-GeV production cross sections on 1-cm carbon target.

SPES II for (K^-, π^-)



Electro-Static Mass Separator

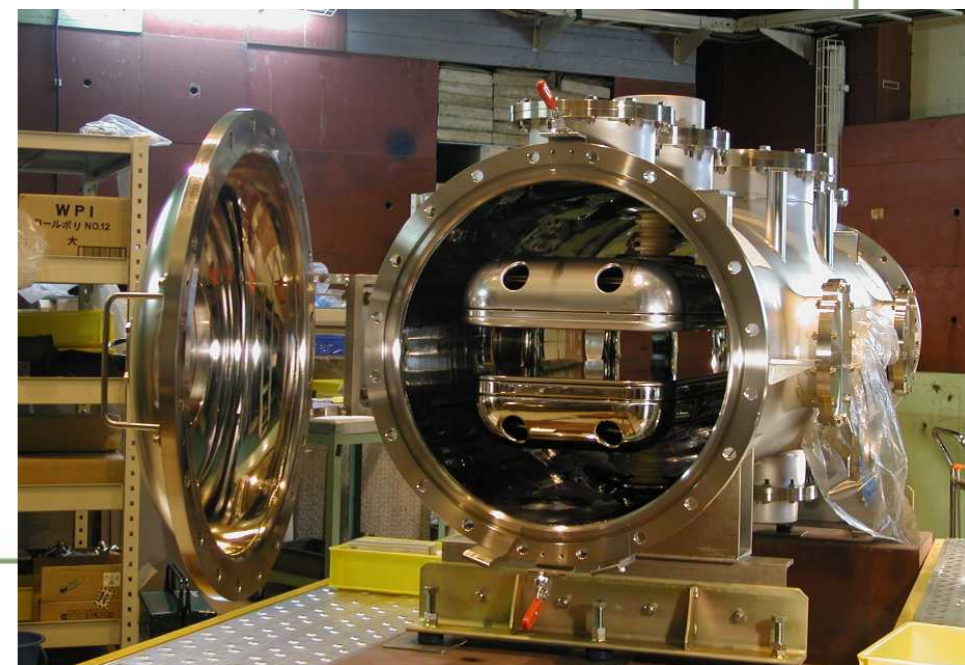


$$\Delta\phi = eEL (\beta_K^{-1} - \beta_\pi^{-1}) / (pc)$$

$$\Delta y = -F\Delta\phi$$

$$\sigma = -(F/f)\sigma_0$$

$$S = \Delta y / \sigma = \Delta\phi \sigma_0 / f$$



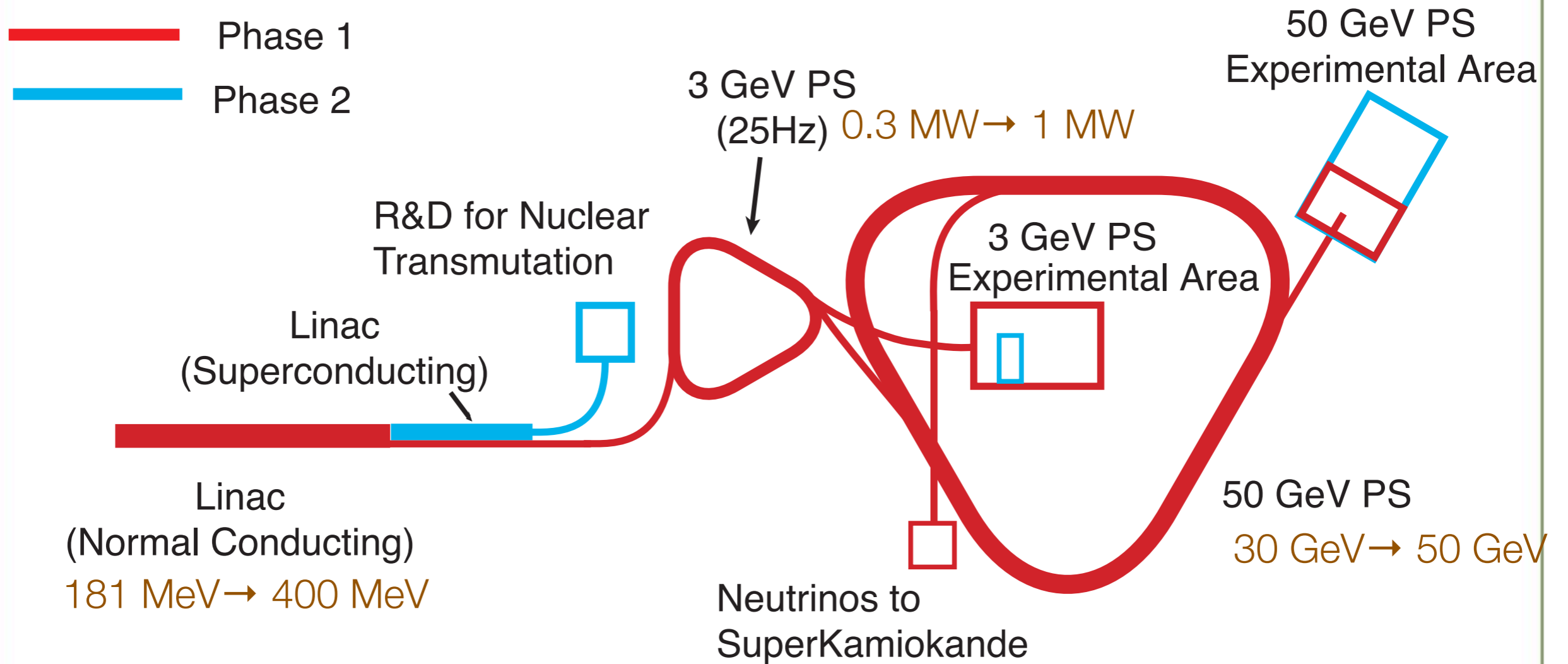
Decay of Meson Beams

- ▶ Lifetime ($c\tau$): π^+ (7.8045 m), K^- (3.713 m)
- ▶ Decay Length = $\beta\gamma c\tau = p/m \cdot c\tau$
 - ▶ K^- @ 1 GeV/c : $1000/500 \cdot c\tau = 7.4$ m
5m line: Decay rate = $1 - \exp(-5\text{m}/7.4\text{m}) \sim 49\%$
 - ▶ π^- @ 1 GeV/c : $1000/140 \cdot c\tau = 55.7$ m
15m line: Decay rate = $1 - \exp(-15\text{m}/55.7\text{m}) \sim 23\%$

Introduction to J-PARC

- ▶ Japan Proton Accelerator Research Complex
- ▶ Three high-intensity proton beams at 400 MeV (LINAC), 3 GeV (RCS), and 50 GeV(MR).
- ▶ To produce various secondary beams in high-intensity: K , π , anti- p , ν , neutron, μ , etc.
- ▶ Construction: 2001 - 2008
- ▶ Joint Project between KEK and JAEA

Phase 1 & 2



Phase 1: → Total 1,500 Oku-Yen (56% JAEA, 44% KEK)!

**J-PARC Facility
(KEK/JAEA)**

South to North

Linac

**3 GeV
Synchrotron**

**Neutrino Beams
(to Kamioka)**

**Materials and Life
Experimental
Facility**

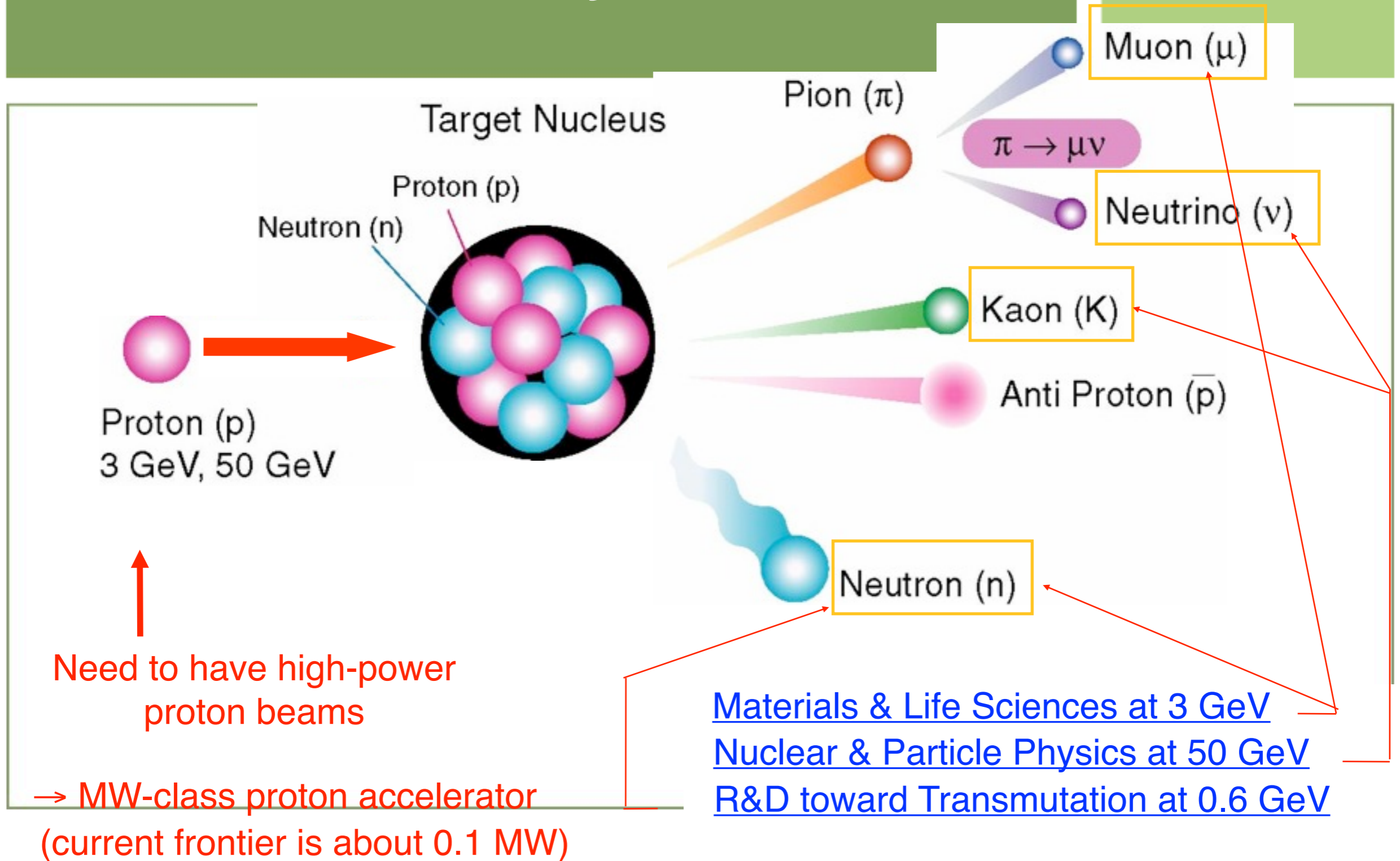
**50 GeV
Synchrotron**

**Hadron Exp.
Facility**

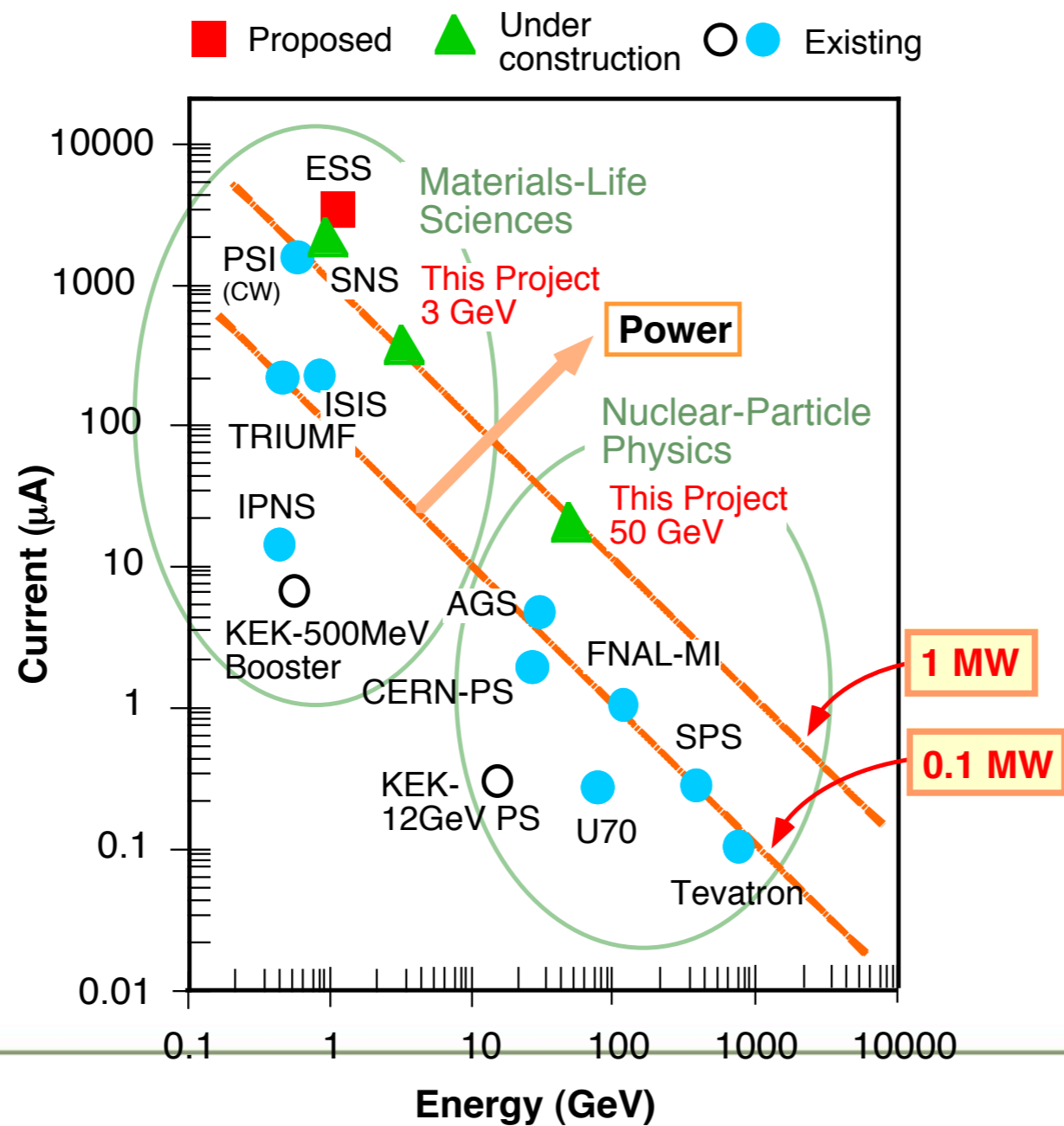
- CY2007 Beams**
- JFY2008 Beams**
- JFY2009 Beams**

Photo in July of 2009

Goals at J-PARC



Beam Power Frontier





Materials and Life Science Experimental Facility

Facility similar to SNS in the US
and to ISIS in the UK



Materials & Life Science Experimental Facility

Number of Users: about 3,000

**Neutron Beam Lines
(23 total)**

Neutron Scattering Area

Muon Experimental Area

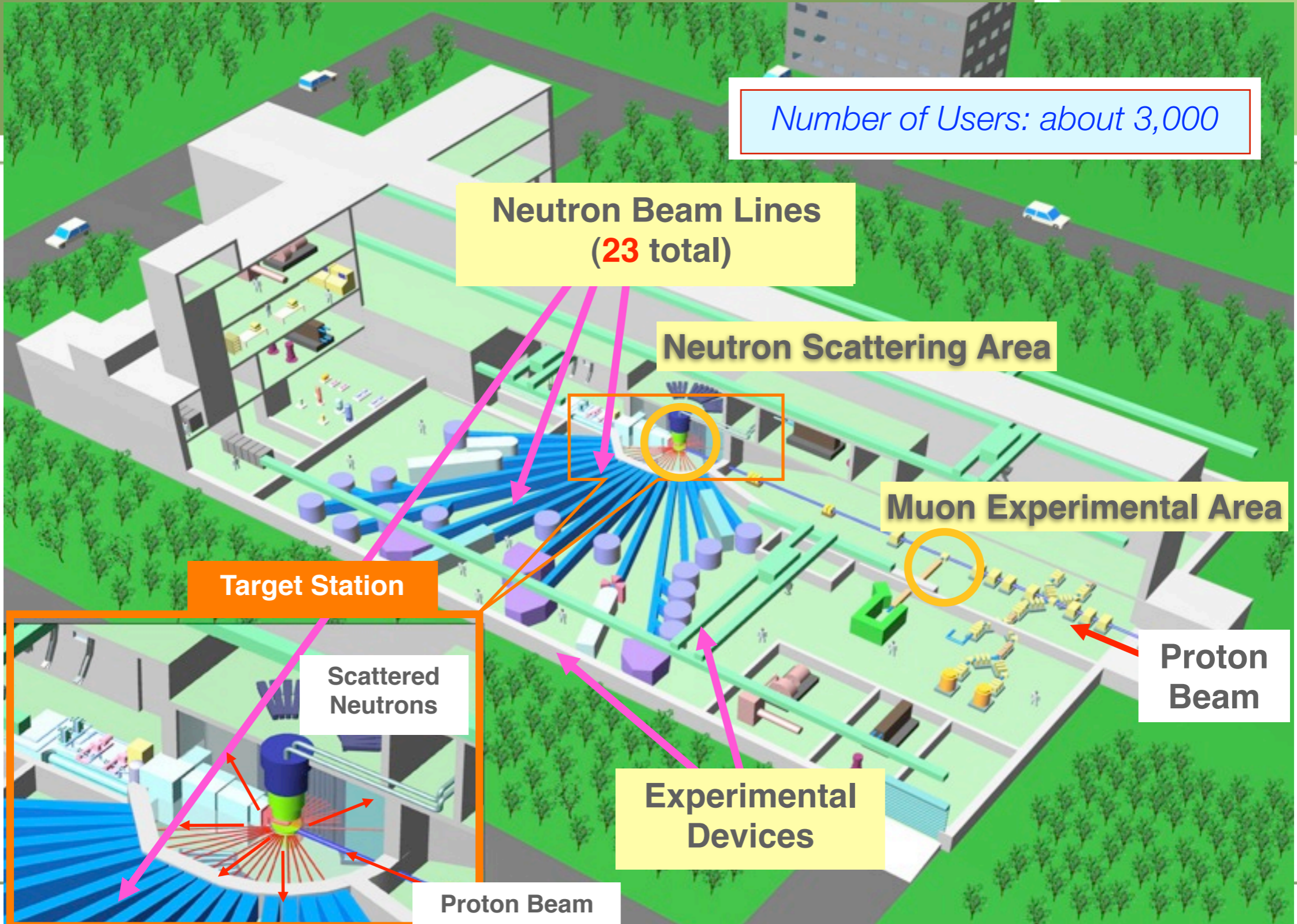
Target Station

**Proton
Beam**

**Scattered
Neutrons**

**Experimental
Devices**

Proton Beam





295 km
West

Neutrino Experimental Facility

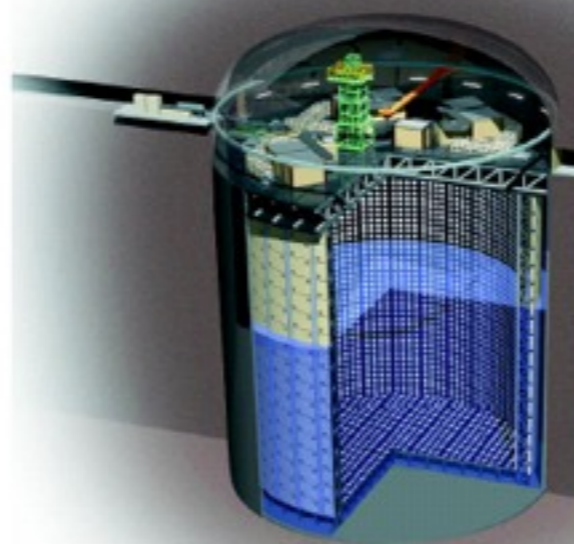


Number of Users: about 400

(about 1/4 from Japan)

Experiments with Intense Neutrino Beams

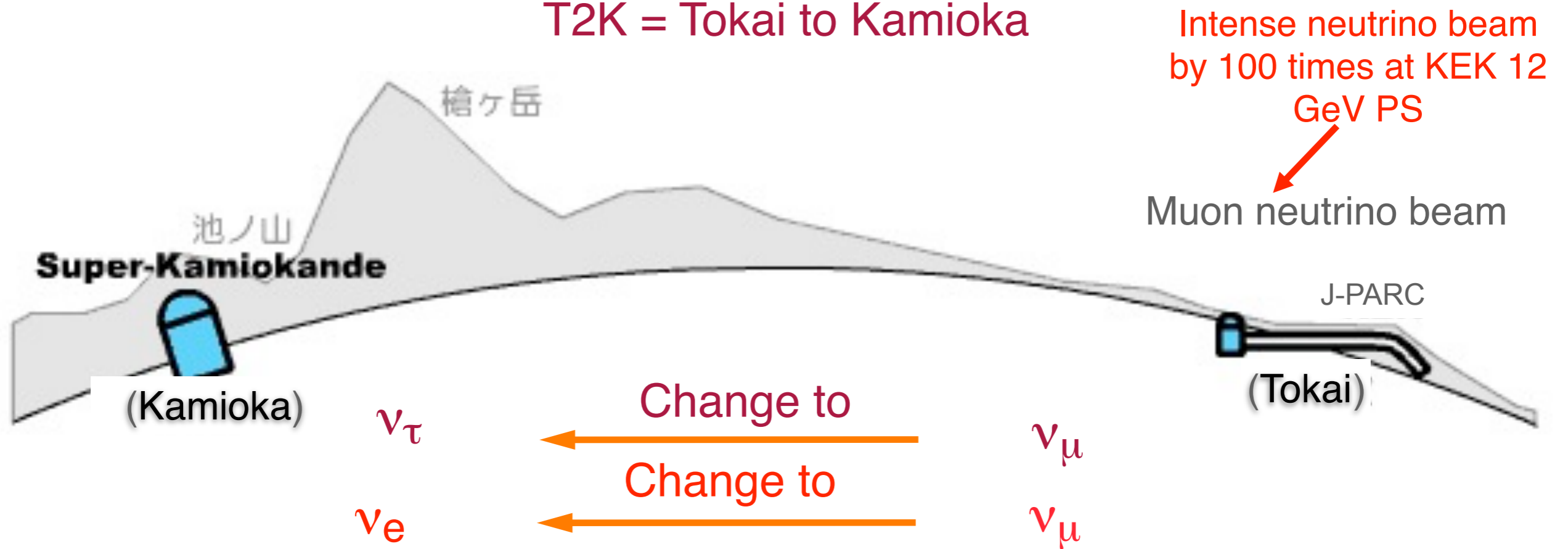
Super Kamiokande



岐阜県神岡町地下1000m
50000トン水チェレンコフ
20インチPMT約12000本
1996~

T2K Experiment

T2K = Tokai to Kamioka

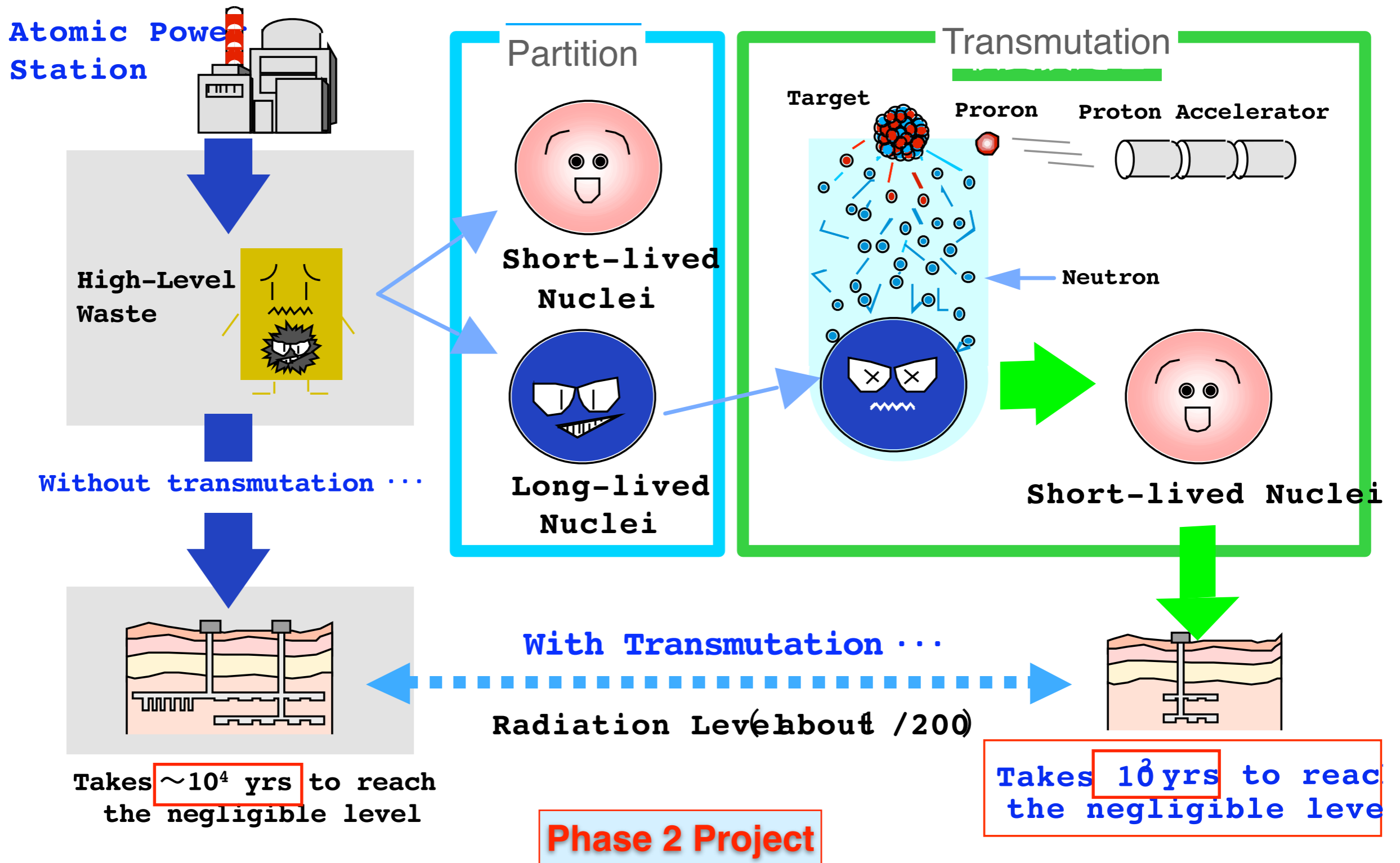


Disappearance of $\nu_\mu \leftrightarrow$ High Statistics T2K

(Five year data at KEK-PS can be measured within a few weeks at J-PARC)

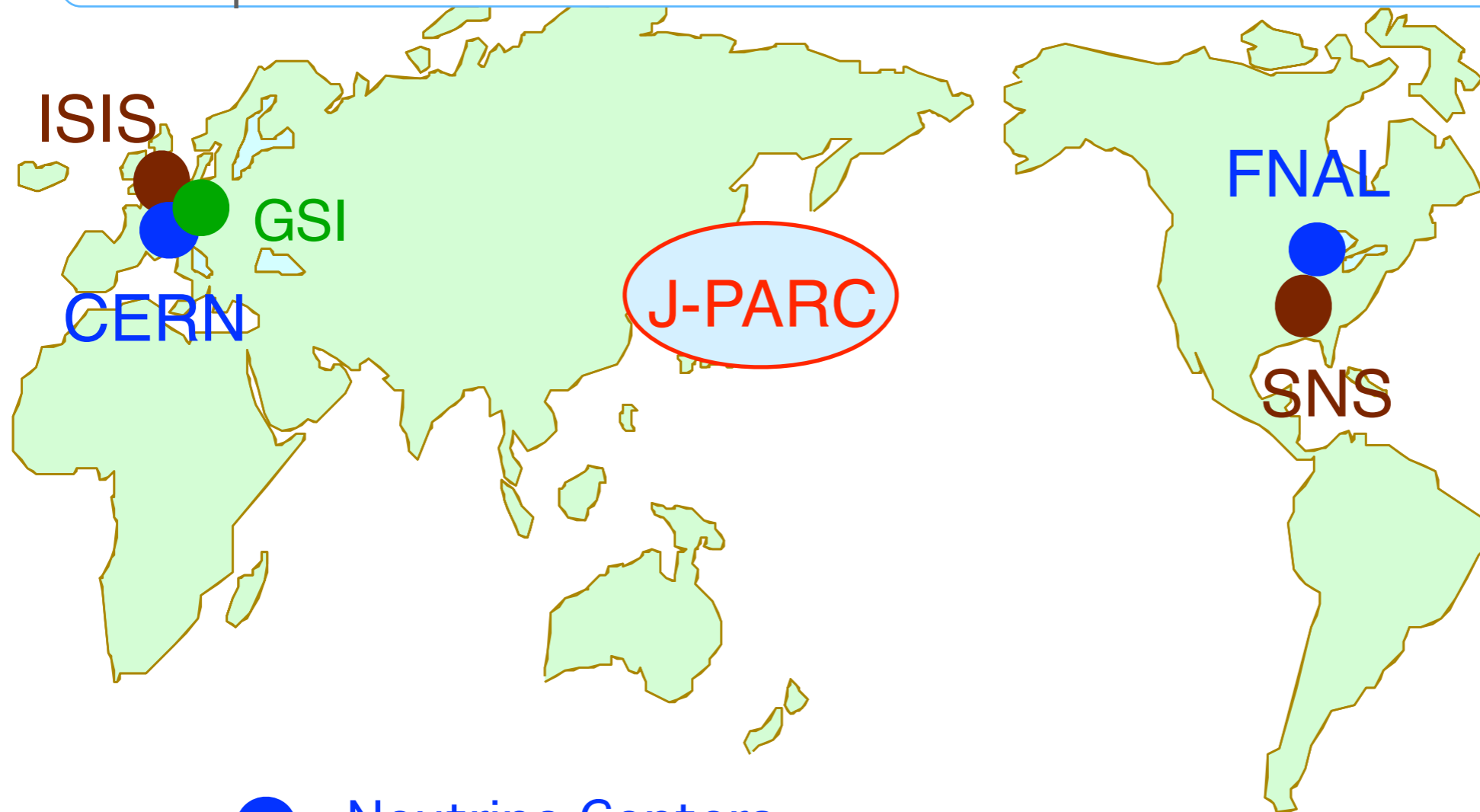
Detection of ν_e at Super Kamiokande \leftrightarrow Totally new experiment

Accelerator-Driven Transmutation (ADS)



International Research Center

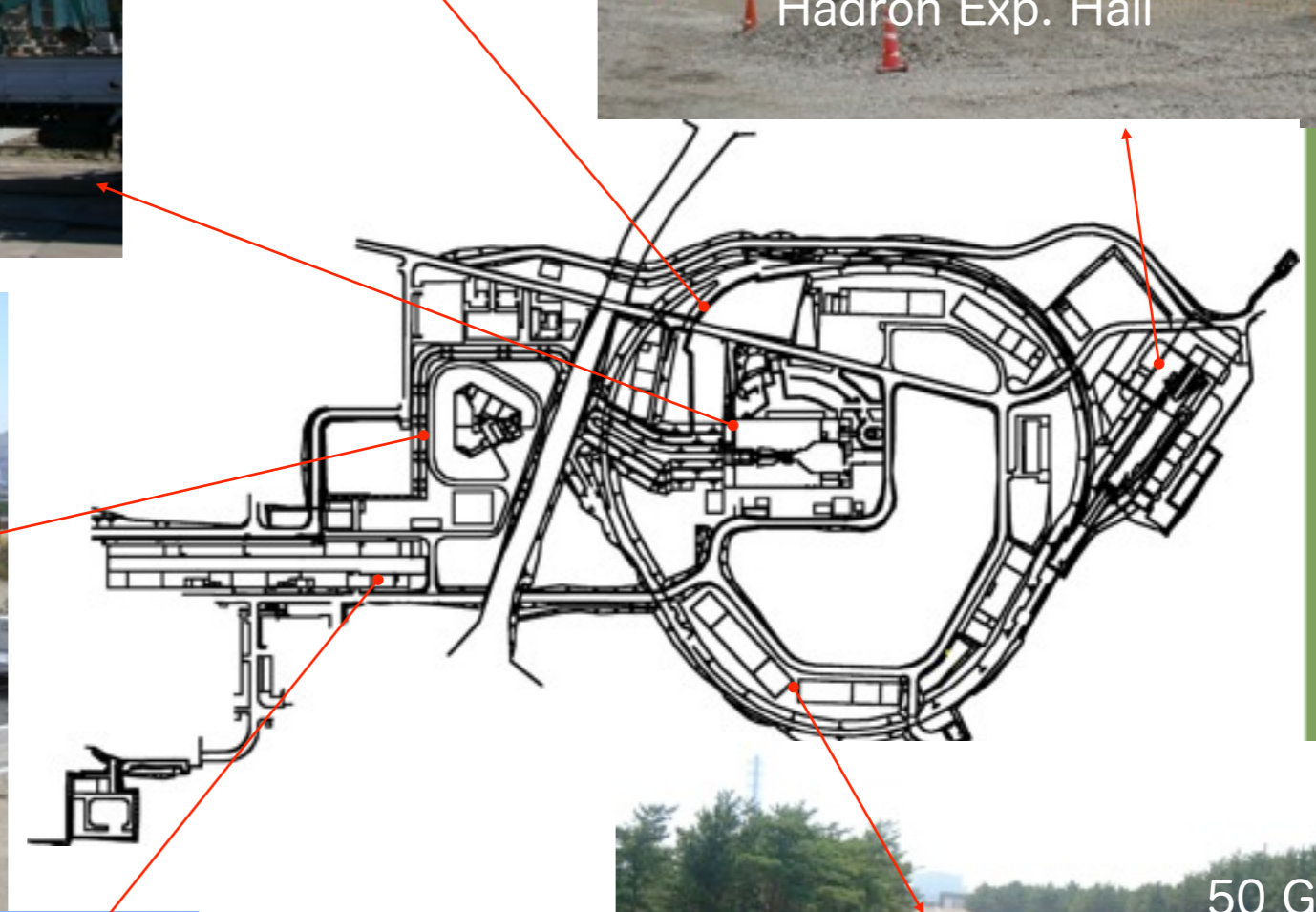
- One of Three major Neutron Sources in Material and Life Science
- Unique Kaon Factory, and One of Three Neutrino beam lines.
Anti-proton in GSI.
- Top runner in ADS.



● Neutrino Centers

● Neutron Centers

● Anti-p





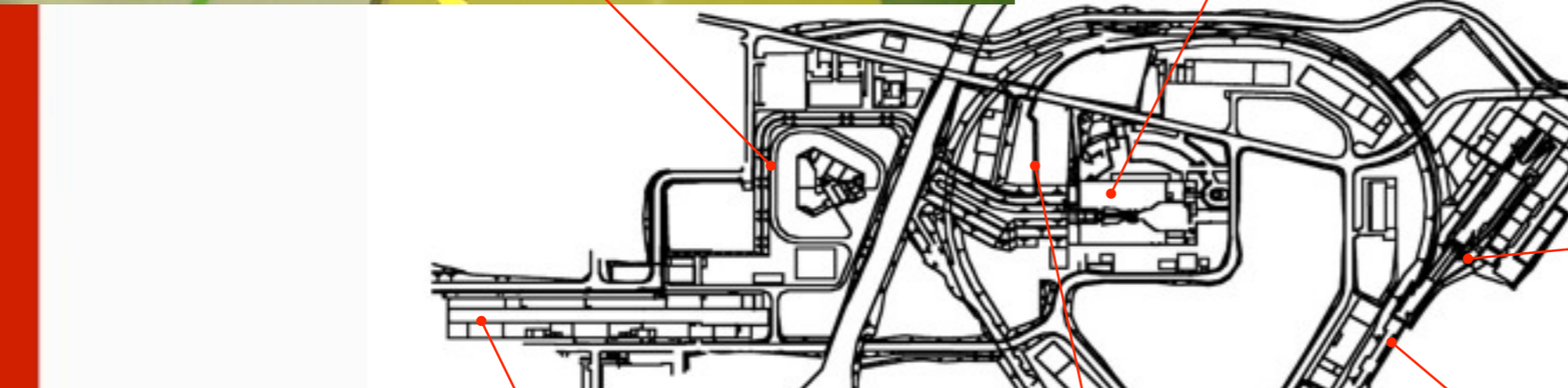
3GeV Synchrotron
(Autumn 2007, Beam Comm.)



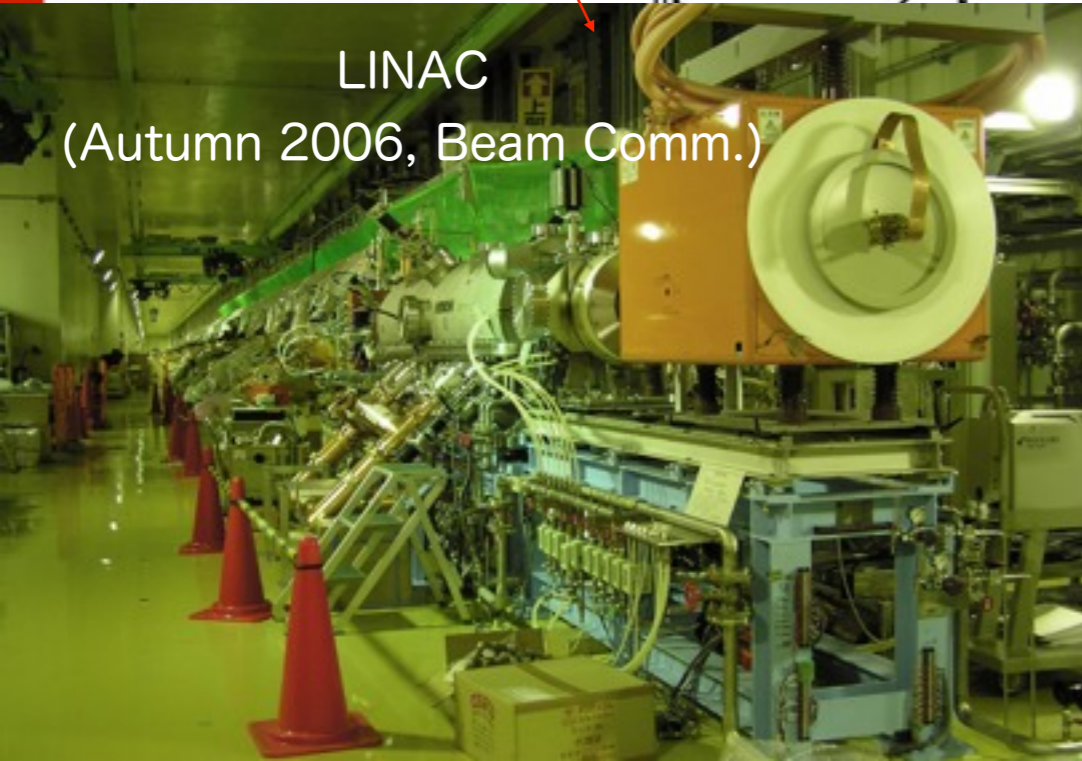
Muon Line
(Mid. 2008)



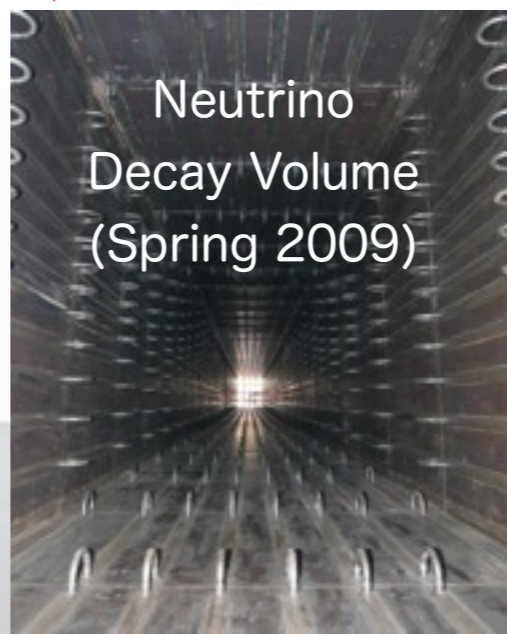
Neutron Source
(Mid. 2008)



Hadron
(Dec. 2008)



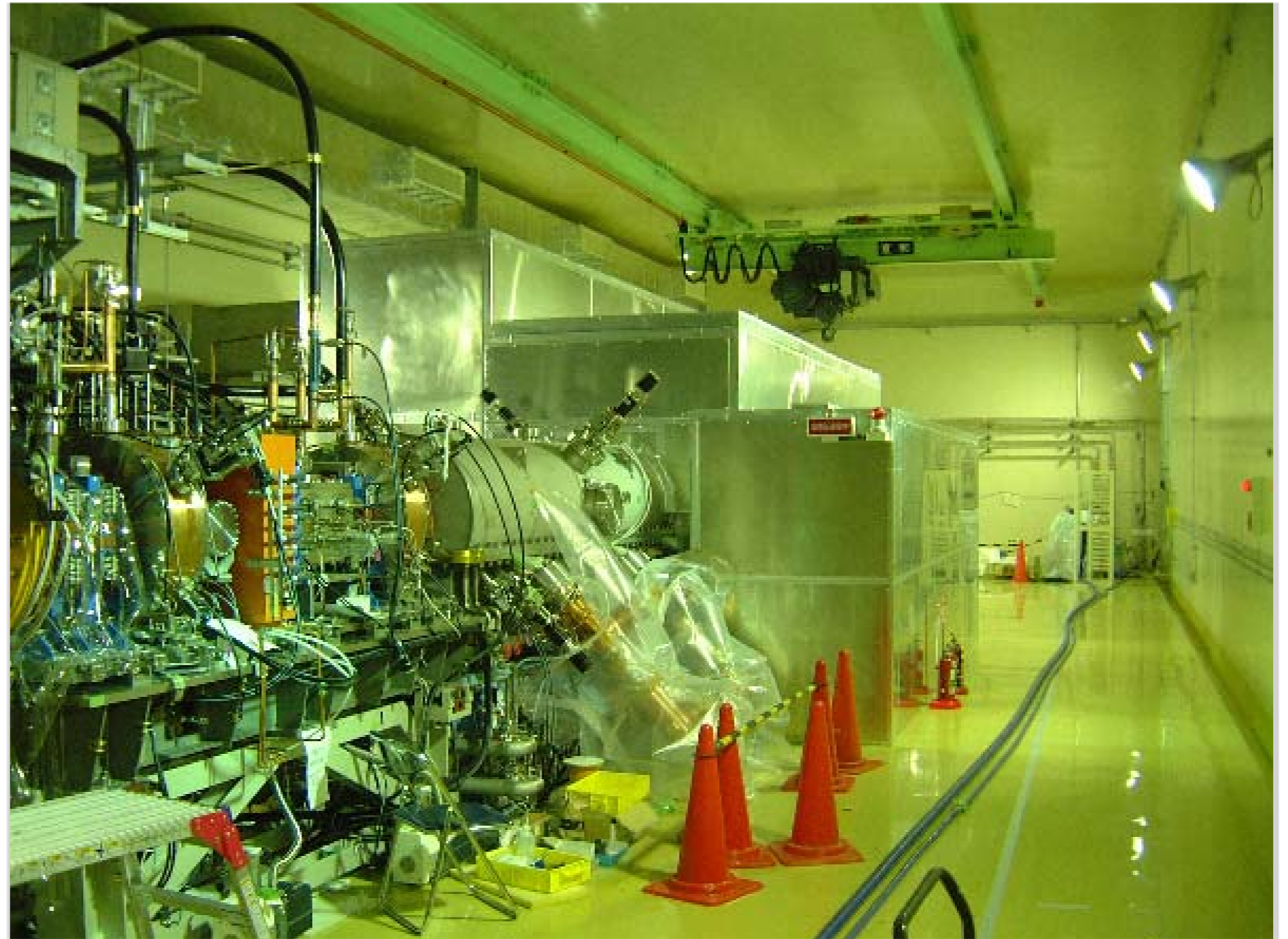
LINAC
(Autumn 2006, Beam Comm.)



Neutrino
Decay Volume
(Spring 2009)



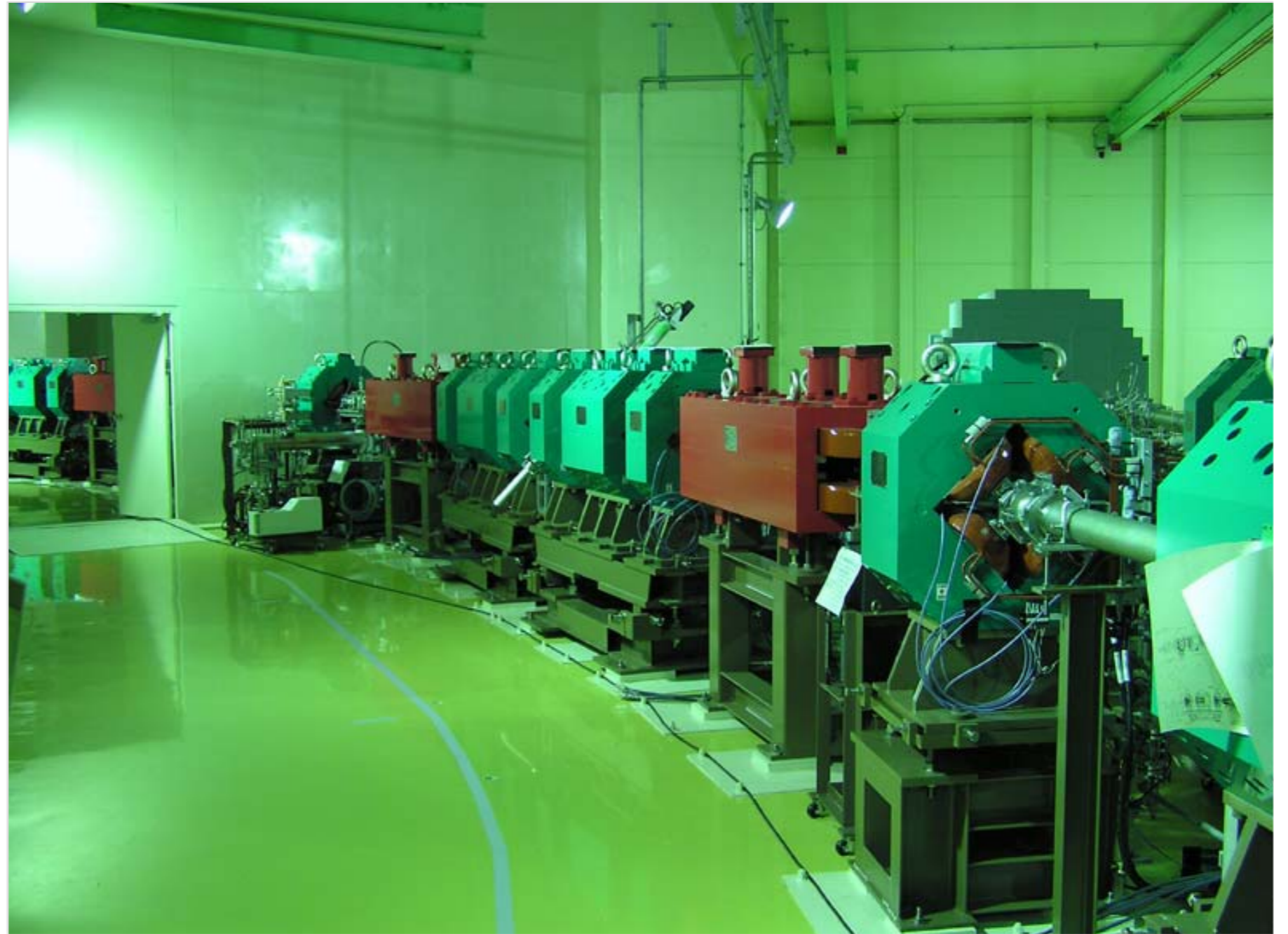
50 GeV Synchrotron
(Spring 2008, Beam Comm.)



H^- Ion Source, RFQ



SDTL



LINAC → 3 GeV



3GeV Ring



50 GeV Ring



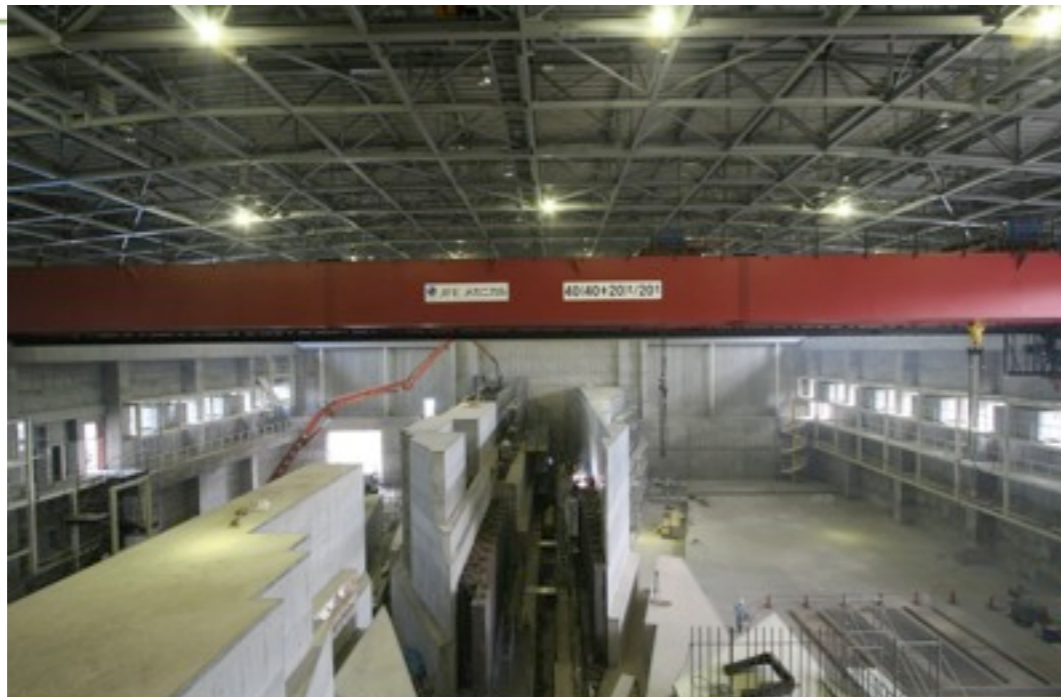
LINAC beam at 181 MeV: Jan.24,07



RCS acceleration at 3 GeV;
Oct. 31, 2007

Hadron Exp. Hall

60m x 56m
Compl. in July, 2007

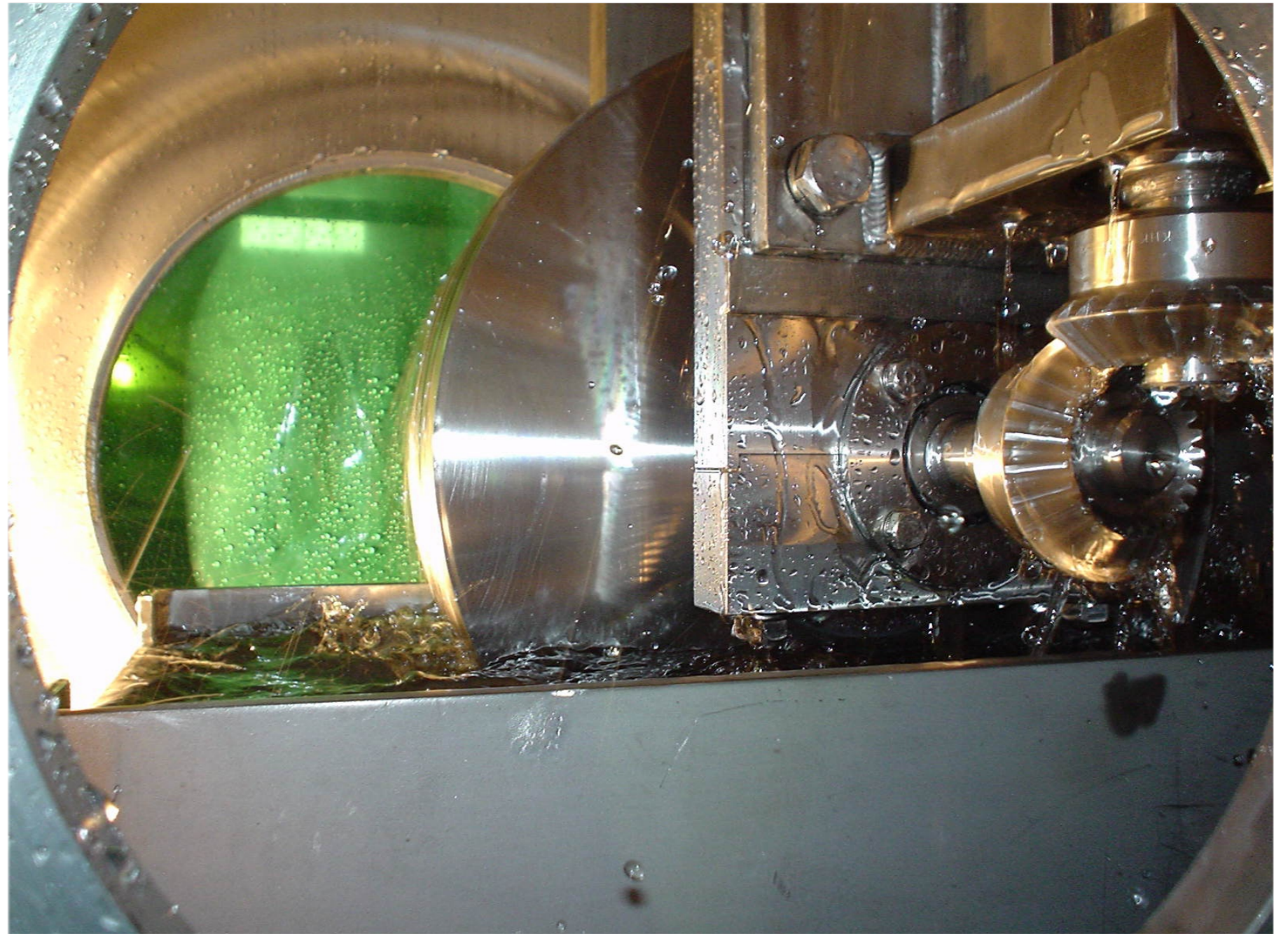




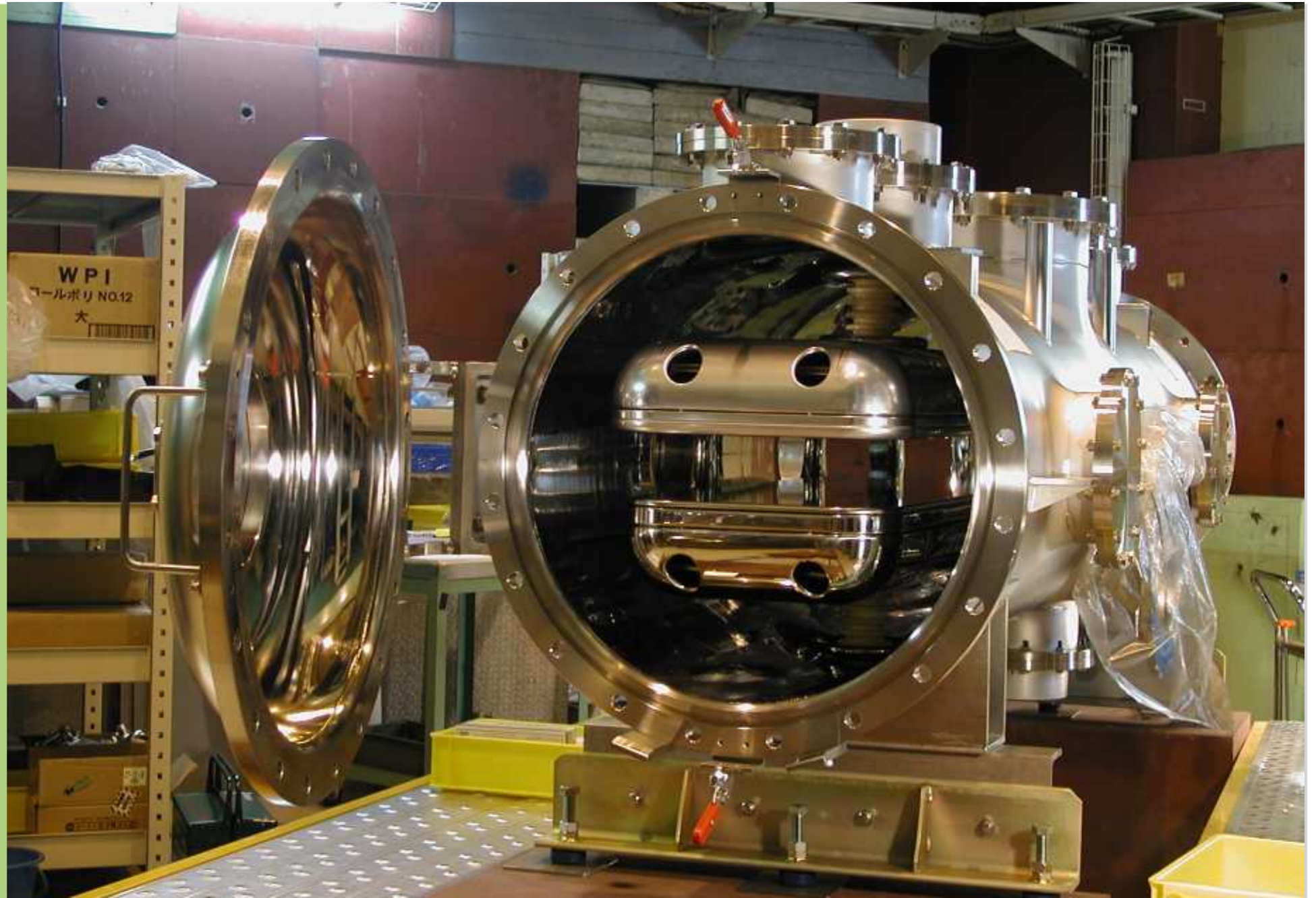
160 m long
Test starts
in Jan., 2007

Slow-extraction Line

12 kW
Ni rotator
water cooled



Production Target T1



3 m long
+/-400 kV
in 10cm gap

Electro-Static Separator

Mineral Insulator
Coil



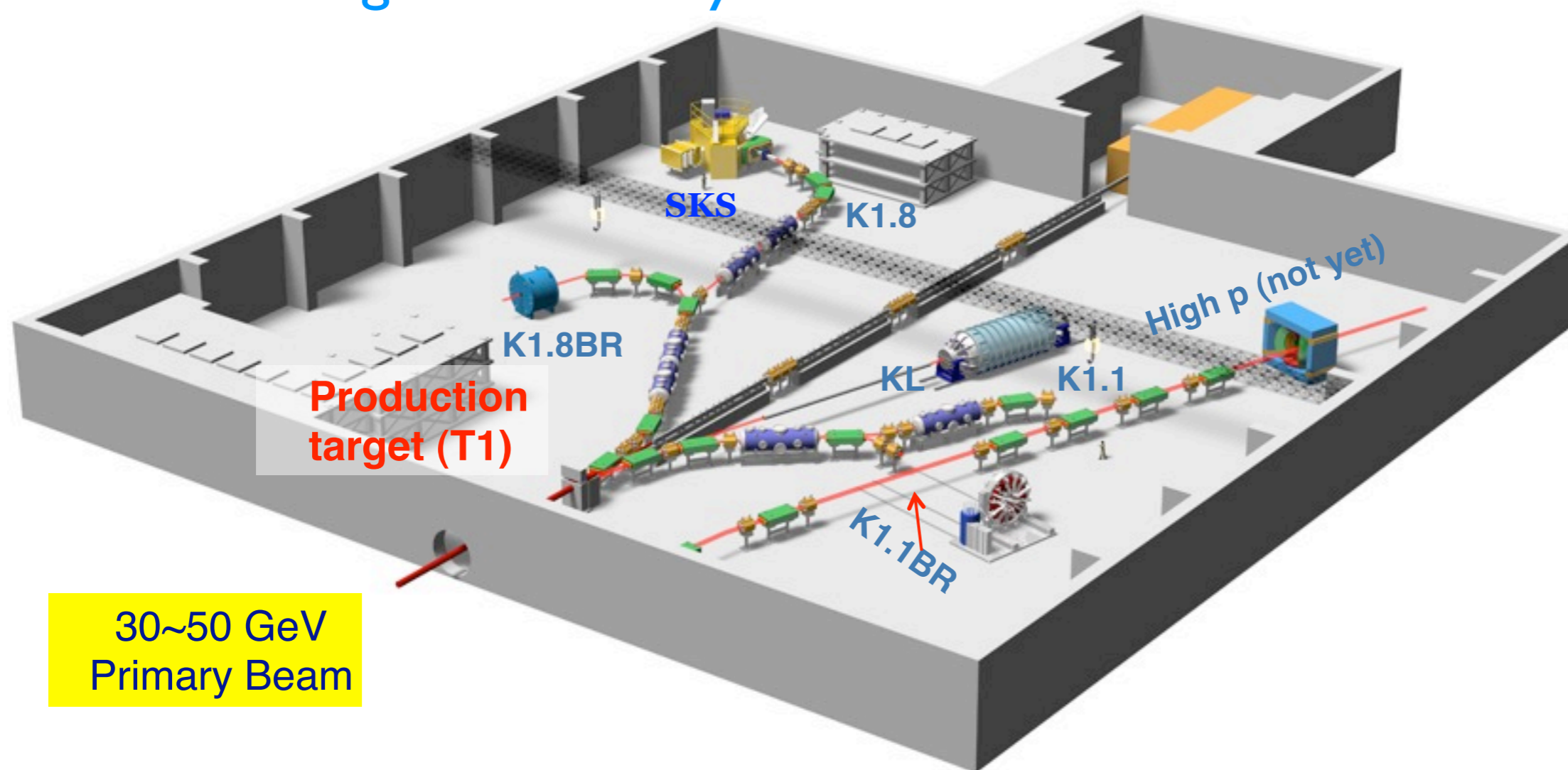
KI.8 DI coil

Hadron Experimental Hall

First beam in Feb. 2009

World highest intensity Kaon beams !

60m x 56m



30~50 GeV
Primary Beam

Production
target (T1)

K1.8BR

SKS

K1.8

KL

K1.1

K1.1BR

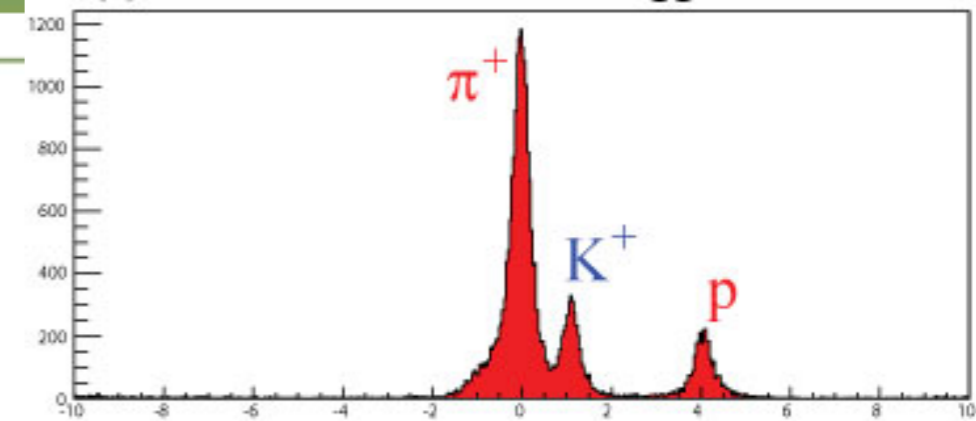
High p (not yet)

Recent beam status At Hadron Hall

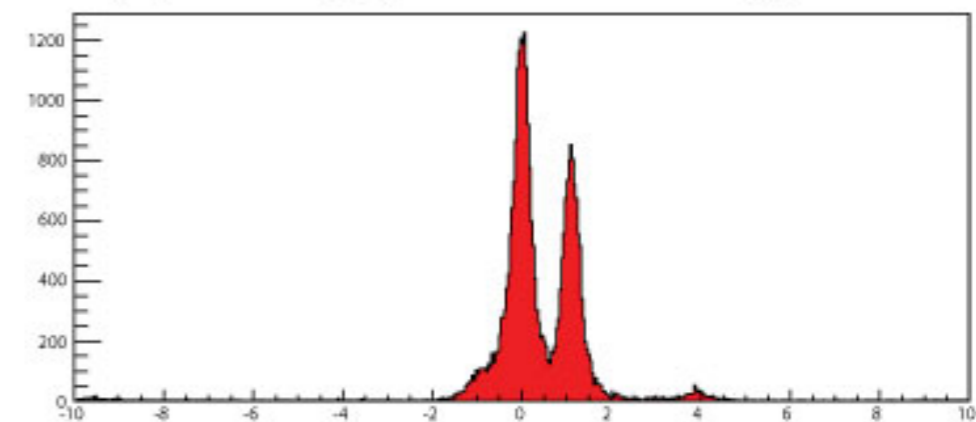
- ▶ Double-stage electro-static separator works very well
 - ▶ Good K/π ratio !
 - ▶ Intensity & Time structure should be improved.



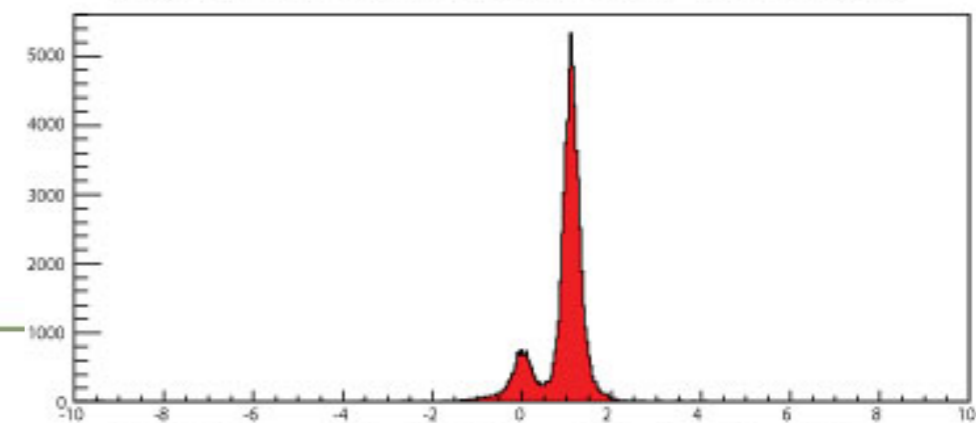
(a) ES1 off / ES2 off / "K" trigger



(b) ES1 on (K) / ES2 off / "K" trigger



(c) ES1 on (K) / ES2 on (K) / "K" trigger



Proposals at J-PARC

- ▶ Proposal Call : Nov., 2005 - Apr., 2006
- ▶ 20 proposals including 4 Lols
 - ▶ 13 proposals in Nuclear Physics
- ▶ **Five Day-I Experiments**
 - ▶ E05: Ξ hypernuclei Spectroscopy (Nagae) [1st priority]
 - ▶ E13: Hypernuclear γ -ray Spectroscopy (Tamura) [2nd priority]

- ▶ E15: Search for K^-pp bound state (Iwasaki, Nagae)
- ▶ E17: Kaonic ${}^3\text{He}$ $3d \rightarrow 2p$ X-ray (Hayano, Ota)
- ▶ E19: Search for Penta-quark in $\pi^-p \rightarrow K^-X$ reaction (Naruki)
 - ▶ ↑ Day-1 experiments --
- ▶ E07: Hybrid-Emulsion for Double- Λ (Imai, Nakazawa, Tamura)
- ▶ E03: Ξ^- -atom X rays (Tanida)
- ▶ E10: Production of neutron-rich Λ -hypernuclei with the double-charge-exchange reaction (A. Sakaguchi and T. Fukuda)
- ▶ and more ...

Kaonic Nuclei

Excitation Energy

(MeV)

500

400

300

200

100

0

$\Xi^0 \otimes^{A-1} [Z]$

$\Xi^- \otimes^{A-1} [Z+1]$

$\Lambda\Lambda \otimes^{A-2} [Z]$

$\bar{K}^0 \otimes^A [Z]$

$K^- \otimes^A [Z+1]$

$\Sigma^+ \otimes^{A-1} [Z-1]$

$\Sigma^0 \otimes^{A-1} [Z]$

$\Sigma^- \otimes^{A-1} [Z+1]$

$\Lambda \otimes^{A-1} [Z]$

$\pi^- \otimes^A [Z+1]$

$A [Z]$

$A [Z+1]$

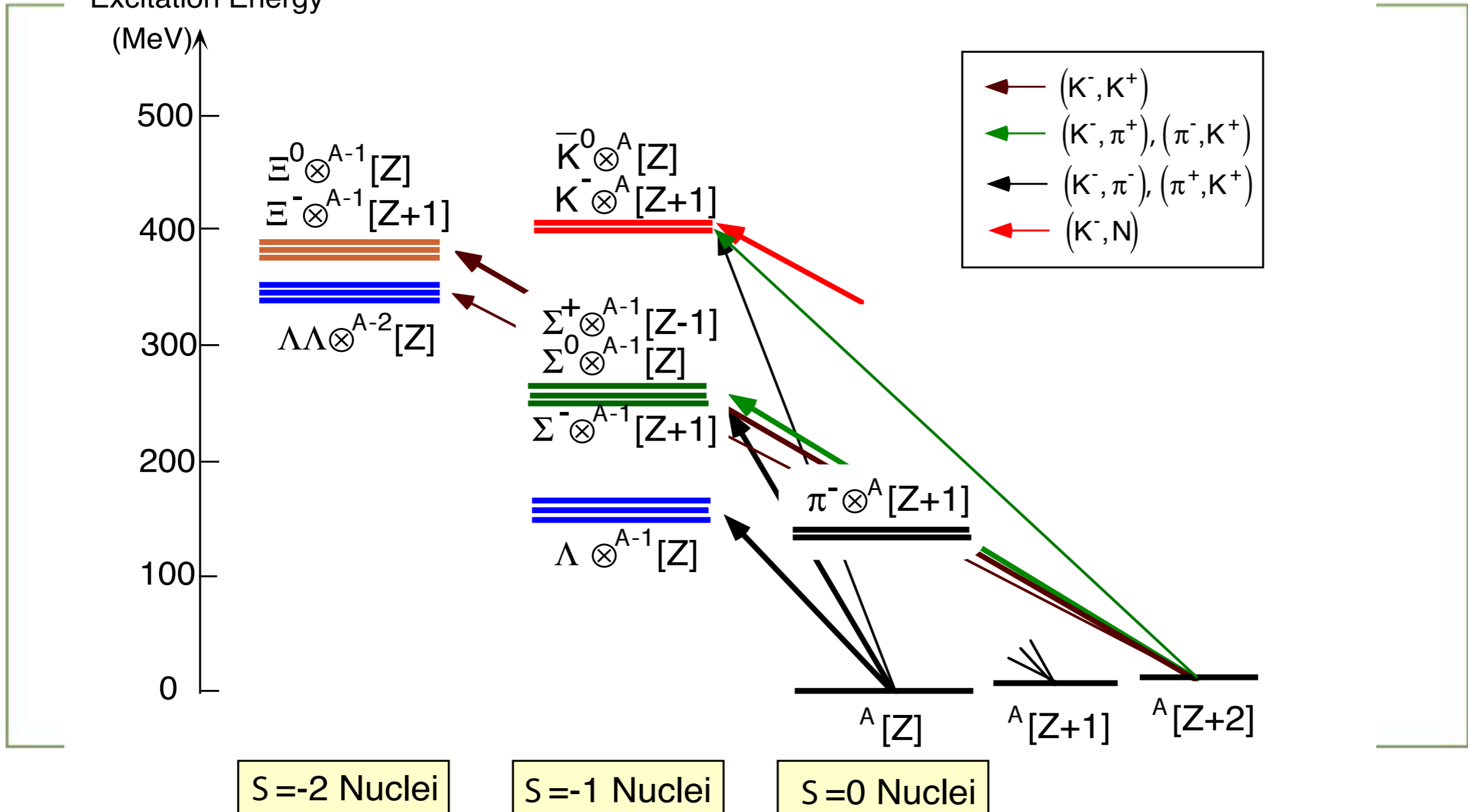
$A [Z+2]$

- $\leftarrow (K^-, K^+)$
- $\leftarrow (K^-, \pi^+), (\pi^-, K^+)$
- $\leftarrow (K^-, \pi^-), (\pi^+, K^+)$
- $\leftarrow (K^-, N)$

S = -2 Nuclei

S = -1 Nuclei

S = 0 Nuclei



$\bar{K}N$ Bound States

► Prediction by Akaishi and Yamazaki

► $\bar{K}N$ scattering lengths

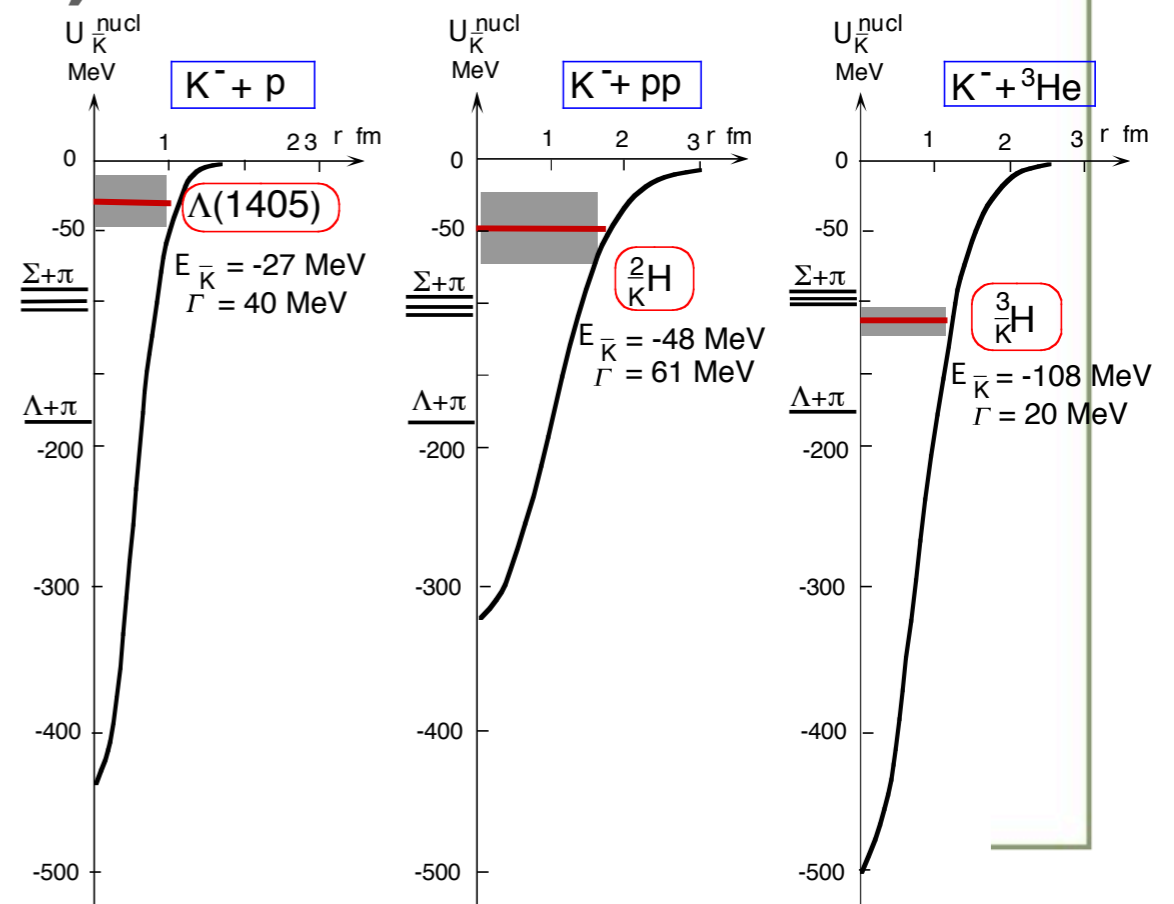
► K^-p atomic shift (KEK E228)

► Mass & width of $\Lambda(1405)$



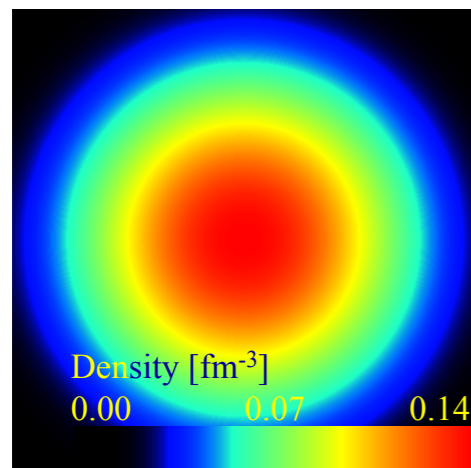
► **Strong attraction in $I=0$ $\bar{K}N$ interaction**

► K^-pp , K^-ppp , K^-pppn , ...

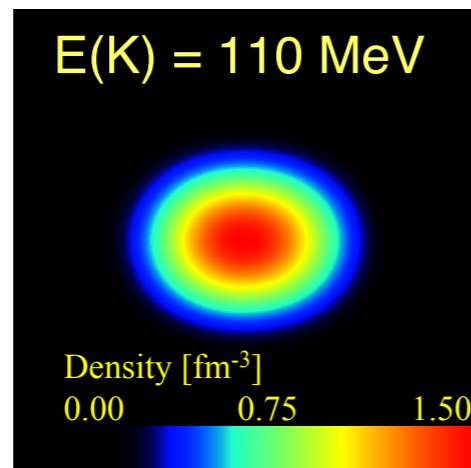


Formation of High Density State

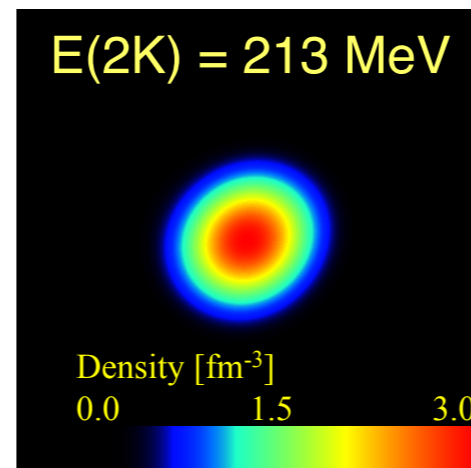
← 4 fm → ← 4 fm → ← 4 fm →



ppn
total B.E. = 6.0 MeV
central density = 0.14 fm^{-3}
 $R_{\text{rms}} = 1.59 \text{ fm}$



ppnK⁻
total B.E. = 118 MeV
central density = 1.50 fm^{-3}
 $R_{\text{rms}} = 0.72 \text{ fm}$

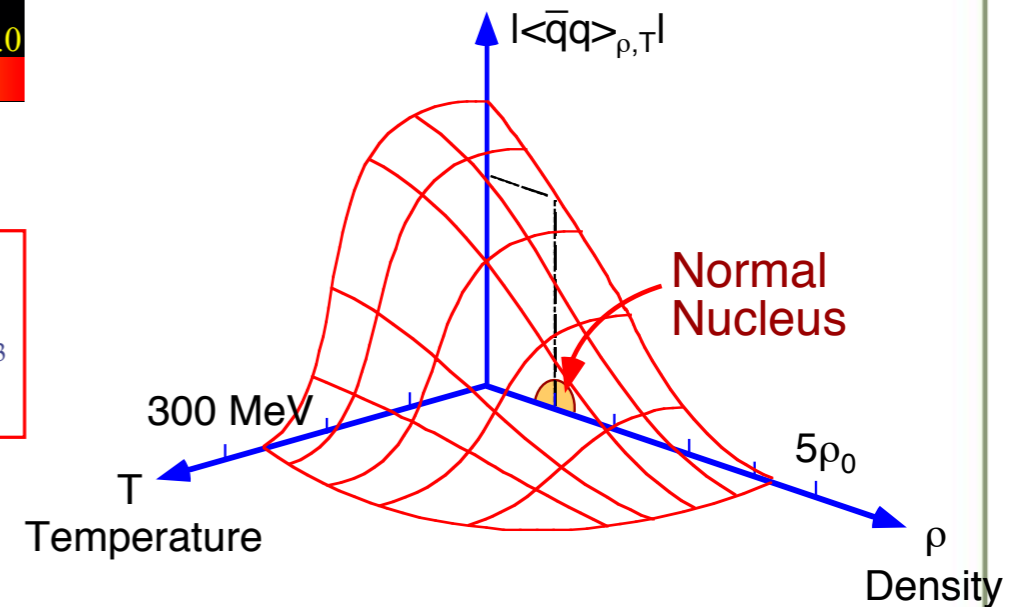


ppnK⁻K⁻
total B.E. = 221 MeV
central density = 3.01 fm^{-3}
 $R_{\text{rms}} = 0.69 \text{ fm}$

$\rho > \rho_0 \times 10$!?


Dote et al.

- ▶ Formation of **Cold**($T=0$) and **Dense**($\rho > 5 \rho_0$) nuclear matter
- ▶ Chiral symmetry restoration
- ▶ Kaon condensation



T. Hatsuda and T. Kunihiro, Phys. Rev. Lett. 55 (1985) 158.
W. Weise, Nucl. Phys. A443 (1993) 59c.

\bar{K} interaction

- ▶ $\bar{K}N$ interaction
 - strongly attractive in the isospin $I=0$ term
(A. D. Martin, kaonic hydrogen X-ray @ KpX)
- 
- ▶ How about \bar{K} -Nucleus interaction ?
 - ▶ Very deep attractive ? (150—200MeV)
 - ▶ Shallow attractive ? (50—75MeV)
 - ▶ *Ambiguity remains with kaonic atom data ($Q \ll Q_0$)*

Hadronic Atoms

E. Friedman, A. Gal / Physics Reports 452 (2007) 89–153

► Klein-Gordon equation

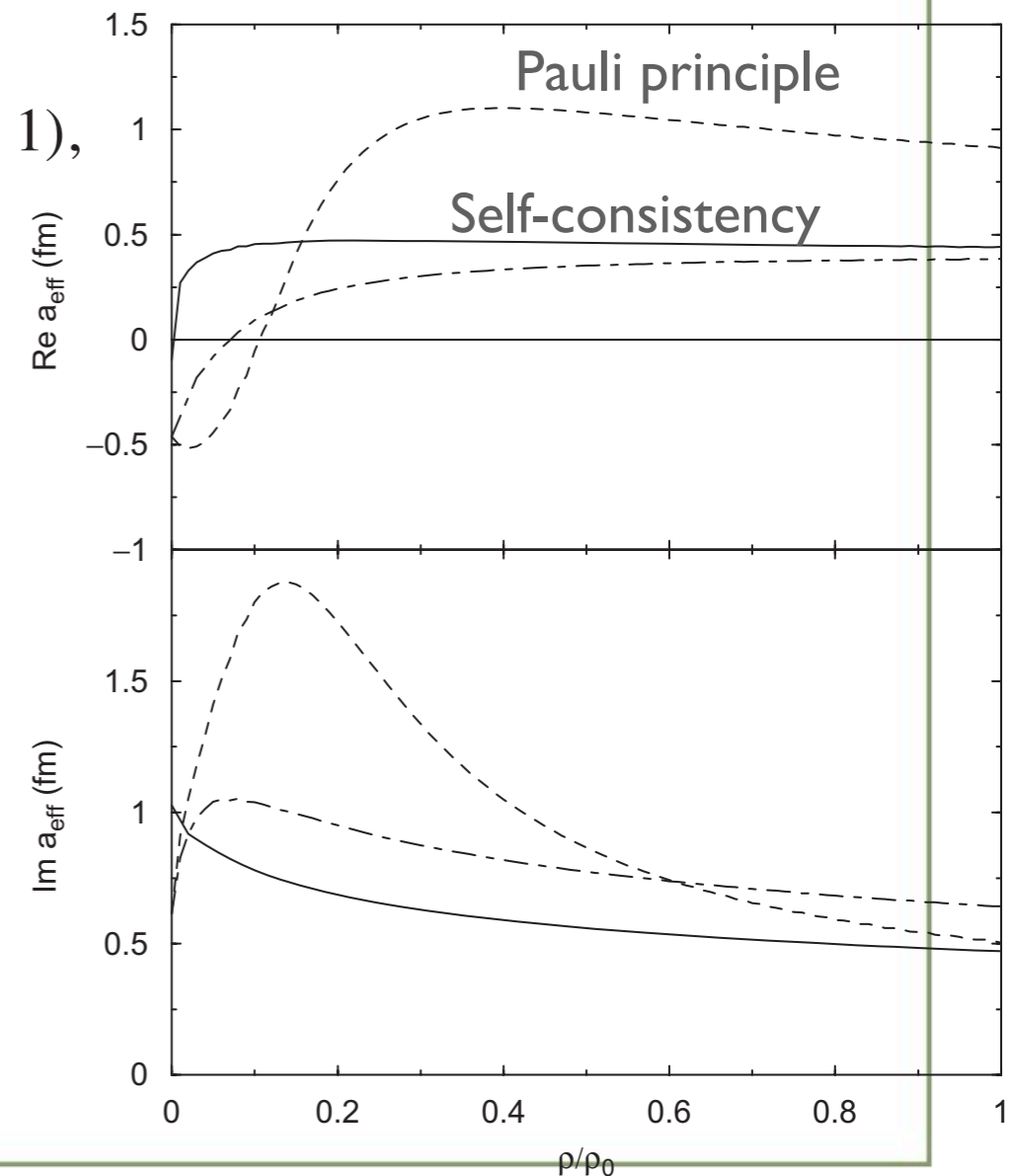
$$[\nabla^2 - 2\mu(B + V_{\text{opt}} + V_c) + (V_c + B)^2]\psi = 0 \quad (\hbar = c = 1),$$

$$2\mu V_{\text{opt}}(r) = -4\pi \left(1 + \frac{A-1}{A} \frac{\mu}{M}\right) \{b_0[\rho_n(r) + \rho_p(r)] + \tau_z b_1[\rho_n(r) - \rho_p(r)]\}.$$

$$2\mu V_{\text{opt}}(r) = -4\pi \left(1 + \frac{\mu}{M}\right) [a_{K-p}(\rho)\rho_p(r) + a_{K-n}(\rho)\rho_n(r)],$$

where

$$a_{K-p} = b_0 - b_1, \quad a_{K-n} = b_0 + b_1$$



K⁻p interaction near threshold

► Threshold branching ratios

$$\gamma = \frac{\Gamma(K^- p \rightarrow \pi^+ \Sigma^-)}{\Gamma(K^- p \rightarrow \pi^- \Sigma^+)} = 2.36 \pm 0.04,$$

$$R_c = \frac{\Gamma(K^- p \rightarrow \pi^+ \Sigma^-, \pi^- \Sigma^+)}{\Gamma(K^- p \rightarrow \text{all inelastic channels})} = 0.664 \pm 0.011,$$

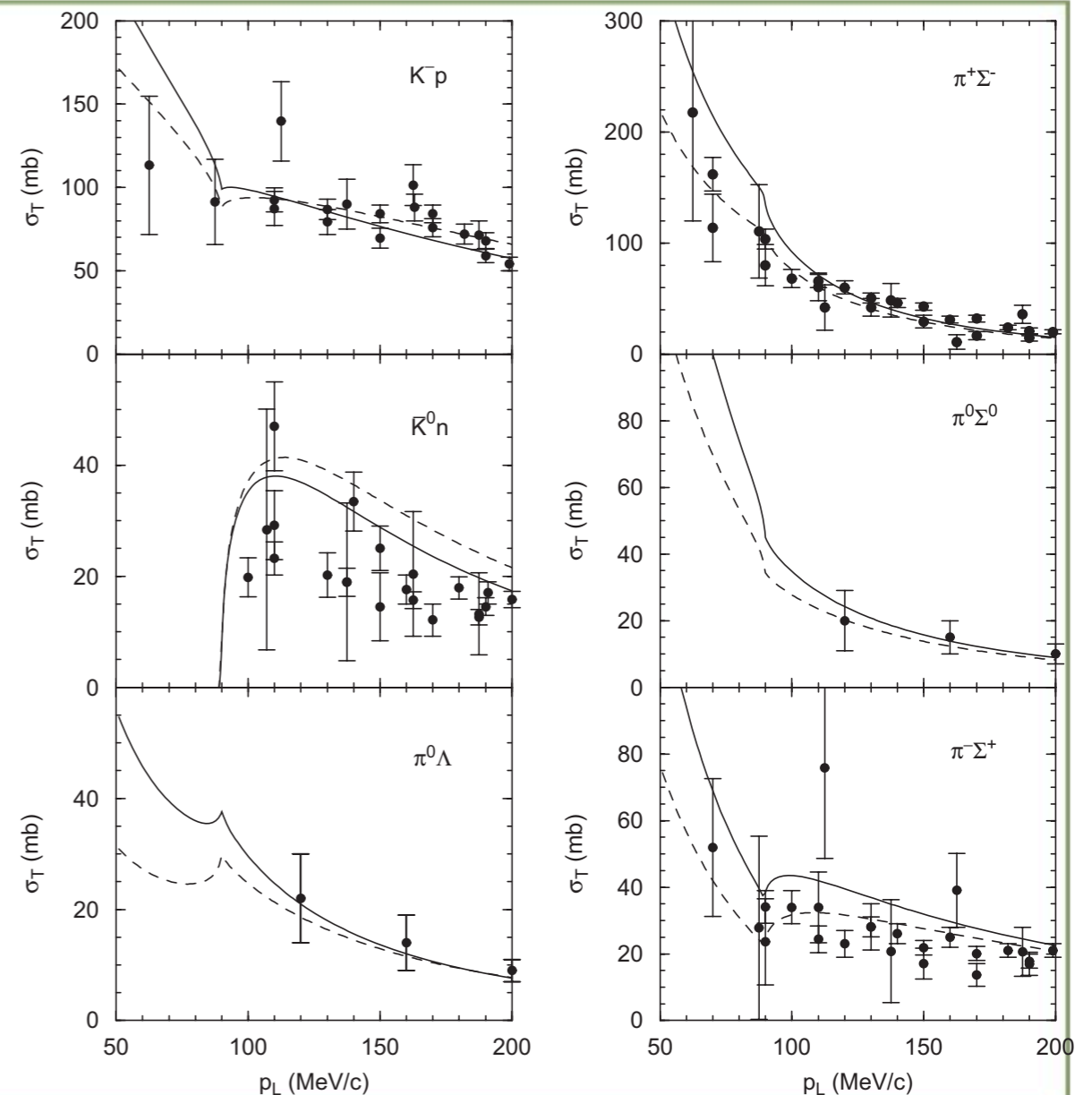
$$R_n = \frac{\Gamma(K^- p \rightarrow \pi^0 \Lambda)}{\Gamma(K^- p \rightarrow \pi^0 \Lambda, \pi^0 \Sigma^0)} = 0.189 \pm 0.015.$$

► K⁻p Scattering data

► Kaonic hydrogen

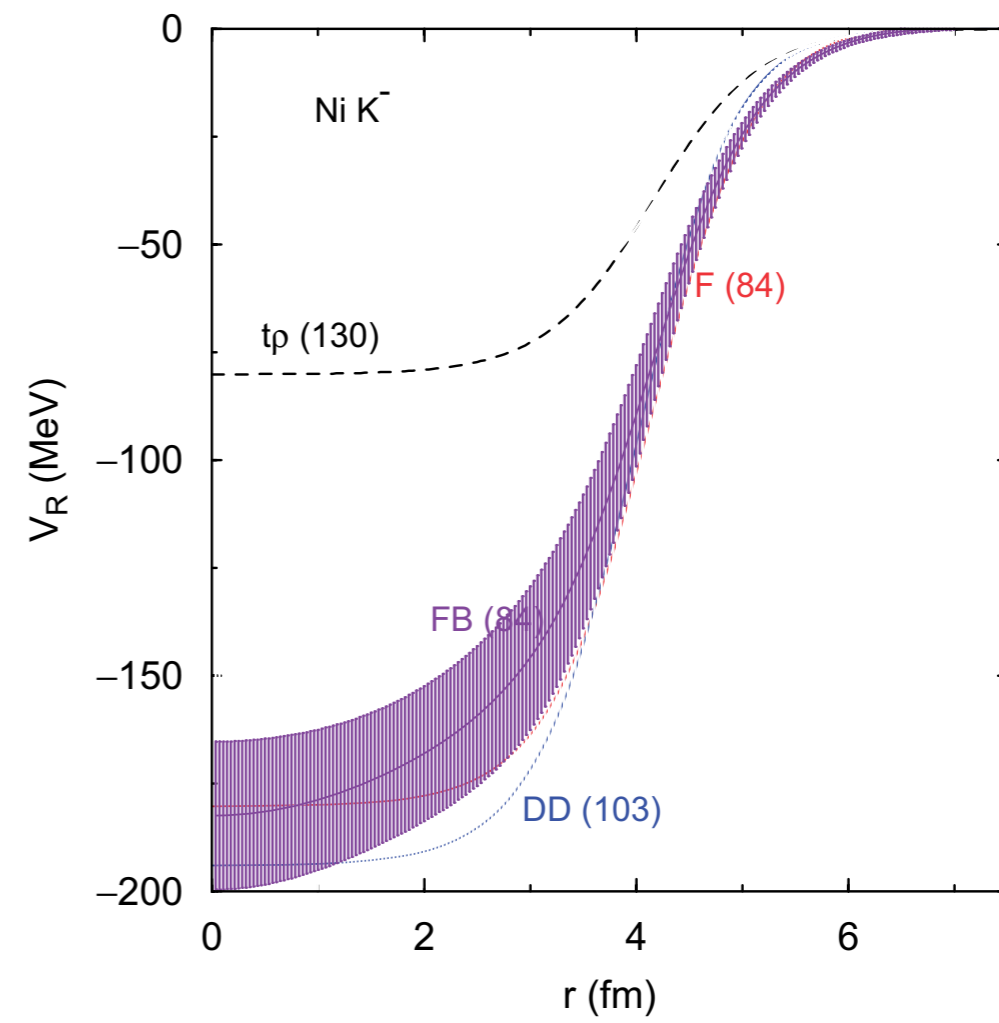
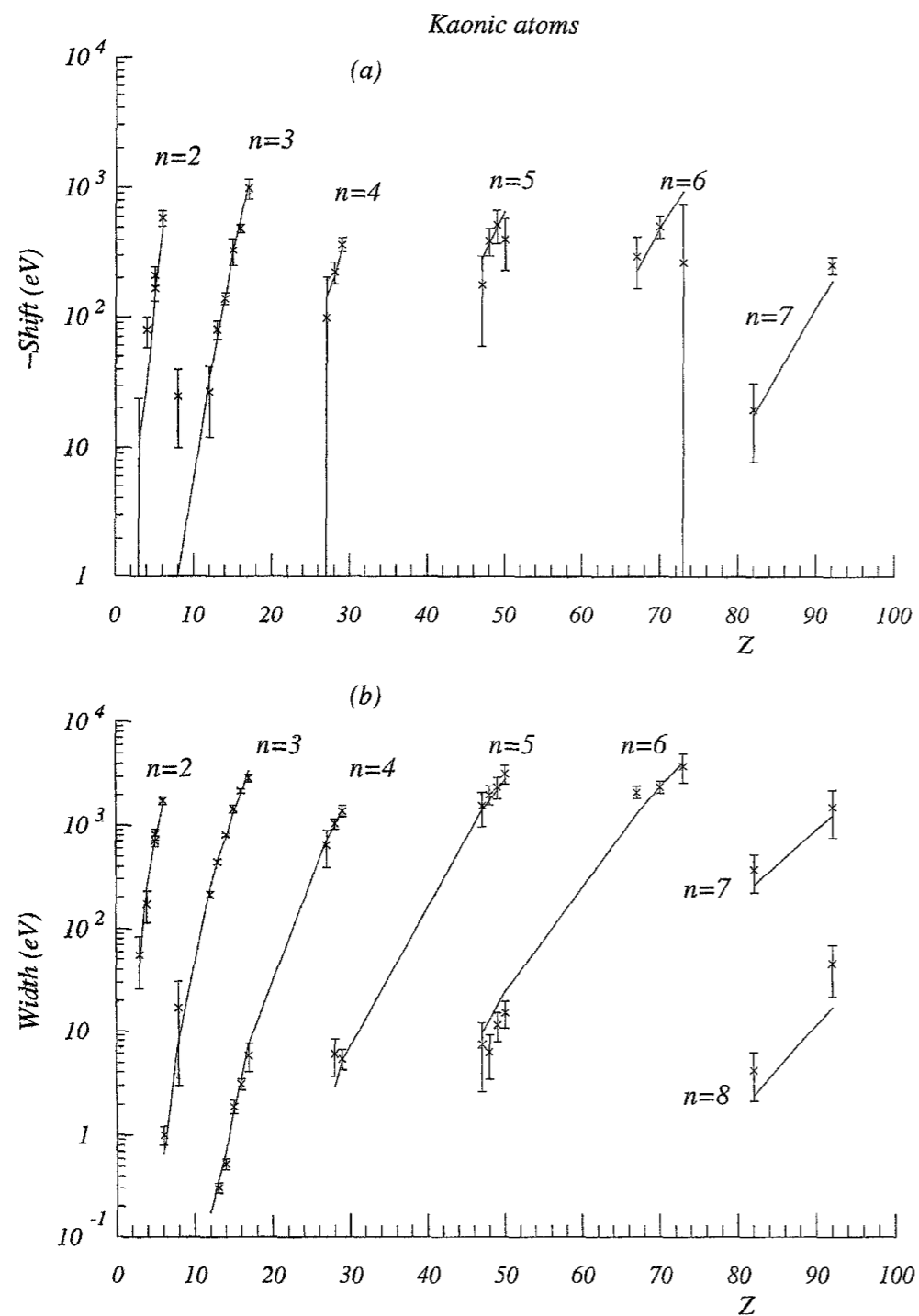
$$\epsilon_{1s} - i \frac{\Gamma_{1s}}{2} \approx -2\alpha^3 \mu_{K^-p}^2 a_{K^-p} (1 - 2\alpha \mu_{K^-p} (\ln \alpha - 1) a_{K^-p})$$

$$a(K^-p) = (-0.78 \pm 0.15 \pm 0.03) + (0.49 \pm 0.25 \pm 0.12)i \text{ fm}$$



Kaonic Atoms

C.J. Batty et al. / *Physics Reports* 287 (1997) 385–445



Antikaon in nuclear medium

- ▶ Theory
 - ▶ Kaon condensation in neutron stars
 - ▶ Mass modification in a high density matter
- ▶ Experiment
 - ▶ Heavy ion collision (high T)
 - ▶ Nuclear \bar{K} bound state (T=0)
 - ▶ could exist when the potential is very deep
 - ▶ predicted by Akaishi and Yamazaki

Importance of $\bar{K}NN$ Systems

- ▶ **K^-p :**

- ▶ $\Lambda(1405)$ is such a bound state or a 3-quark state ?

- **K^-pp , K^-pn , (K^-nn):**

- *modification of $\bar{K}N$ interaction, isospin dependence*

- ▶ **K^-ppn and/or K^-pnn , K^-ppp :**

- ▶ modification of $\bar{K}N$ interaction ?, Isospin dependence ?
- ▶ nuclear contraction effects
- ▶ many-body effect, relativistic effect,

Detection Methods (I)

▶ **Missing-mass spectroscopy**

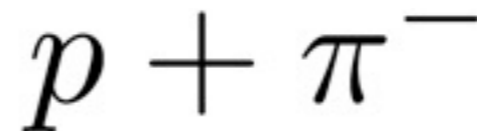
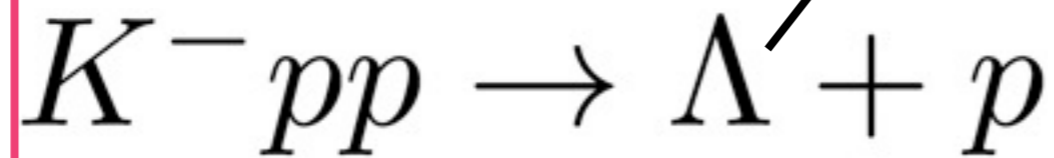
- ▶ $(K^-_{\text{stop}}, n \text{ or } p) \dots$ KEK-PS E471/E549, **FINUDA**
 - ▶ ${}^4\text{He}(K^-_{\text{stop}}, n)S^+(3140) \dots K^-ppn ?$
 - ▶ ${}^4\text{He}(K^-_{\text{stop}}, p)S^0(3115) \dots K^-pnn ?$
- ▶ $(K^-, n \text{ or } p) \dots$ BNL-AGS E930 / KEK-PS E548
 - ▶ ${}^{16}\text{O}(K^-, n){}^{15}\text{OK}^- \dots B_K = 130, 90, (50) \text{ MeV}$
- ▶ $(K^-, \pi^-), (\pi^+, K^+) \dots$ J-PARC

Detection Methods (2)

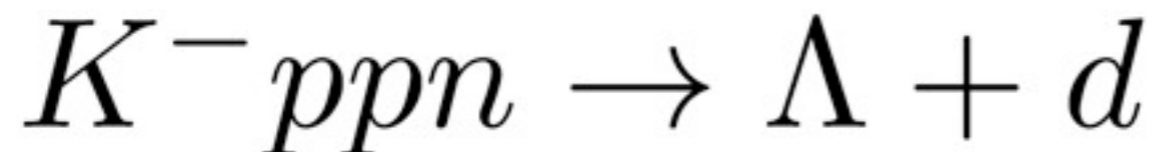
- ▶ **Invariant-mass spectroscopy**

- ▶ Heavy-ion collision ... GSI-FOPI

- ▶ K^- absorption at rest in a nucleus ... **FINUDA**

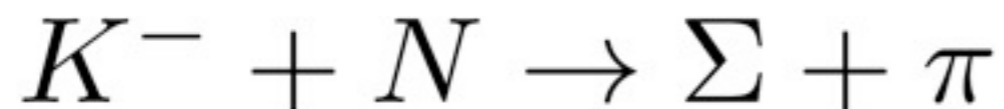


three final particles
to be detected

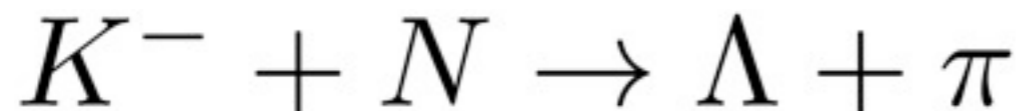


Decay Modes

► Mesonic decay



closed if the state is deep enough



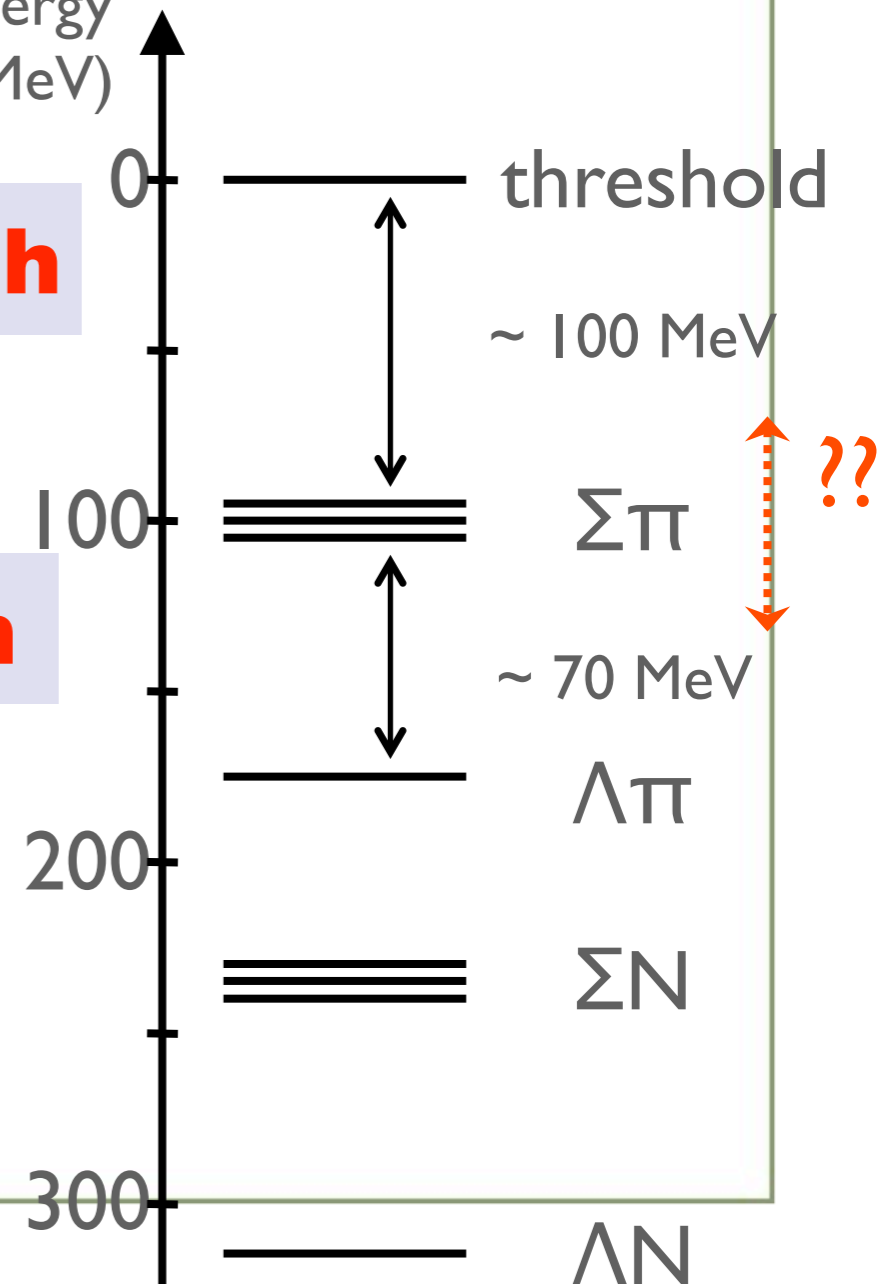
suppressed by the I=0 attraction

► Non-mesonic decay



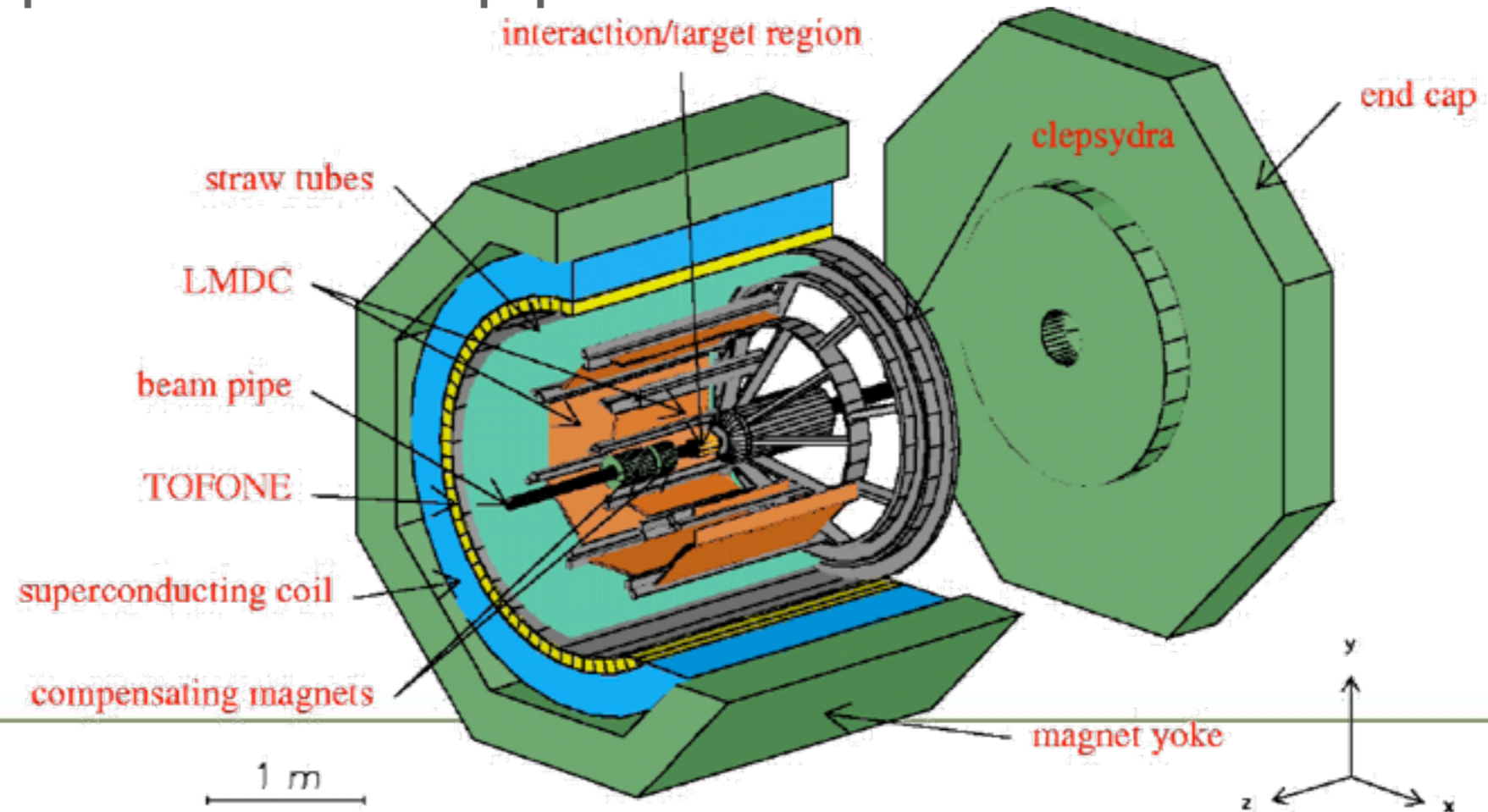
should exist

Binding
Energy
(MeV)



FINUDA experiment

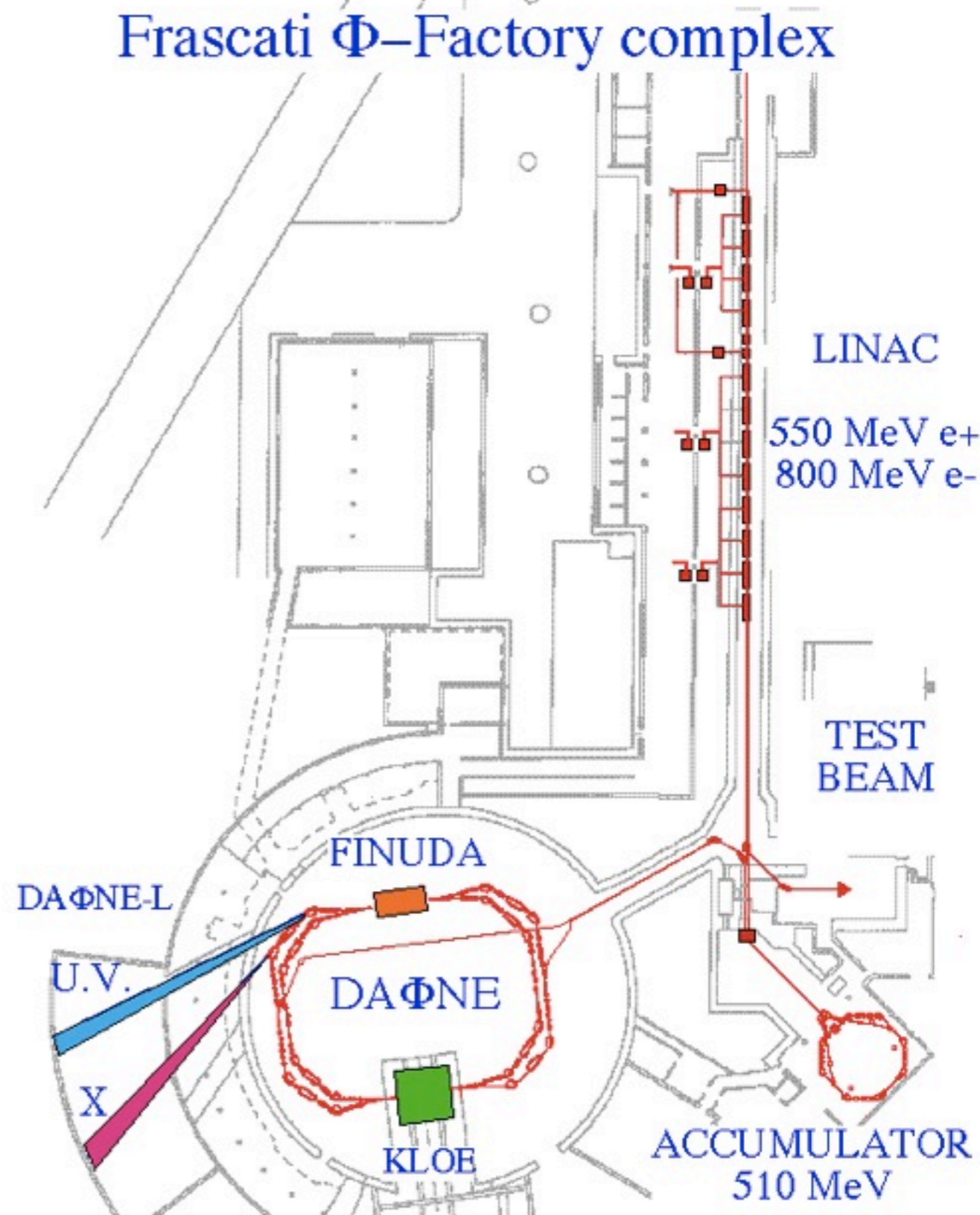
- ▶ Λ -hypernuclear spectroscopy
with the $(K^-_{\text{stop}}, \pi^-)$ reaction
- ▶ $B=1.0\text{T}$, acceptance $\sim 70\%$, $\Delta p/p \sim 0.35\%$



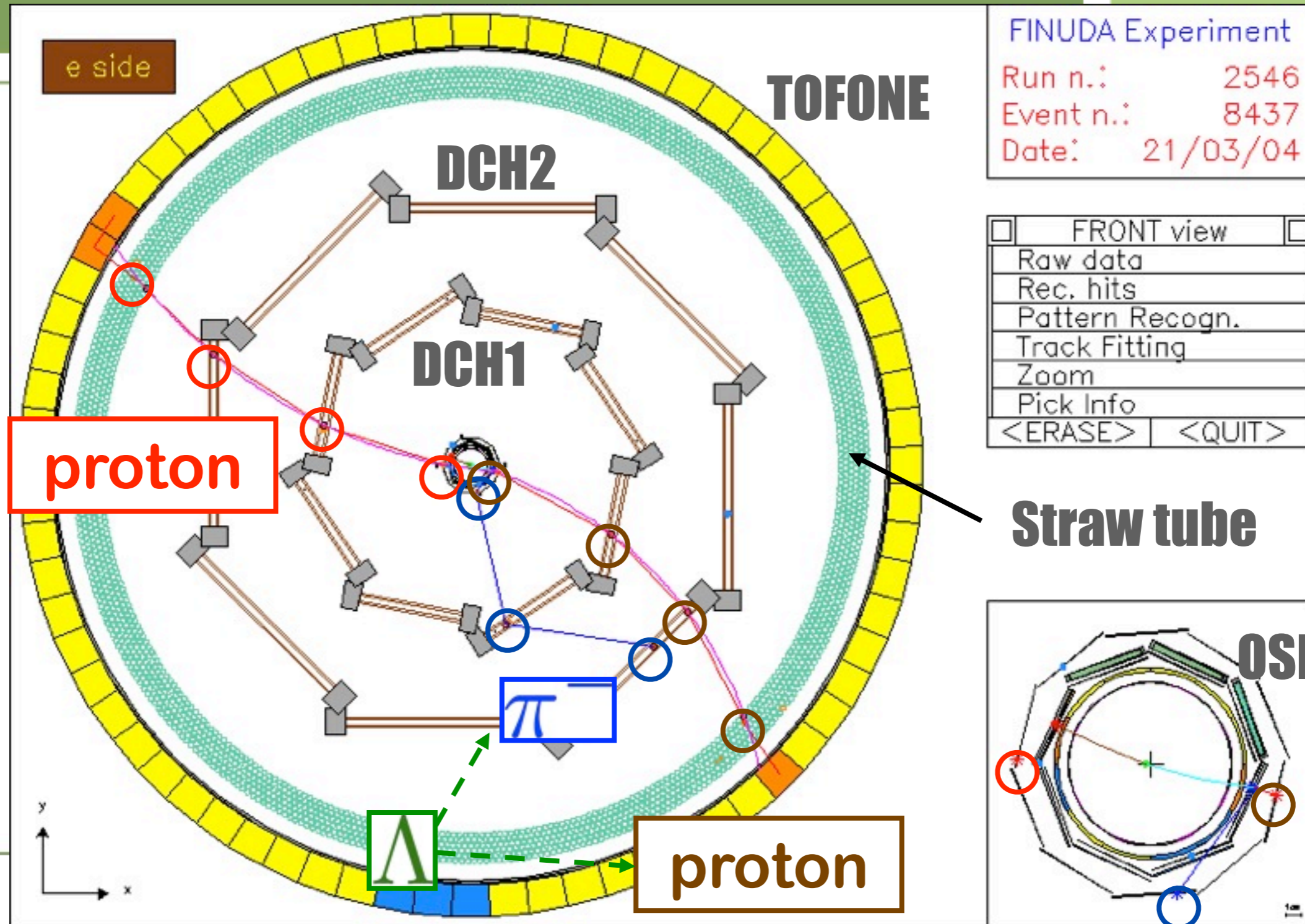
DAΦNE ϕ -factory

- ▶ Beam energy 510 MeV
- ▶ Luminosity $< 5 \times 10^{32}/\text{cm}^2/\text{s}$
 - ▶ ($10^{32}/\text{cm}^2/\text{s} = 216 \text{ K}^\pm/\text{s}$)
- ▶ Crossing angle 12.5 mrad

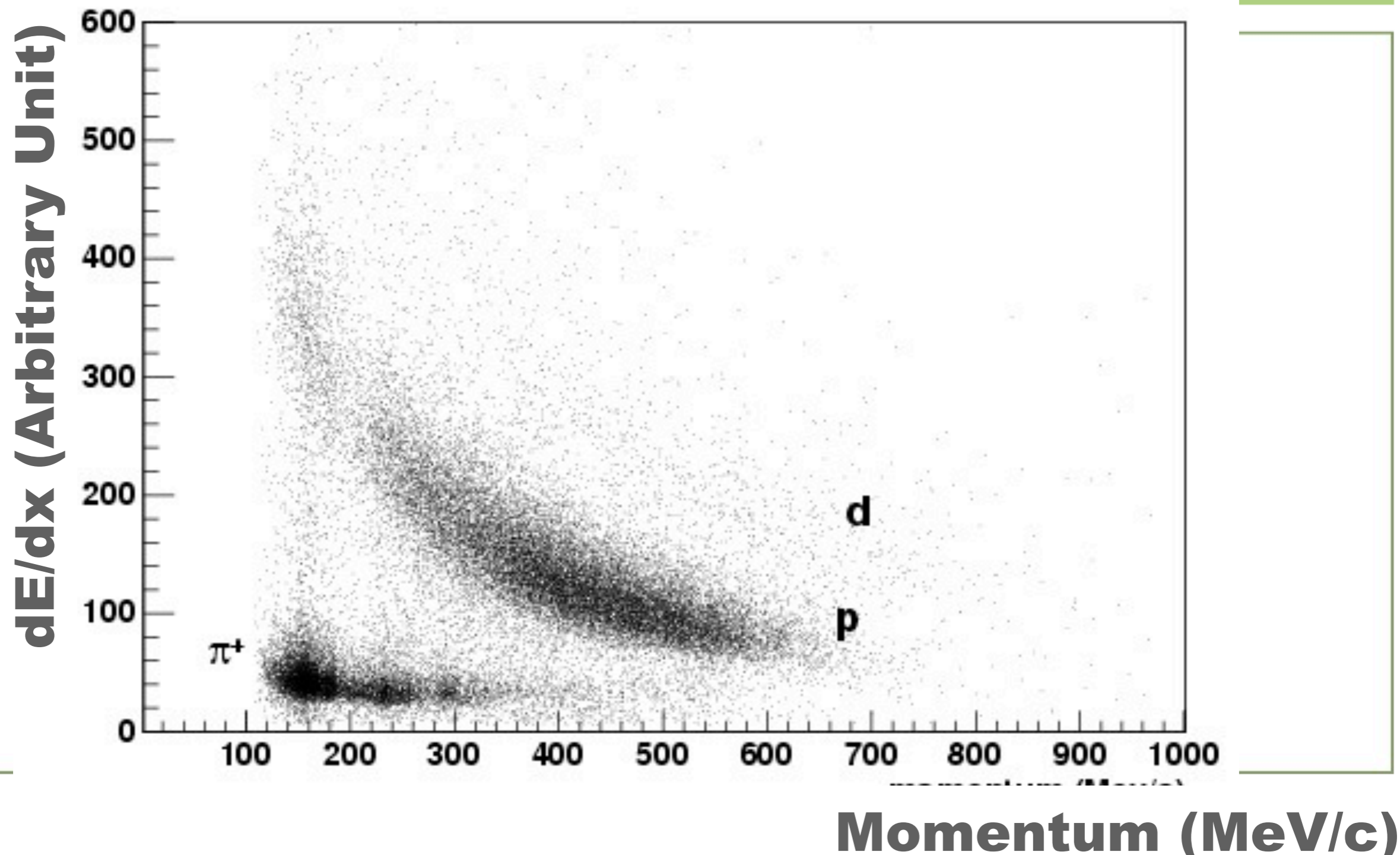
$$e^+e^- \rightarrow \phi(1020) \rightarrow K^+K^- \quad (T_K=16 \text{ MeV})$$



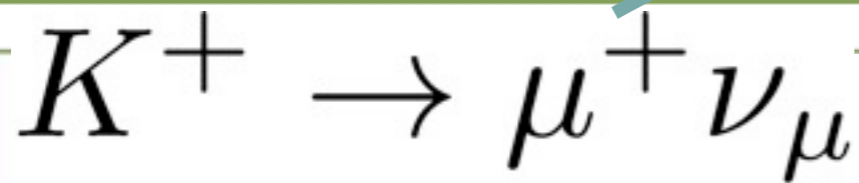
Event display ($K^-pp \rightarrow \Lambda + p$)



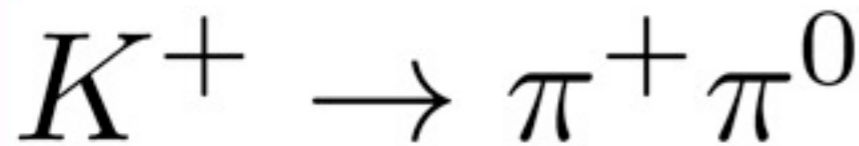
PID by dE/dx in OSIM



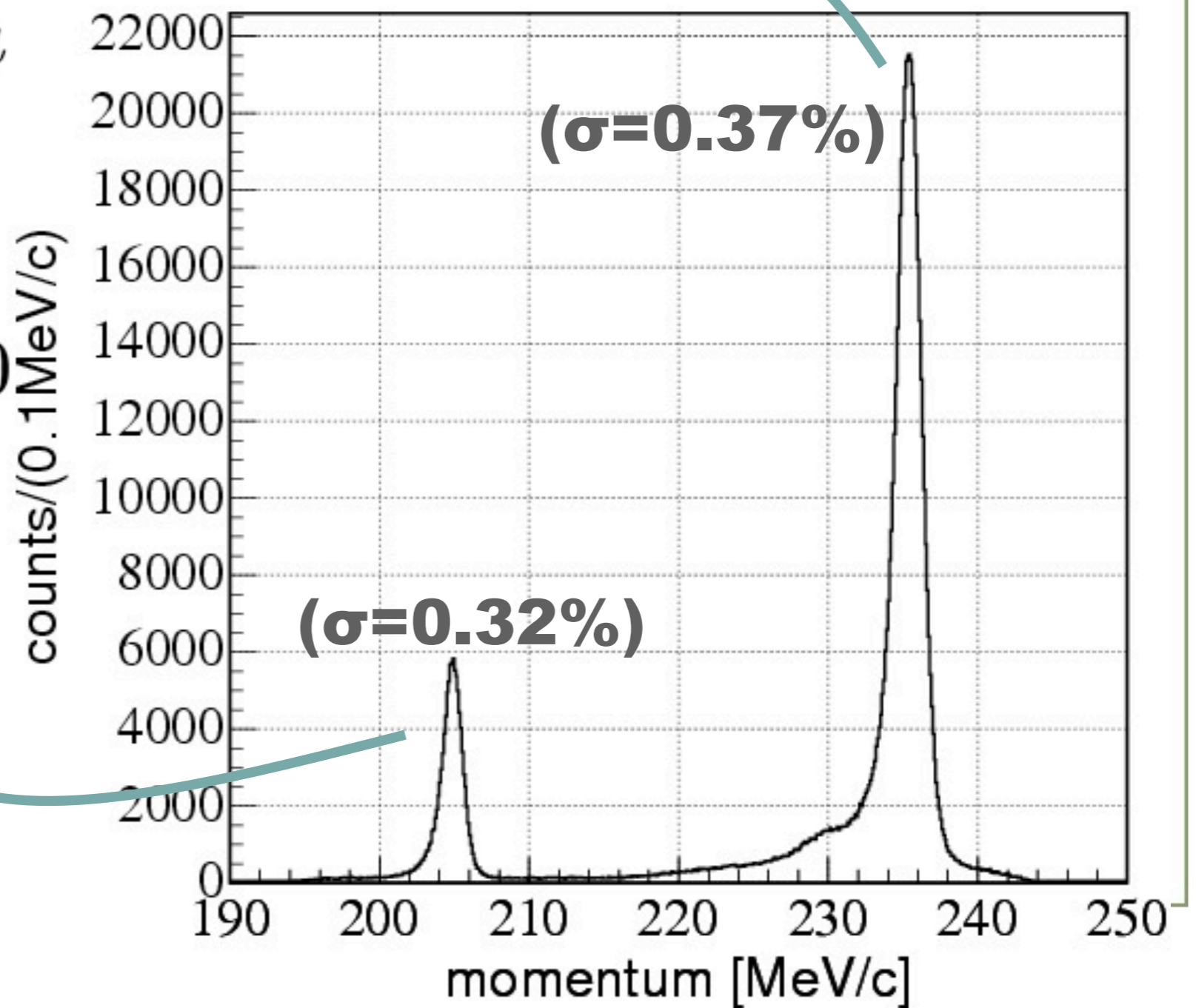
Momentum calibration



b.r. 63.4%
236 MeV/c

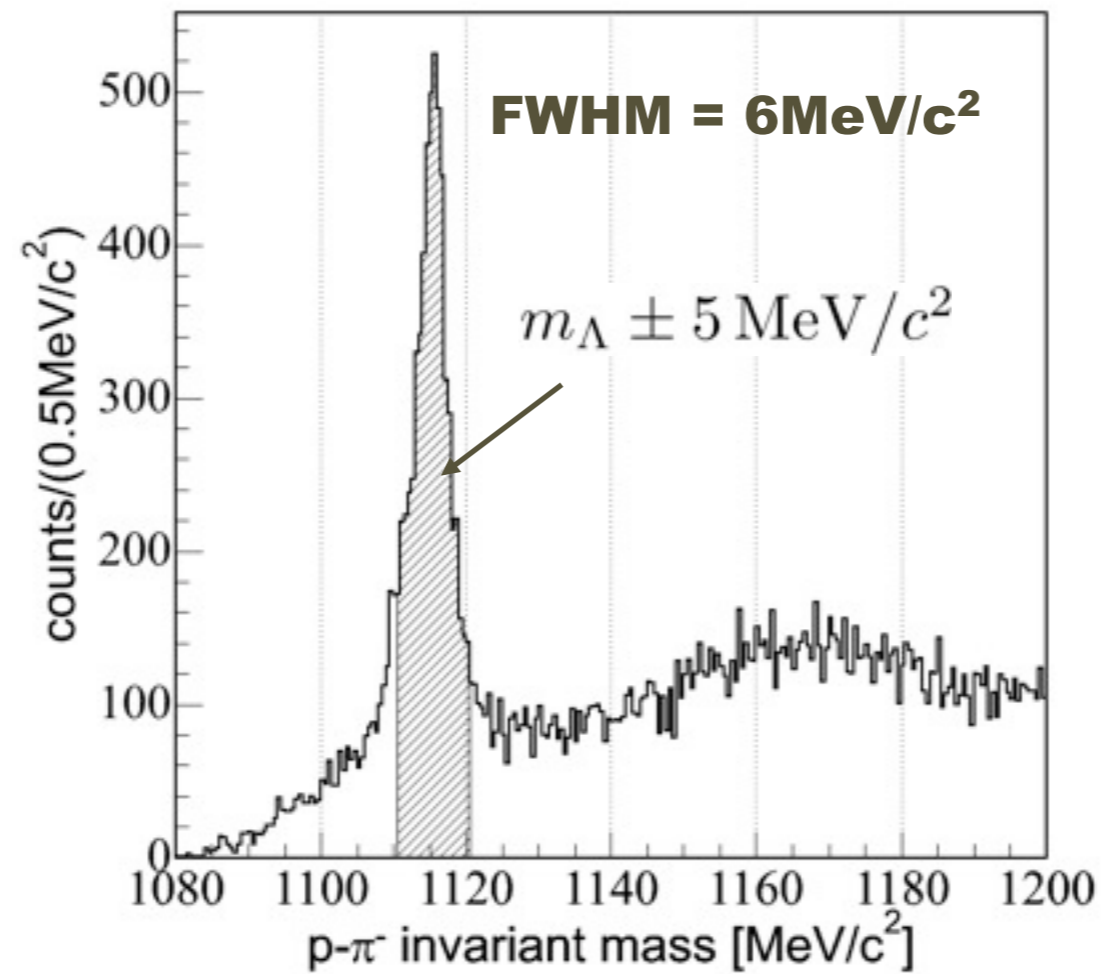


b.r. 21.1%
205 MeV/c



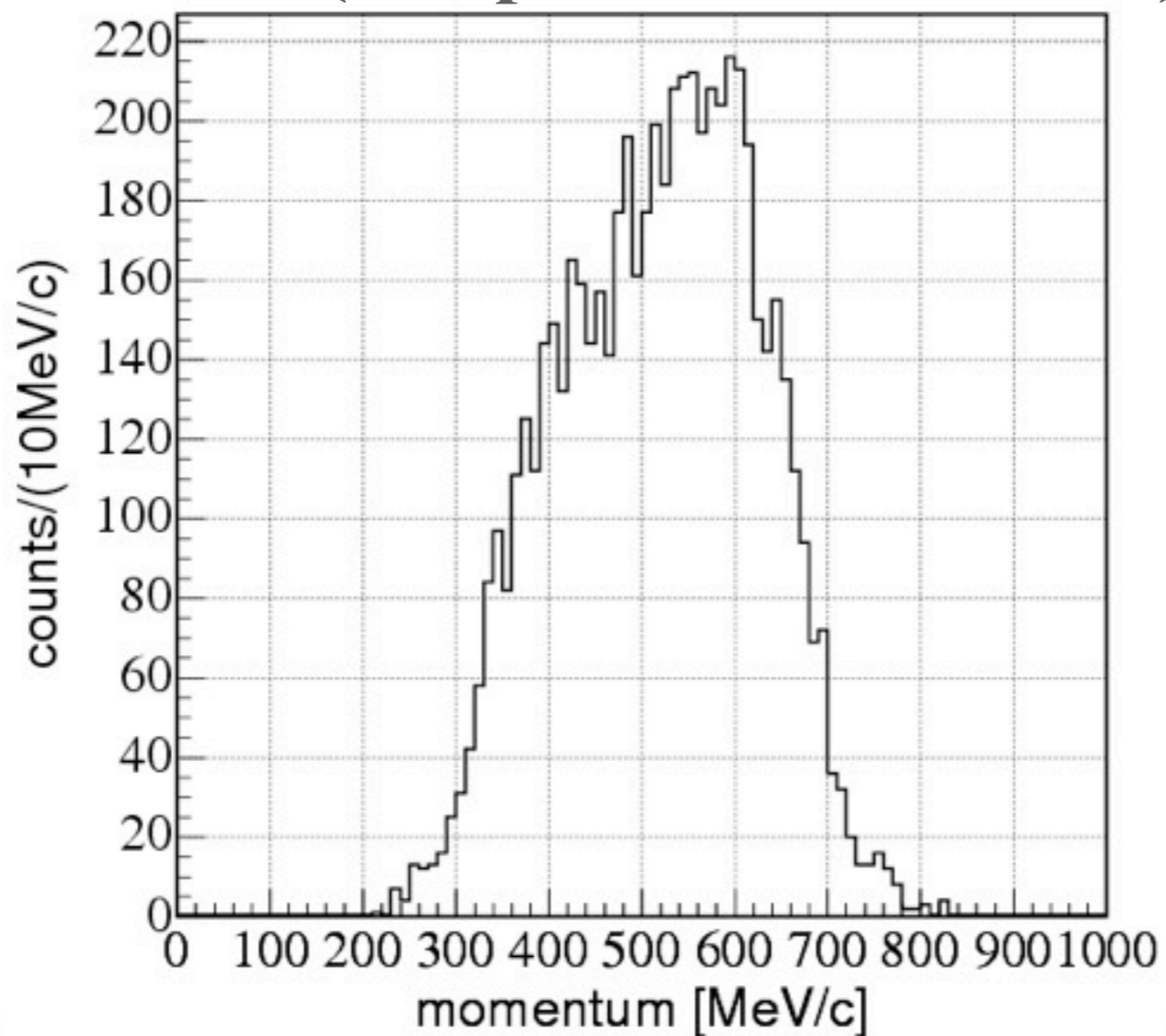
Detection of a Λ hyperon

Invariant mass of a proton and a π^-



Λ momentum distribution

(acceptance uncorrected)



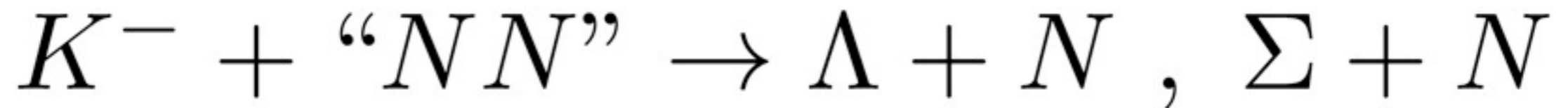
Λ in Kaon absorption

- ▶ **quasi-free process (80–85%)**



$$p_\Lambda \lesssim 400 \text{ MeV}/c$$

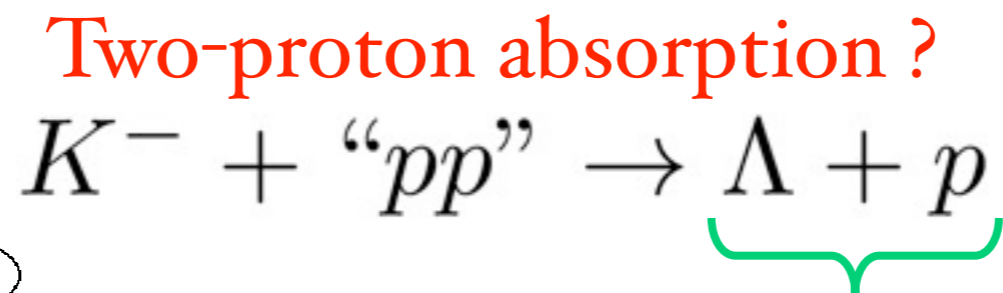
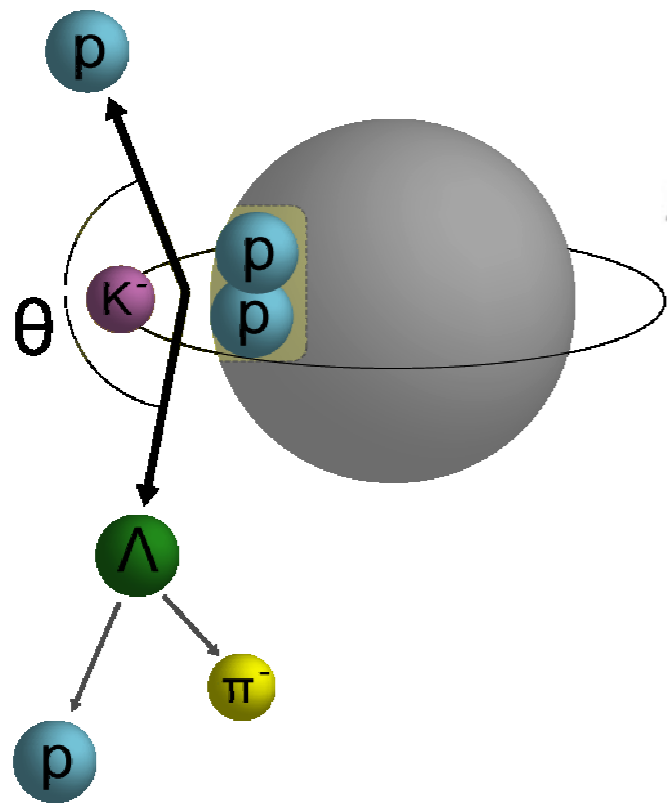
- ▶ **two-nucleon absorption (15–20%)**



$$p_\Lambda: 400 - 700 \text{ MeV}/c$$

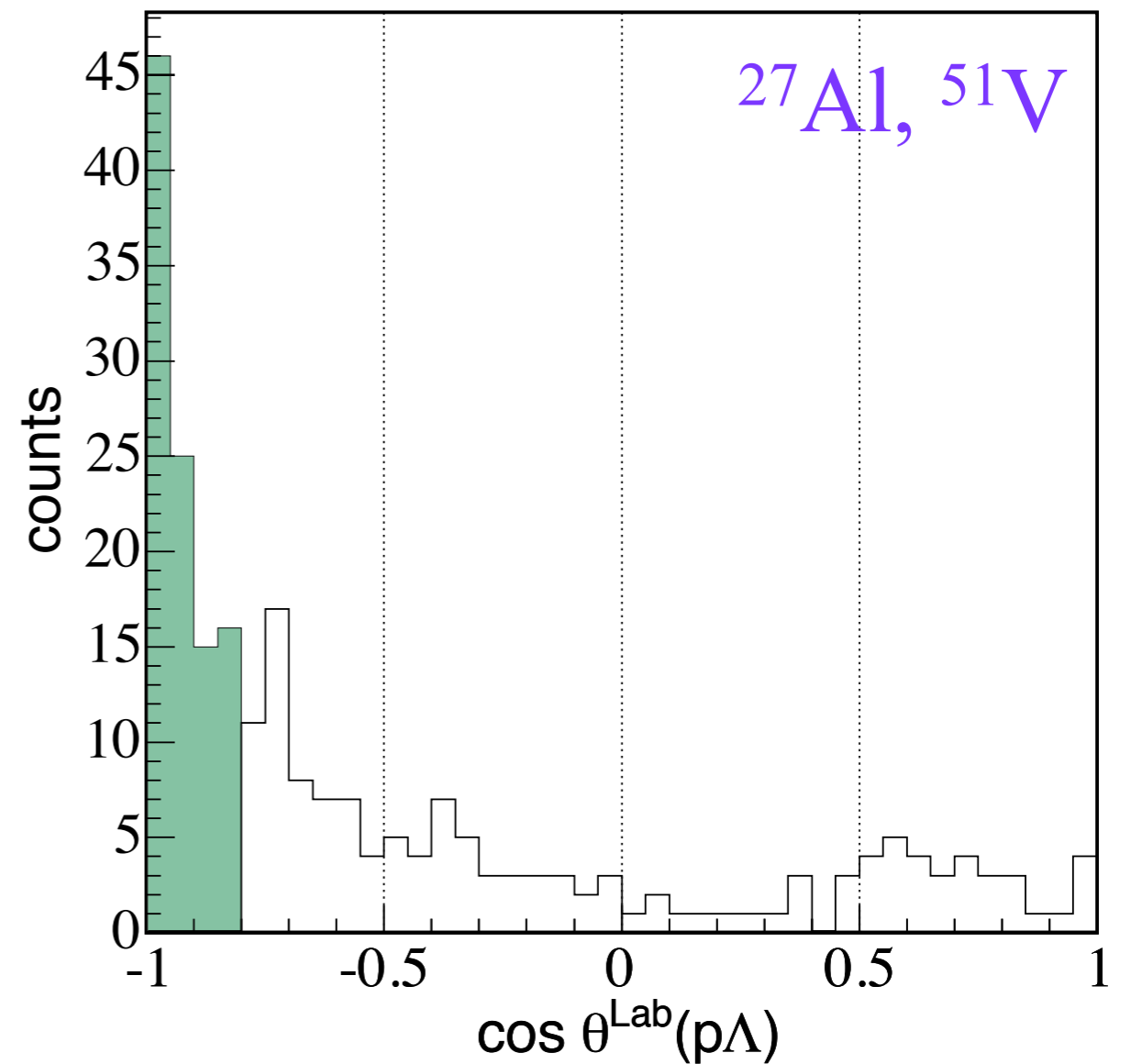
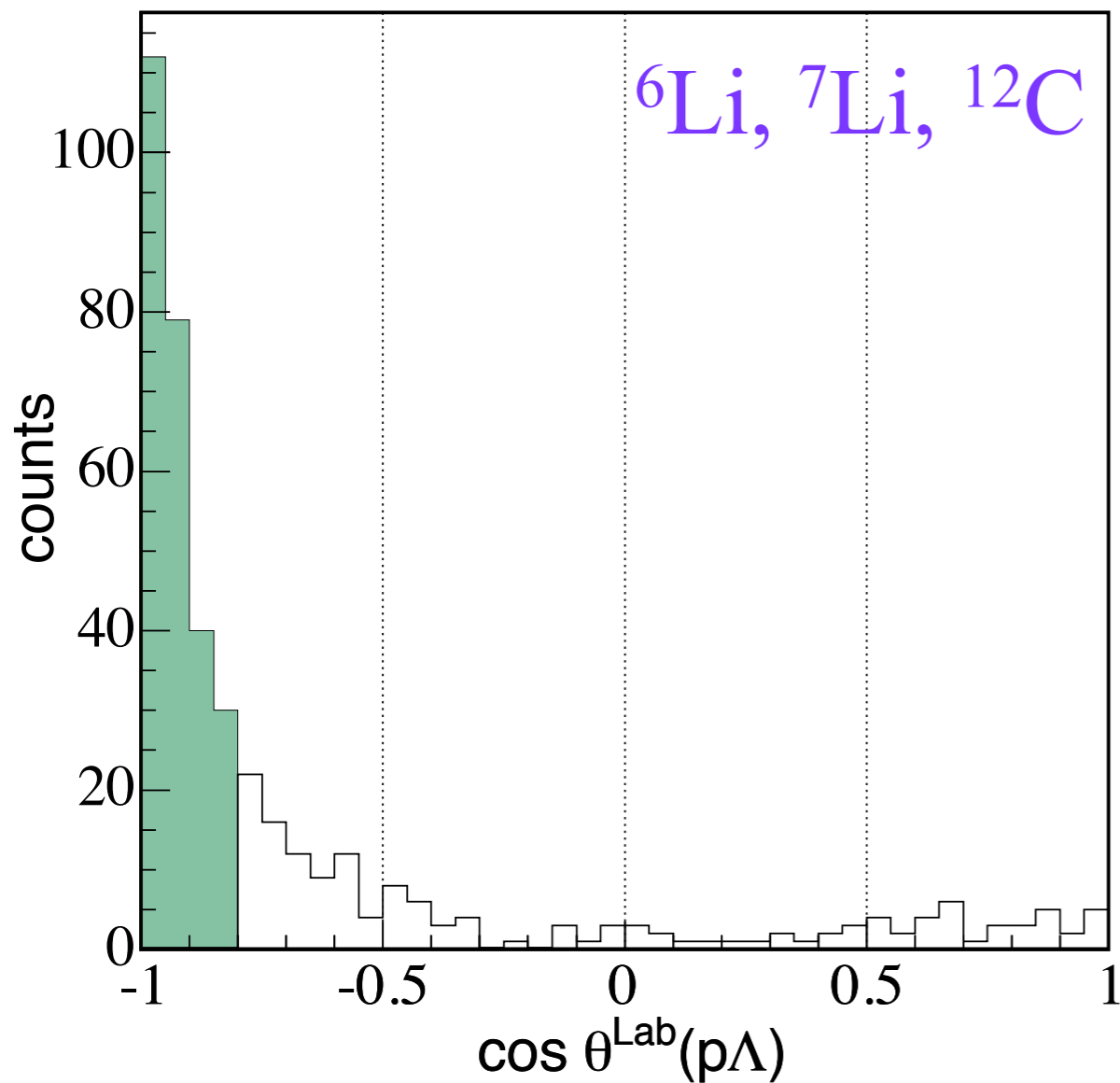
Λ -p coincidence events

- About 5% of the Λ events are associated with a proton.



Back-to-back correlation
is expected.

Angular correlation of Λ -p



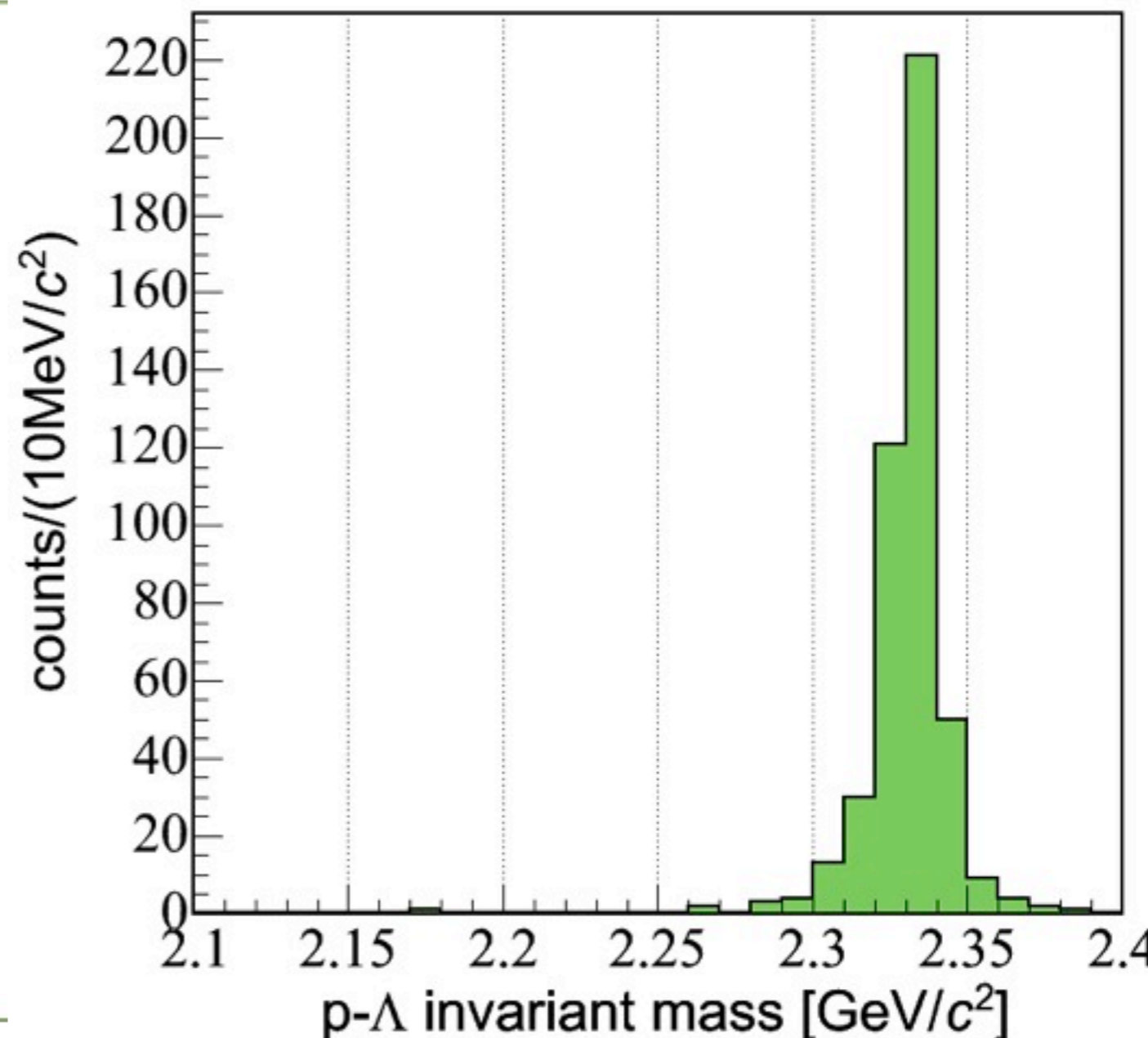
Naive expectation of invariant mass distribution

- ▶ Peak around

$$m_{K^-} + 2m_p = 2.37 \text{ GeV}/c^2$$

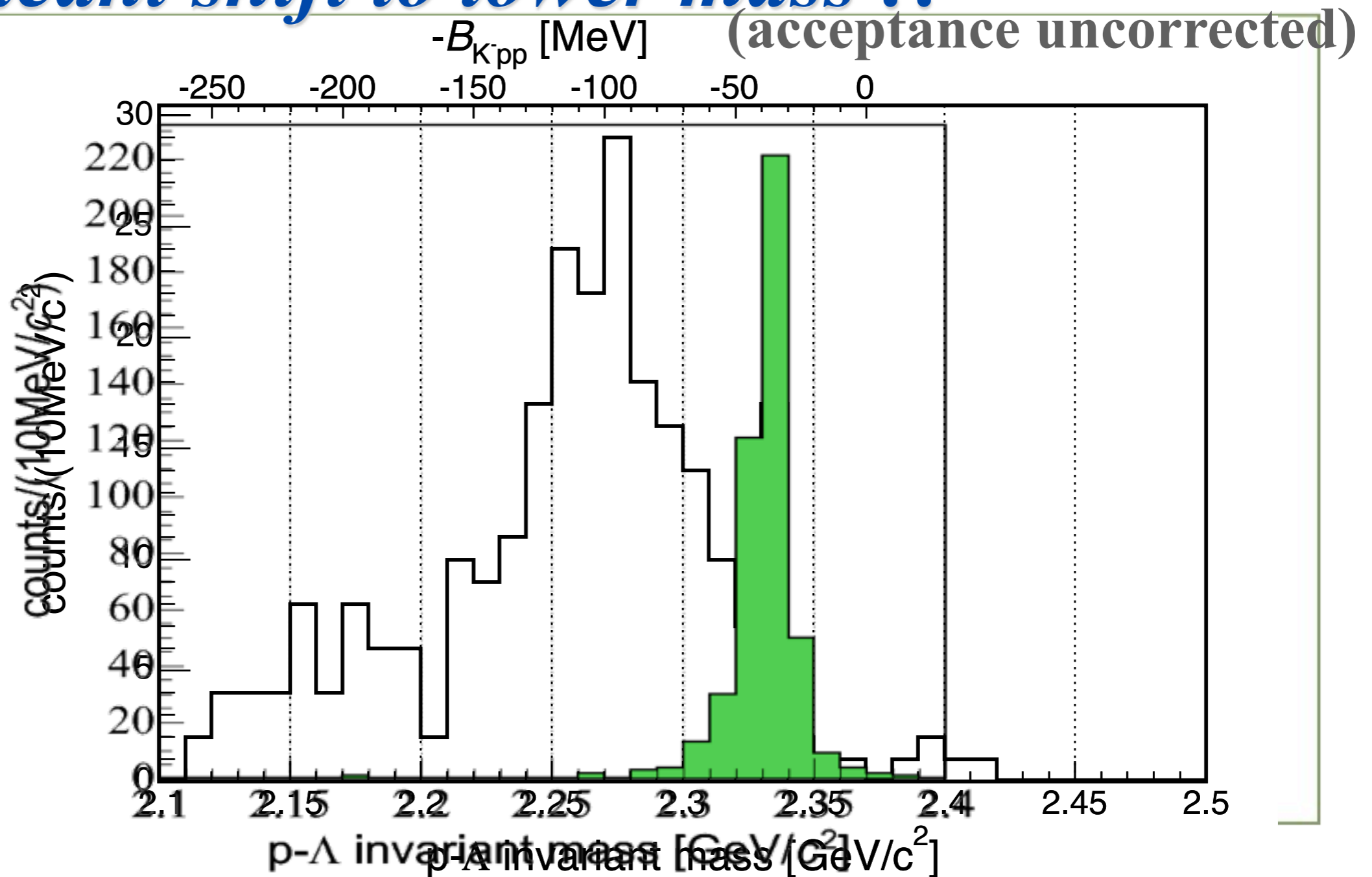
- ▶ Shift due to

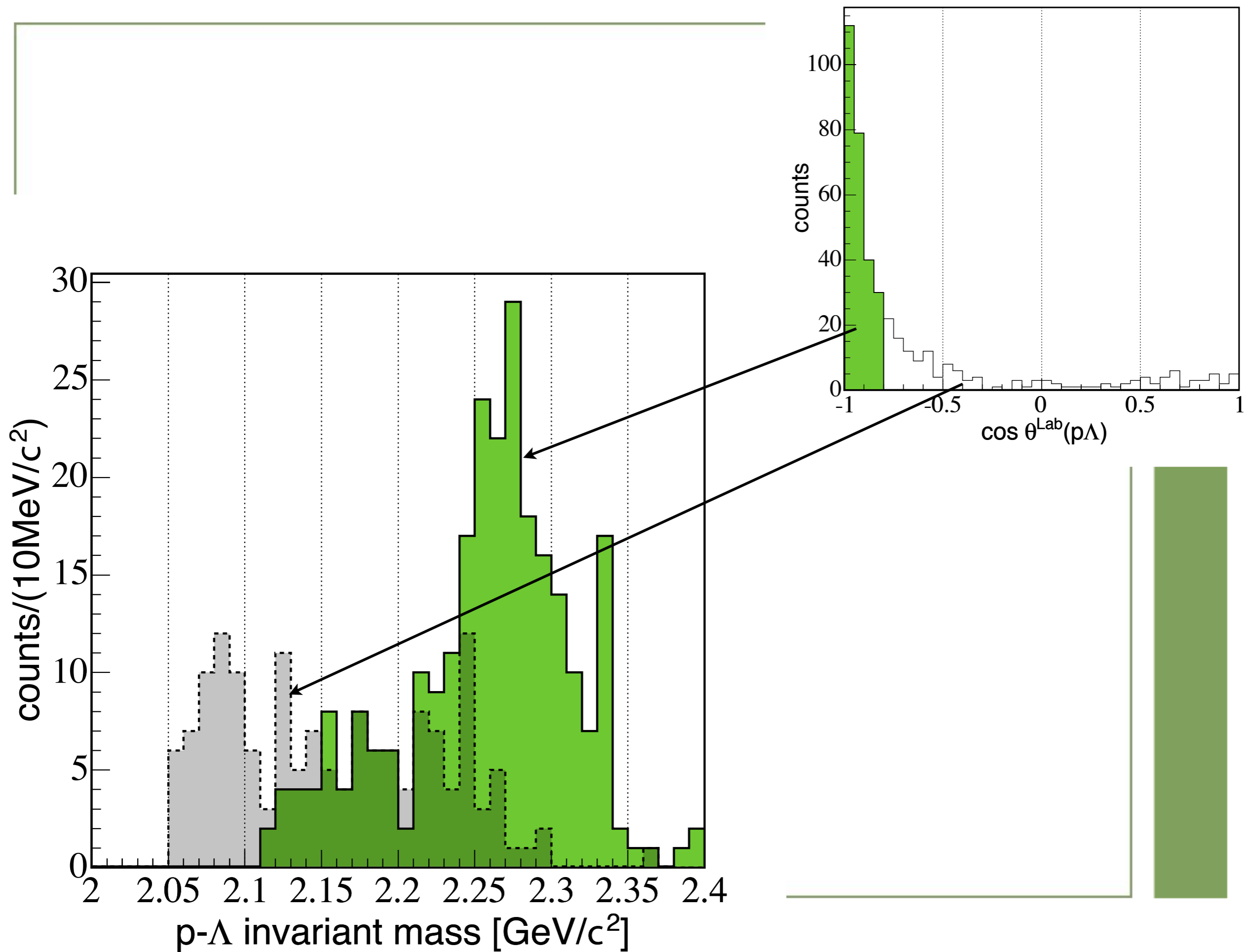
- ▶ separation energy of two protons
- ▶ kinetic energy of the system



Invariant-mass distribution

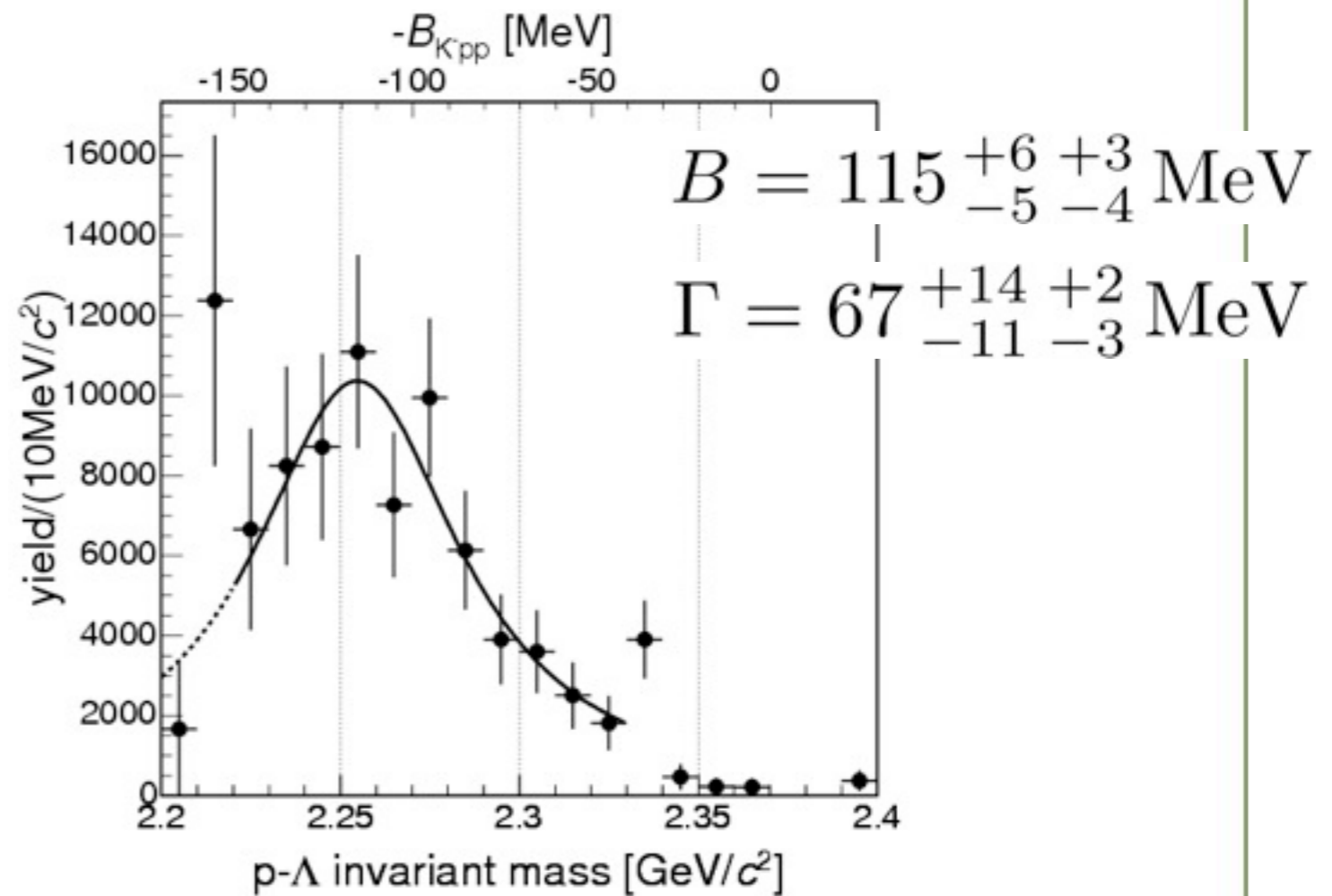
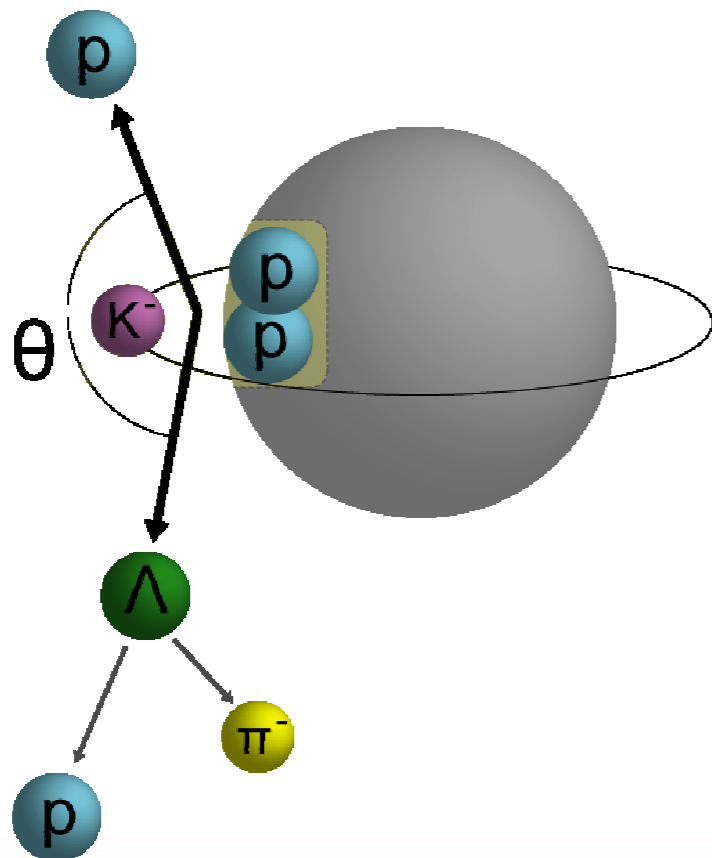
Significant shift to lower mass !!





Evidence for K^-pp in FINUDA

K^- Absorption on ${}^6,7\text{Li}$, ${}^{12}\text{C}$
Back-to-back $\Lambda + p$ pair



M. Agnello et al., PRL 94(2005) 212303.

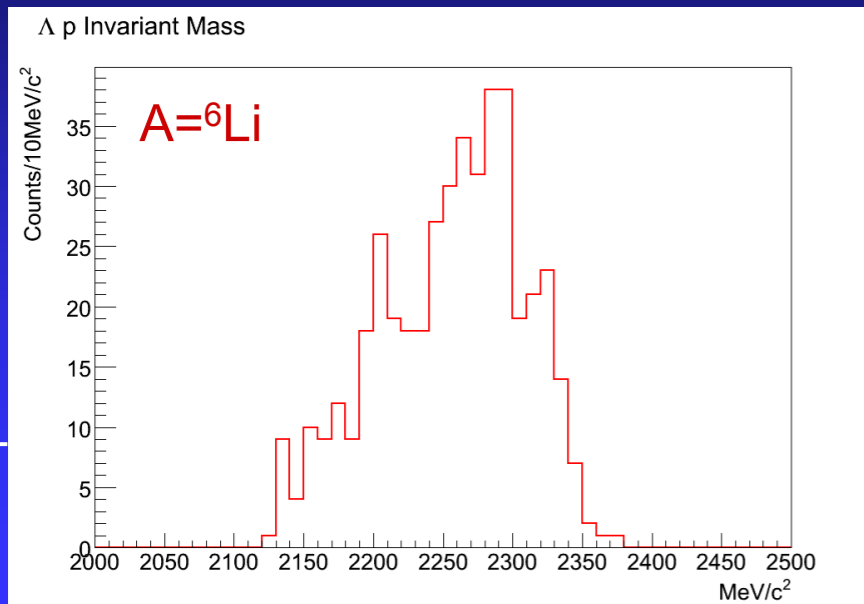
Few-body calculations on K^-pp

- K^-pp does exist !!
... but maybe broad.

(MeV)	ATMS Yamazaki & Akaishi, PLB535 (2002) 70.	Variational Dote, Hyodo, Weise, PRC79 (2009) 014003.	Faddeev Shevchenko, Gal, Mares, PRL98 (2007) 082301.	Faddeev Ikeda & Sato, PRC79 (2009) 035201.	Variational Wycech & Green, PRC79 (2009) 014001.
B	48	17-23	50-70	60-95	40-80
Γ	61	40-70	90-110	45-80	40-85

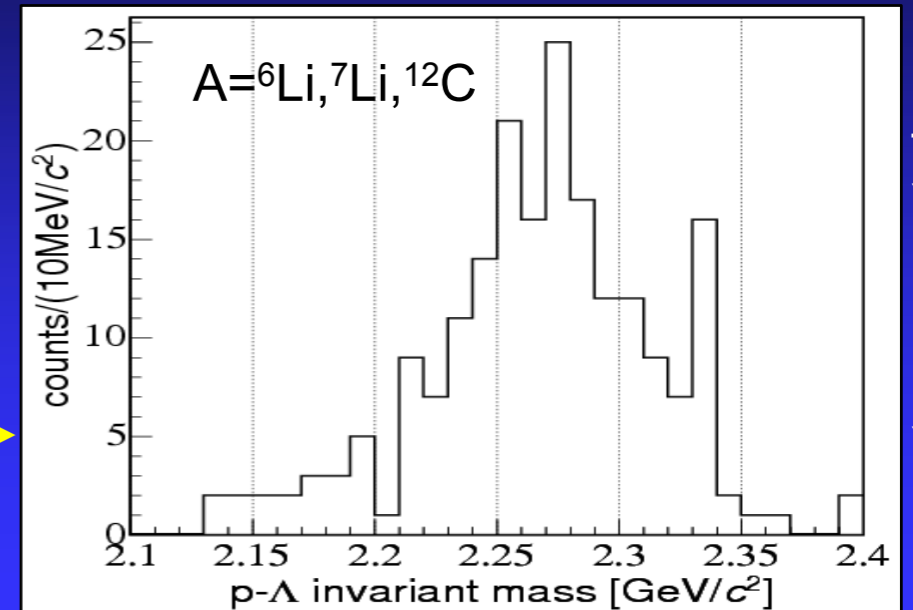
New FINUDA data

- K^-pp confirmed for ${}^6\text{Li}$ only, with better statistics



New
inv mass spectra
compatible with
published one

New data ← Old data
Same cuts applied



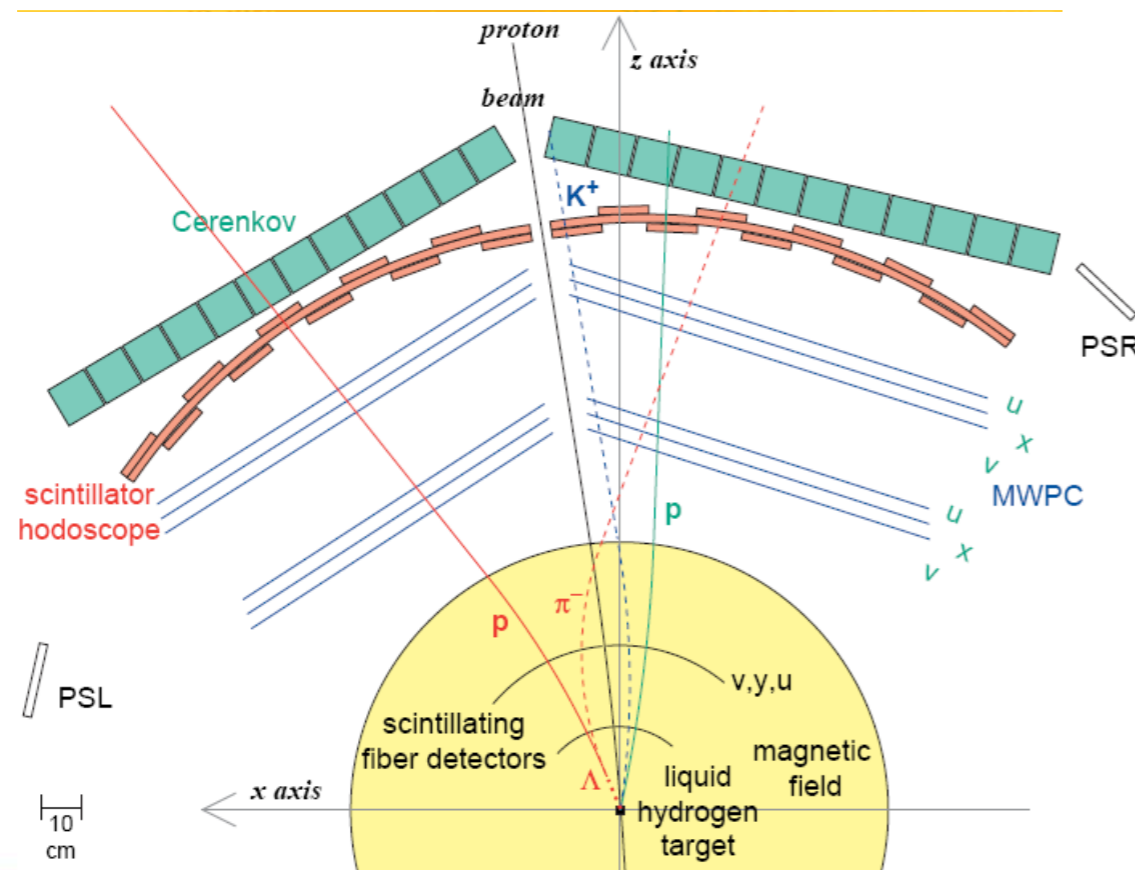
FINUDA Coll., PRL 94(2005)212303

no acceptance corrected

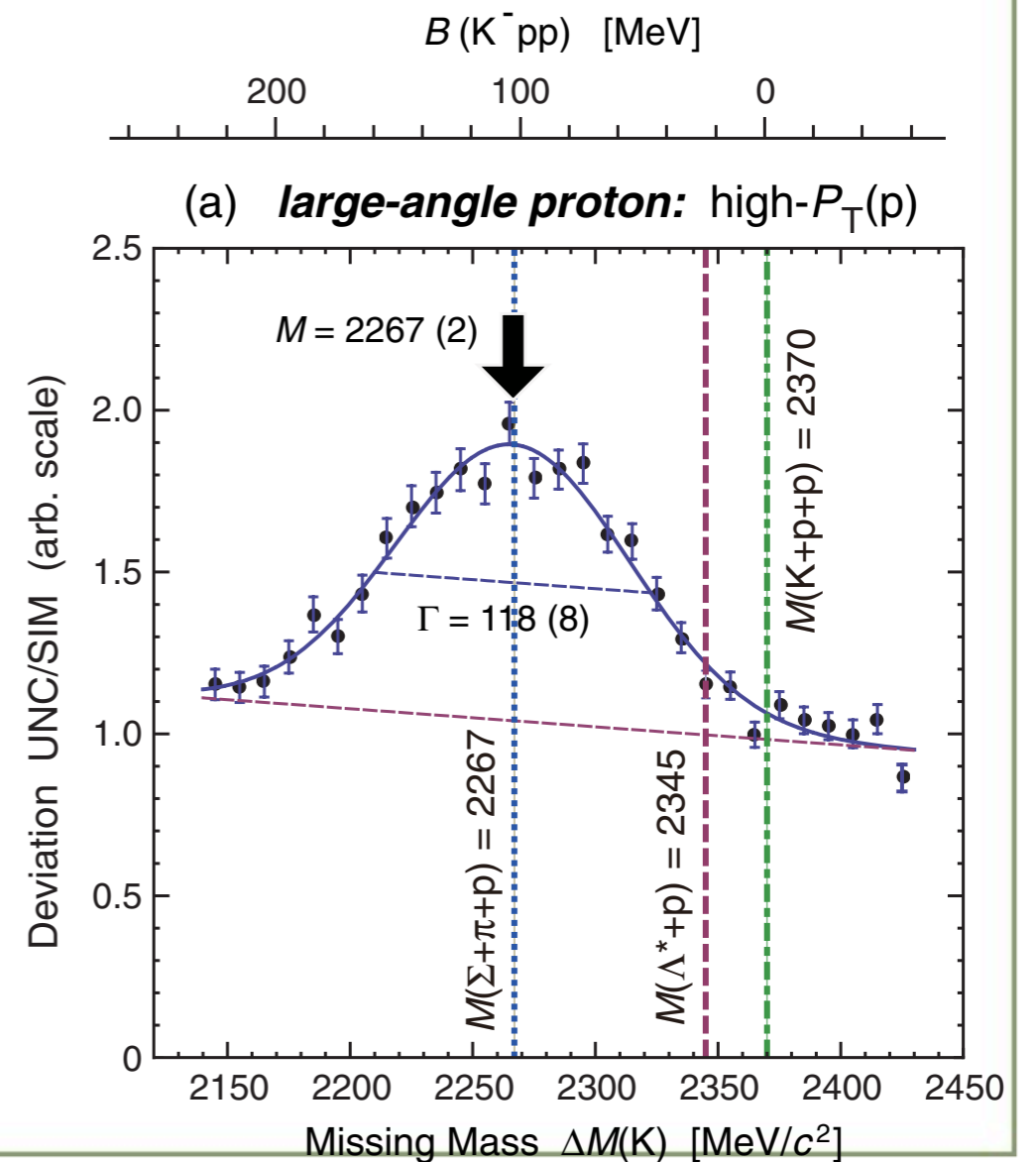
no acceptance corrected

DISTO data on K^-pp

- ▶ $p+p \rightarrow K^-pp + K^+$ at 2.85 GeV
 - ▶ $M = 2267 \pm 3 \pm 5 \text{ MeV}/c^2$
 - ▶ $\Gamma = 118 \pm 8 \pm 10 \text{ MeV}$



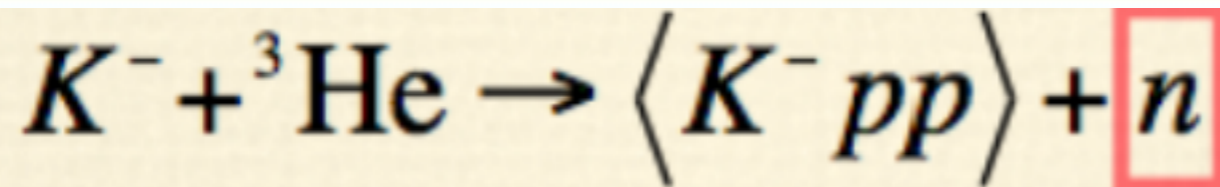
T. Yamazaki et al., PRL 104 (2010) 132502.



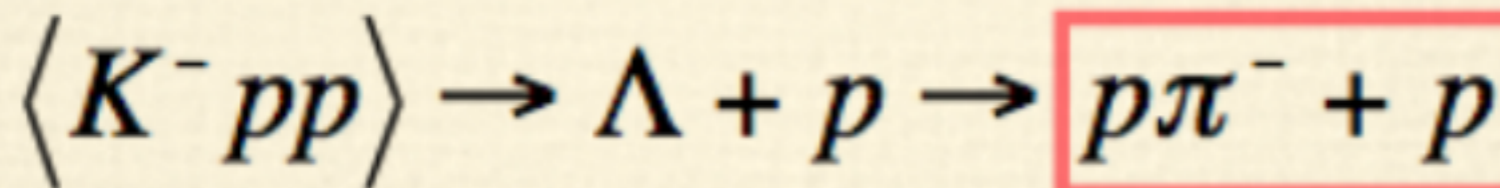
A Search for deeply-bound kaonic nuclear states by in-flight ${}^3\text{He}(K^-,n)$ reaction

E15

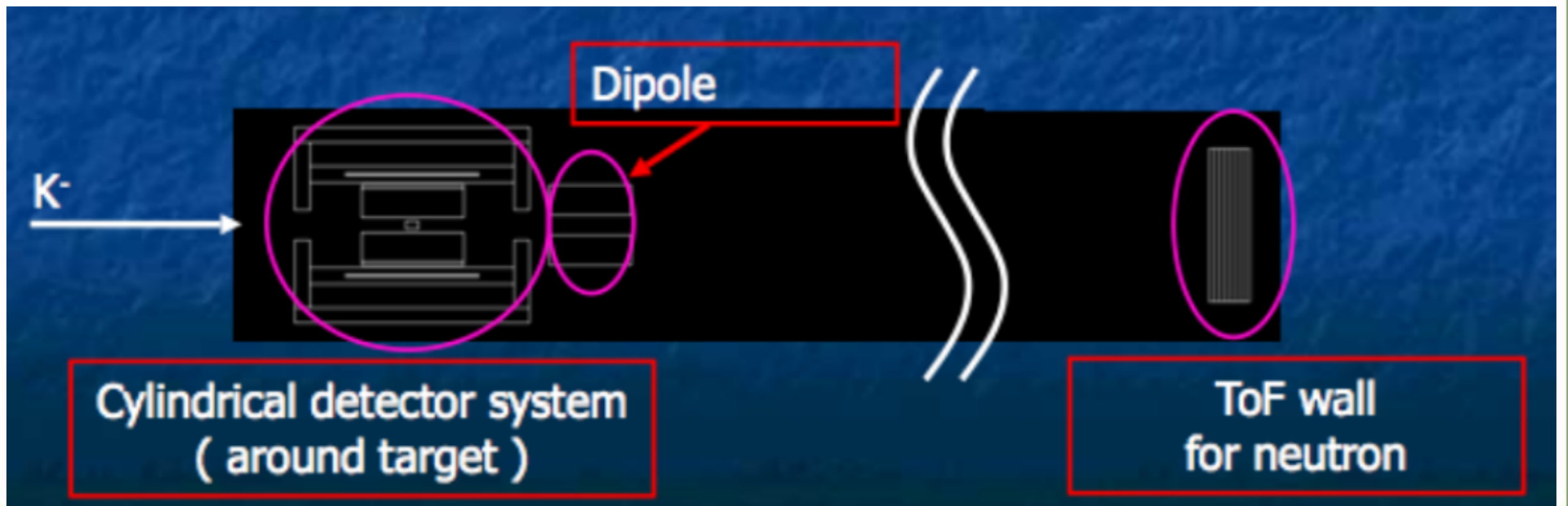
M. Iwasaki et al.



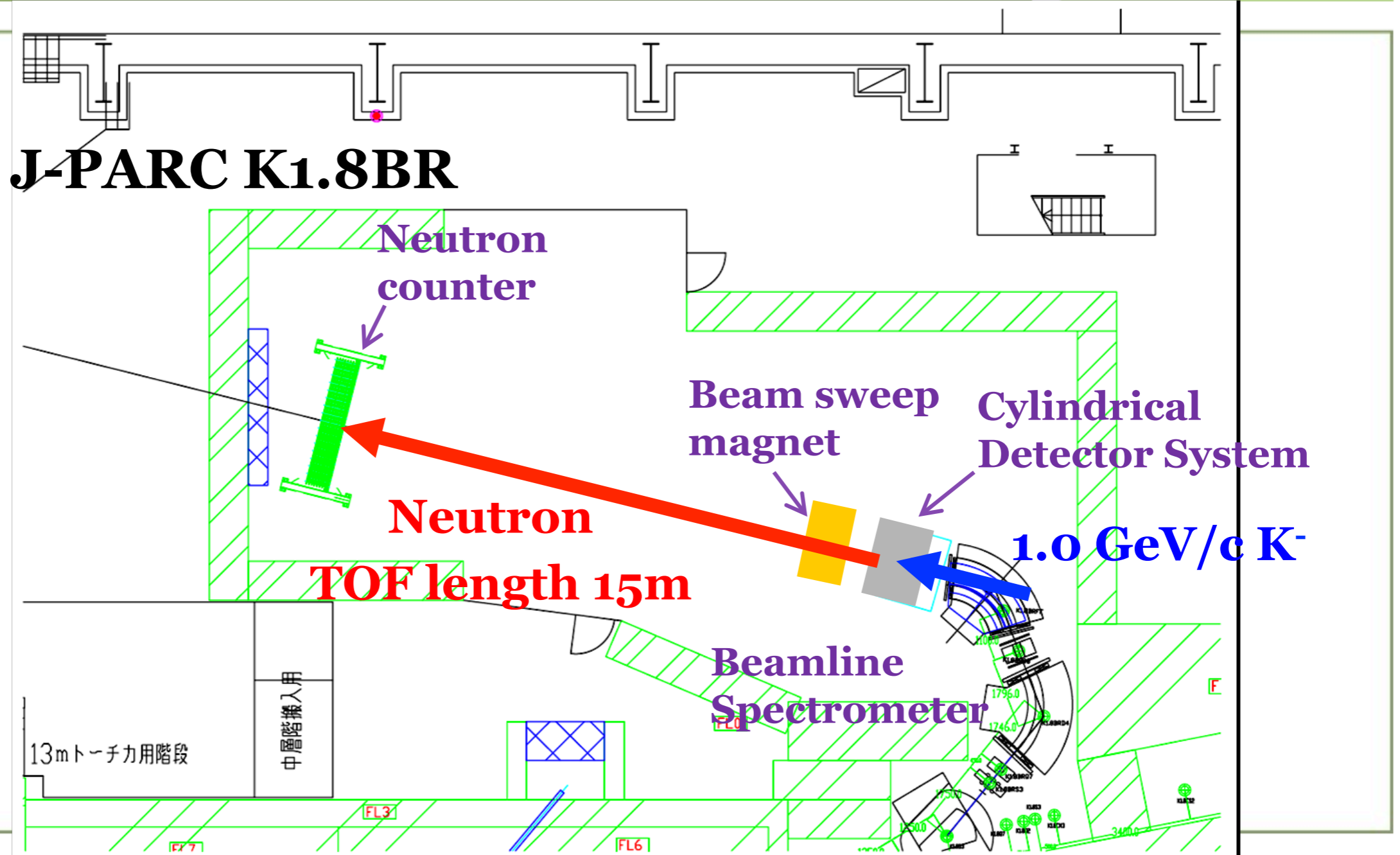
TOF



CDC

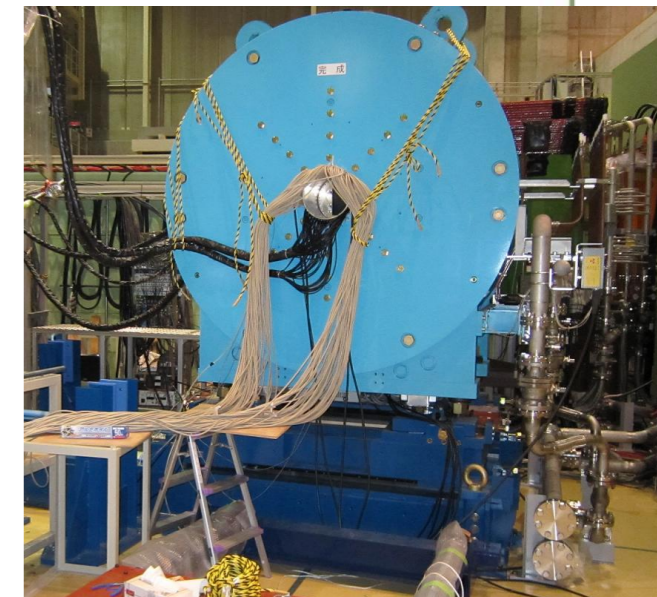
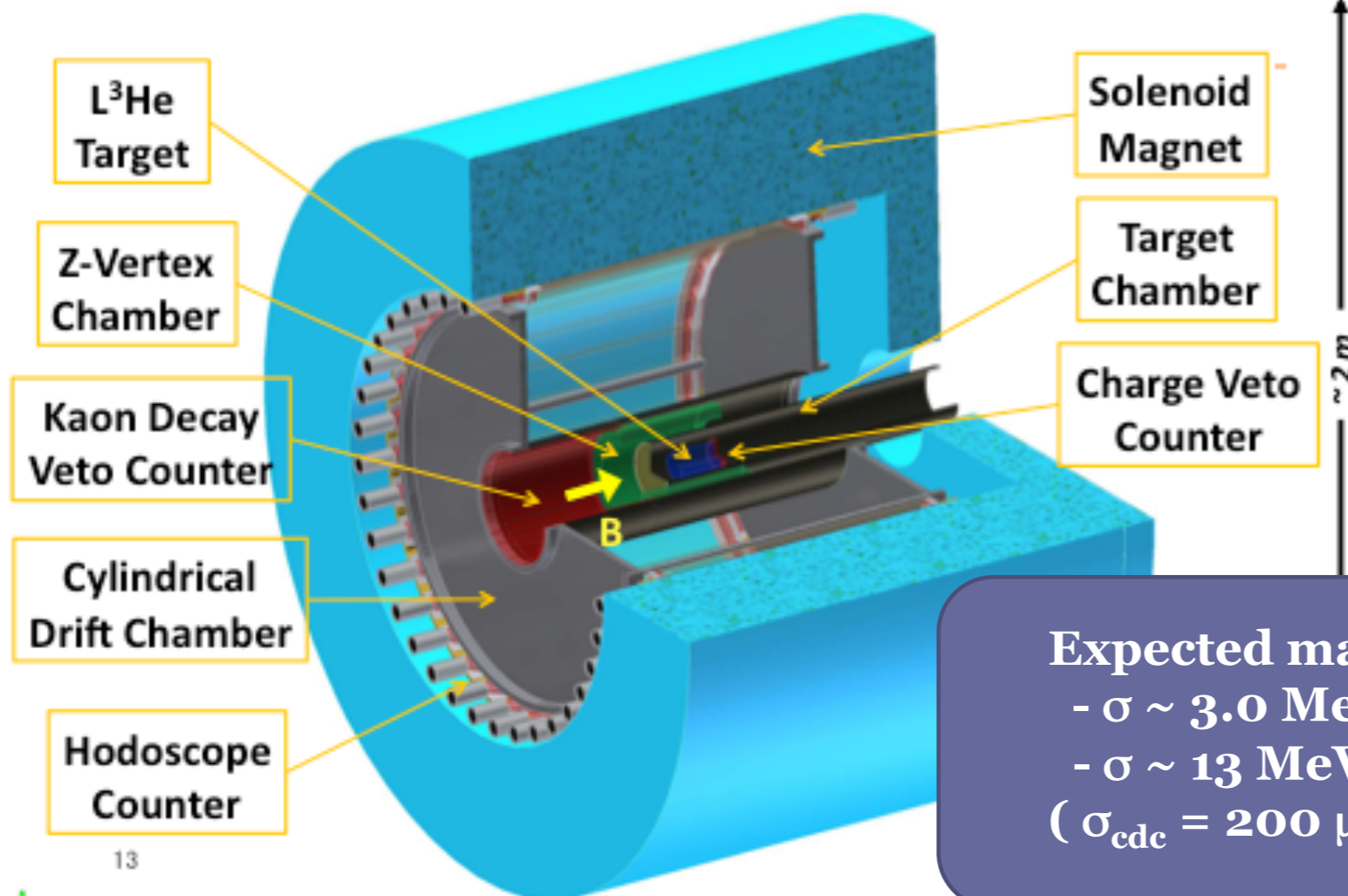


Experimental Setup



Cylindrical Detector System

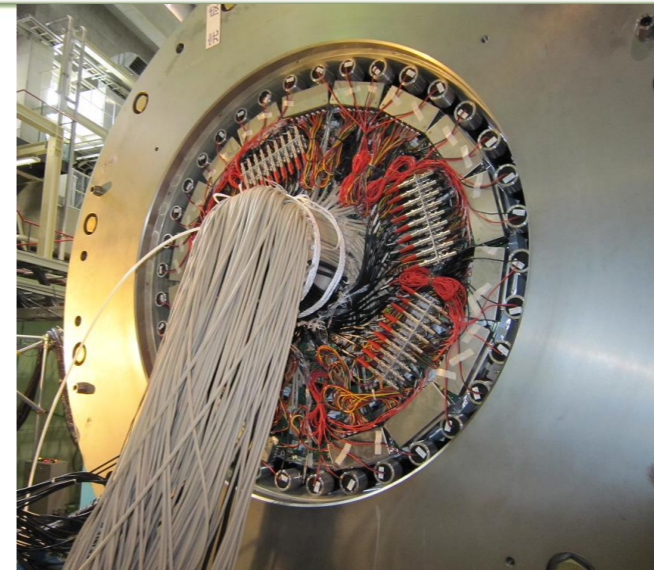
- **A newly developed system for invariant mass study**



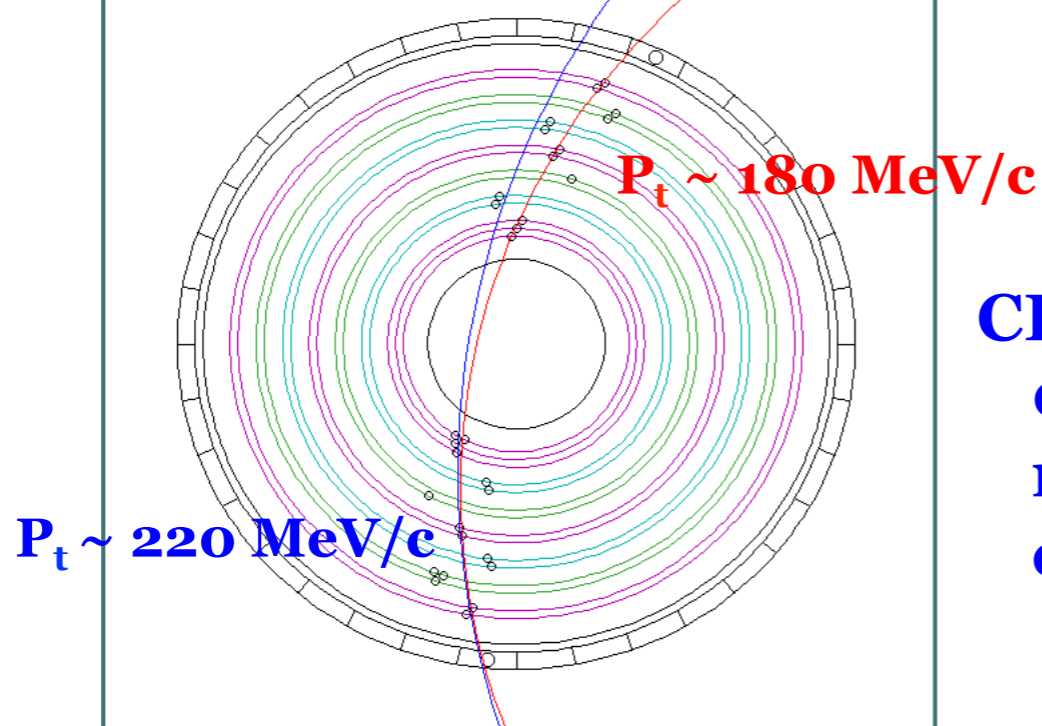
Expected mass resolution :
- $\sigma \sim 3.0 \text{ MeV}/c^2$ for Λ
- $\sigma \sim 13 \text{ MeV}/c^2$ for K^-pp
($\sigma_{cdc} = 200 \mu\text{m} / \text{Field} : 0.5 \text{ T}$)

Status of CDS

- All of the components(CDC, CDH) have been installed into the solenoid magnet.

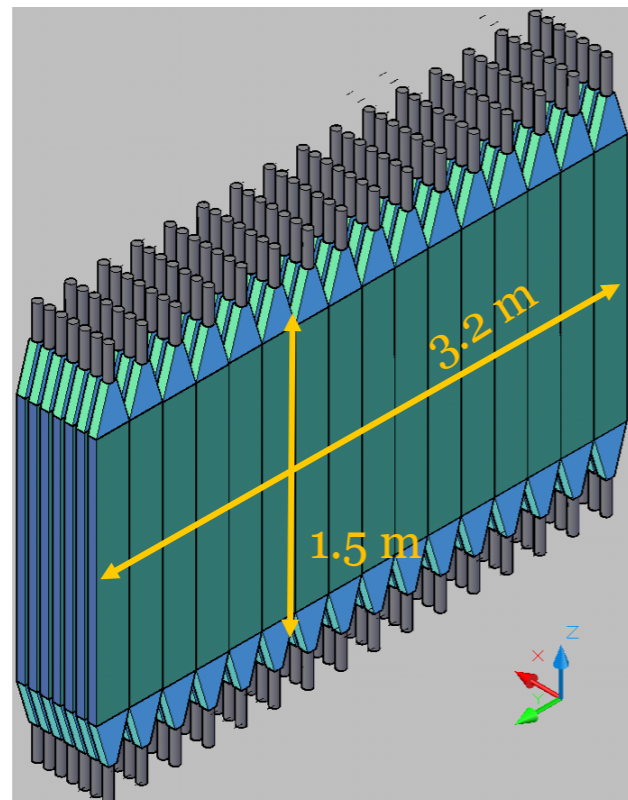


Typical Event Display

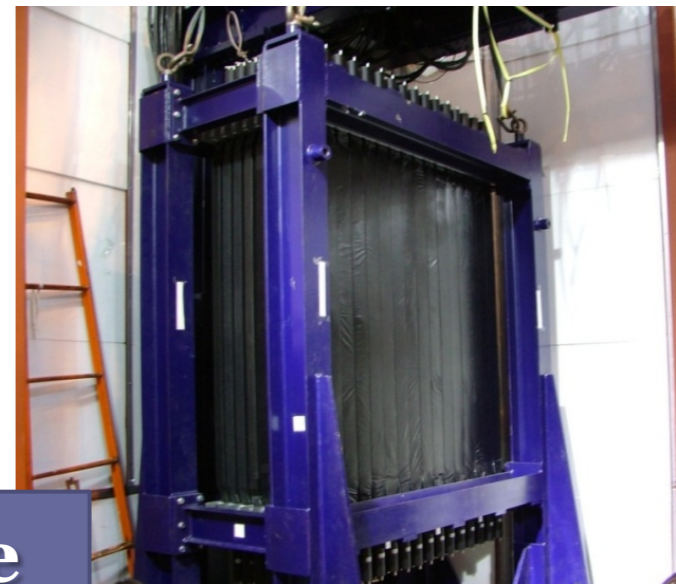


CDS commissioning with 0.5 T magnetic field is now under way using cosmic ray.

Neutron counter



rearrange



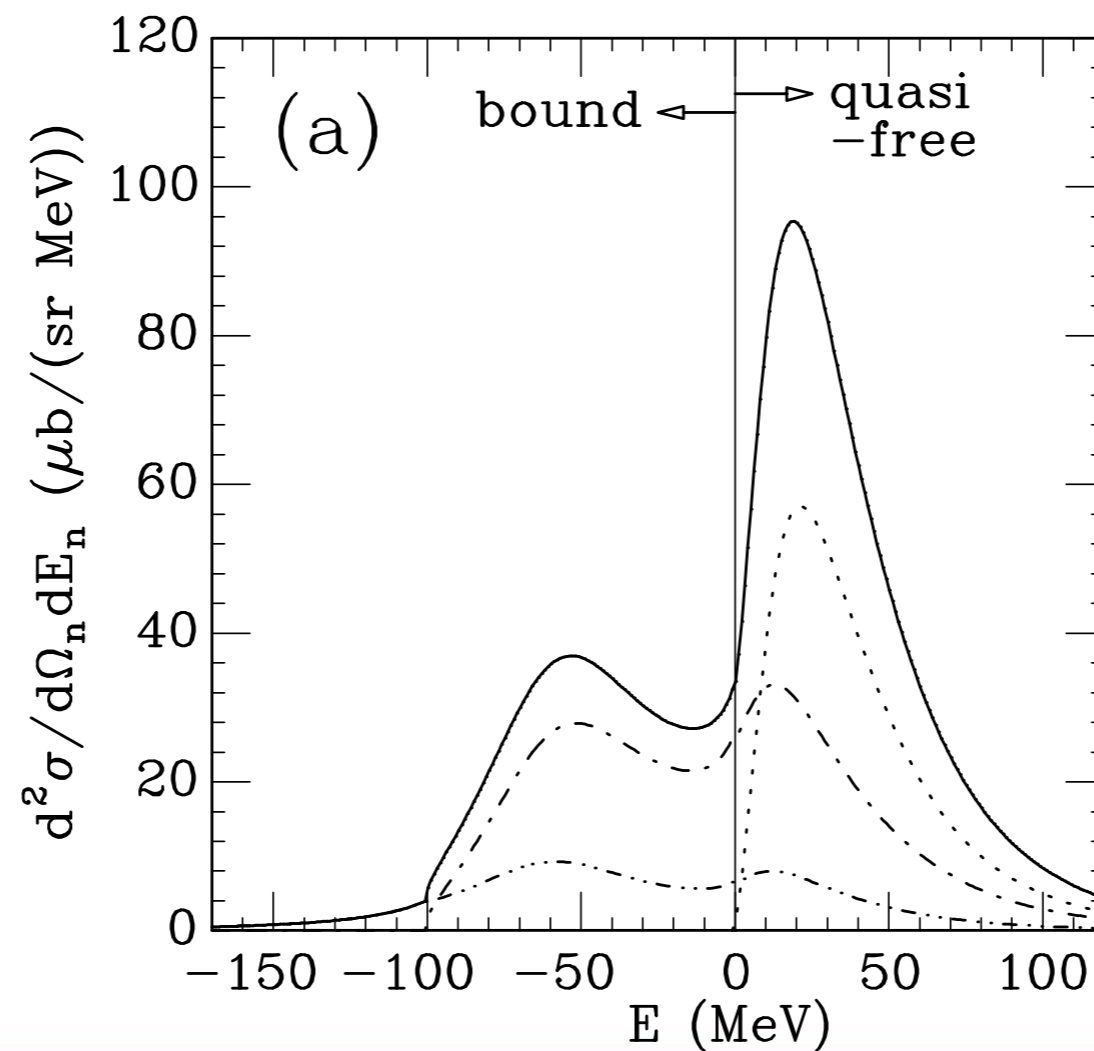
support frame for E15



- $20 \times 5 \times 150 \text{ cm}^3$ Plastic Scintillator
- Configuration : 16 (wide) x 7 (depth)
- Surface area : 3.2m x 1.5m
- missing mass resolution for K^-pp
 $\sigma = 9.2 \text{ MeV}/c^2$ ($P_n=1.3 \text{ GeV}/c$, $\sigma_{\text{TOF}}=150 \text{ ps}$)

Neutron spectrum

- ▶ $(V_0, W_0) = (-300 \text{ MeV}, -93 \text{ MeV}) \rightarrow B = 51 \text{ MeV}, \Gamma = 67 \text{ MeV}$

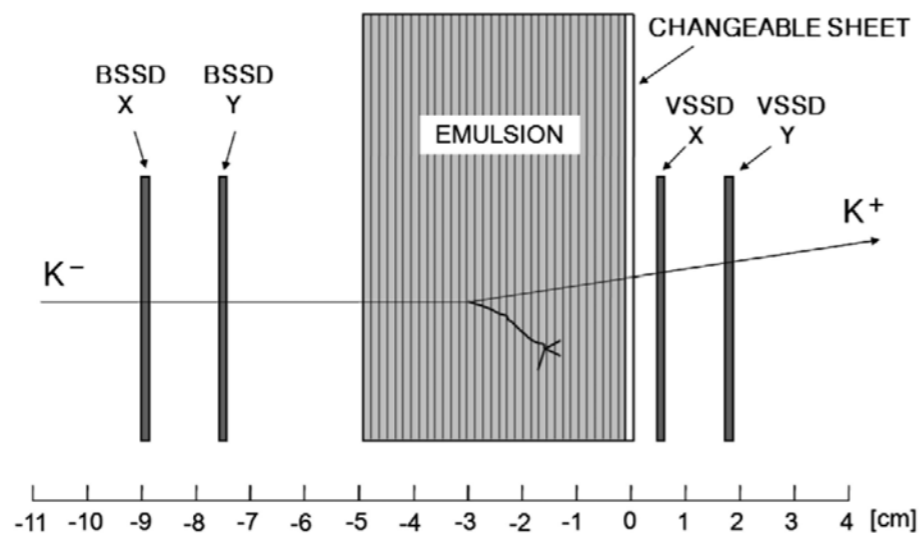


$S=-2$ Systems

Hybrid Emulsion Experiments

by K. Nakazawa

KEK E176

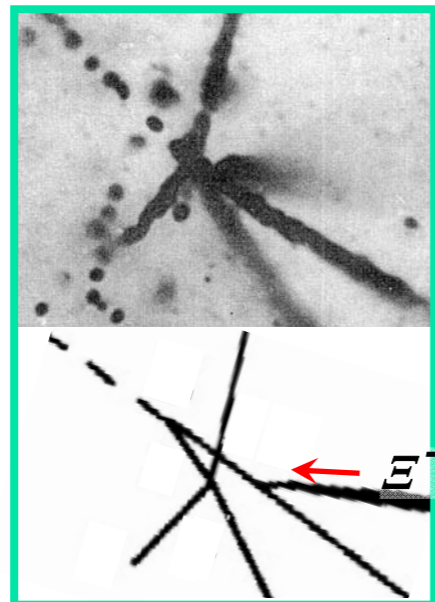


Introduction of experimental method

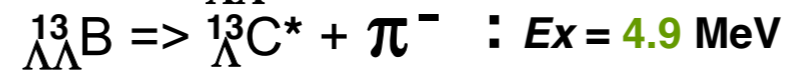
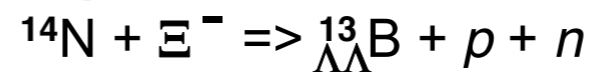
1. select Q.F. (K-,K+) reaction & reconstruct K⁺.
2. following up K⁺ meson in emulsion.
3. following down Ξ^- cand. track.
4. check seq. topology of DHY at end point.

⇒ Ξ^- stops : **77.6 +/- 5.1 events captured by**

light elem. (C,N,O) : $42.3^{+4.5}_{-9.6}$ %
 heavy elem. (Ag, Br) : $57.7^{+6.1}_{-9.6}$ %



most probable case



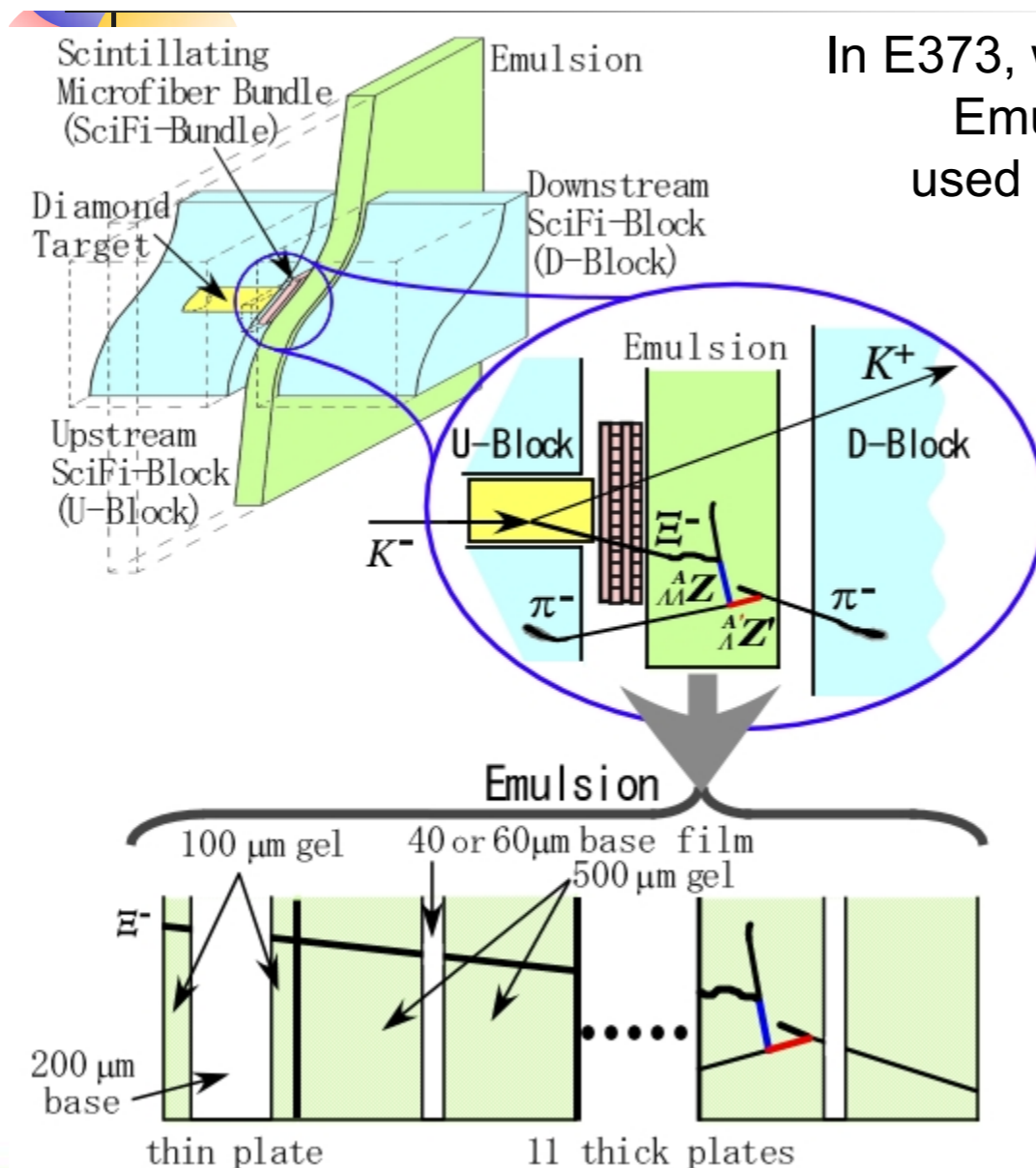
$$\Lambda\Lambda^{13}\text{B} \quad B_{\Lambda\Lambda} = 23.3 \pm 0.7 \text{ MeV}$$

$$\Delta B_{\Lambda\Lambda} = 0.6 \pm 0.8 \text{ MeV}$$

[Assumption]

$$B_{\Xi^-} = 0.17 \text{ MeV (atomic 3D in } ^{14}\text{N-}\Xi^-)$$

KEK E373



In E373, we changed the target Emulsion (E176) ==> Diamond, used SciFi-Block and -Bundle.

1. select Q.F. (K^-, K^+) reaction,
2. reconstruct Ξ^- cand. track,
3. following down Ξ^- cand. track,
4. careful analysis of the vertex.

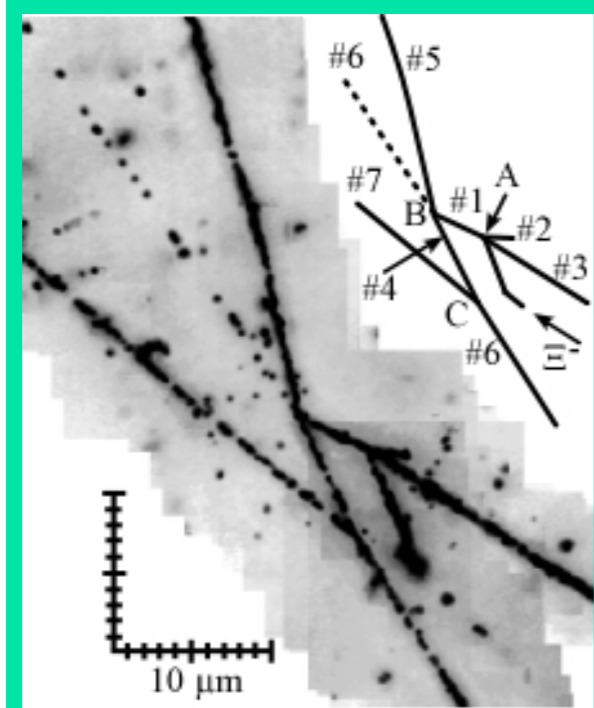
==> $\sim 10^3$ Ξ^- stops

“ the most significant result of the past 5 years in hypernuclear physics. ”

Final Report of the 2004 KEK PS External Review Committee (August 30, 2004), p5.

for NAGARA event

► Nagara Event



Unique assignment $^{12}\text{C} + \Xi^- \rightarrow \Lambda\Lambda^6\text{He} + {}^4\text{He} + t$
 $\hookrightarrow \Lambda^5\text{He} + p + \pi^-.$

1. From Consistency in A & B : $B_{\Xi^-} < 1.86 \text{ MeV}$
2. By kinematical fitting : $B_{\Lambda\Lambda} = 6.79 + 0.91 B_{\Xi^-} (+/- 0.16) \text{ MeV}$
 $\Delta B_{\Lambda\Lambda} = 0.55 + 0.91 B_{\Xi^-} (+/- 0.17) \text{ MeV}$

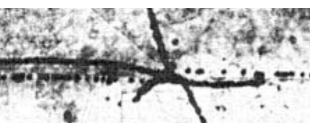
if we take into account $B_{\Xi^-} = 0.13 \text{ MeV}$ [atomic 3D : $^{12}\text{C} - \Xi^-$]

$\Lambda\Lambda^6\text{He}$ $B_{\Lambda\Lambda} = 6.91 +/- 0.16 \text{ MeV}, \Delta B_{\Lambda\Lambda} = 0.67 +/- 0.17 \text{ MeV}$

cf. in the paper PRL(2001) $B_{\Lambda\Lambda} = 7.25 +/- 0.19 \text{ MeV}, \Delta B_{\Lambda\Lambda} = 1.01 +/- 0.20 \text{ MeV}$

This discrepancy was come from the mass change of Xi- hyperon in PDG.

Summary of Emulsion events

	$\Lambda\Lambda Z$ Captured:	$B_{\Lambda\Lambda} - B_{\Xi^-}$ [MeV]	$\Delta B_{\Lambda\Lambda} - B_{\Xi^-}$ [MeV]	Assumed level	$B_{\Lambda\Lambda}$ [MeV]	$\Delta B_{\Lambda\Lambda}$ [MeV]
NAGARA	$\Lambda\Lambda^6\text{He}^{12}\text{C}$	$B_{\Lambda\Lambda} = 6.79 + 0.91 B_{\Xi^-}$ (+/- 0.16) $\Delta B_{\Lambda\Lambda} = 0.55 + 0.91 B_{\Xi^-}$ (+/- 0.17) $B_{\Xi^-} < 1.86$		3D	6.91 +/- 0.16	0.67 +/- 0.17
MIKAGE	$\Lambda\Lambda^6\text{He}^{12}\text{C}$	9.93 +/- 1.72	3.69 +/- 1.72	3D	10.06 +/- 1.72	3.82 +/- 1.72
DEMACHI-YANAGI	$\Lambda\Lambda^{10}\text{Be}^{*12}\text{C}$	11.77 +/- 0.13	-1.65 +/- 0.15 <i>cf. Ex = 3.0</i>	3D	11.90 +/- 0.13	-1.52 +/- 0.15 <i>cf. Ex = 3.0</i>
HIDA	$\Lambda\Lambda^{11}\text{Be}^{16}\text{O}$	20.26 +/- 1.15	2.04 +/- 1.23	3D	20.49 +/- 1.15	2.27 +/- 1.23
	$\Lambda\Lambda^{12}\text{Be}^{14}\text{N}$	22.06 +/- 1.15	-----	3D	22.23 +/- 1.15	-----
E176	$\Lambda\Lambda^{13}\text{B} \rightarrow \Lambda^{13}\text{C}^*$	----- <i>Ex = 4.9</i>	-----	3D	23.3 +/- 0.7	0.6 +/- 0.8
	 $\Lambda\Lambda^{10}\text{Be} \rightarrow \Lambda^9\text{Be}^*$	----- <i>Ex = 3.0</i>	-----	not checked, yet.	14.7 +/- 0.4	1.3 +/- 0.4

M.Danyasz et al., PRL.11(1963)29;
R.H.Dalitz et al., Proc. R.S.Lond.A436(1989)1

Search for Double- Λ with Sequential Weak Decay

- ▶ Large Branch of Mesonic Weak Decay in Light hyperfragments
- ▶ Characteristic π^- emission



$$P_{\pi^{-}} \sim 130 \text{ MeV}/c$$

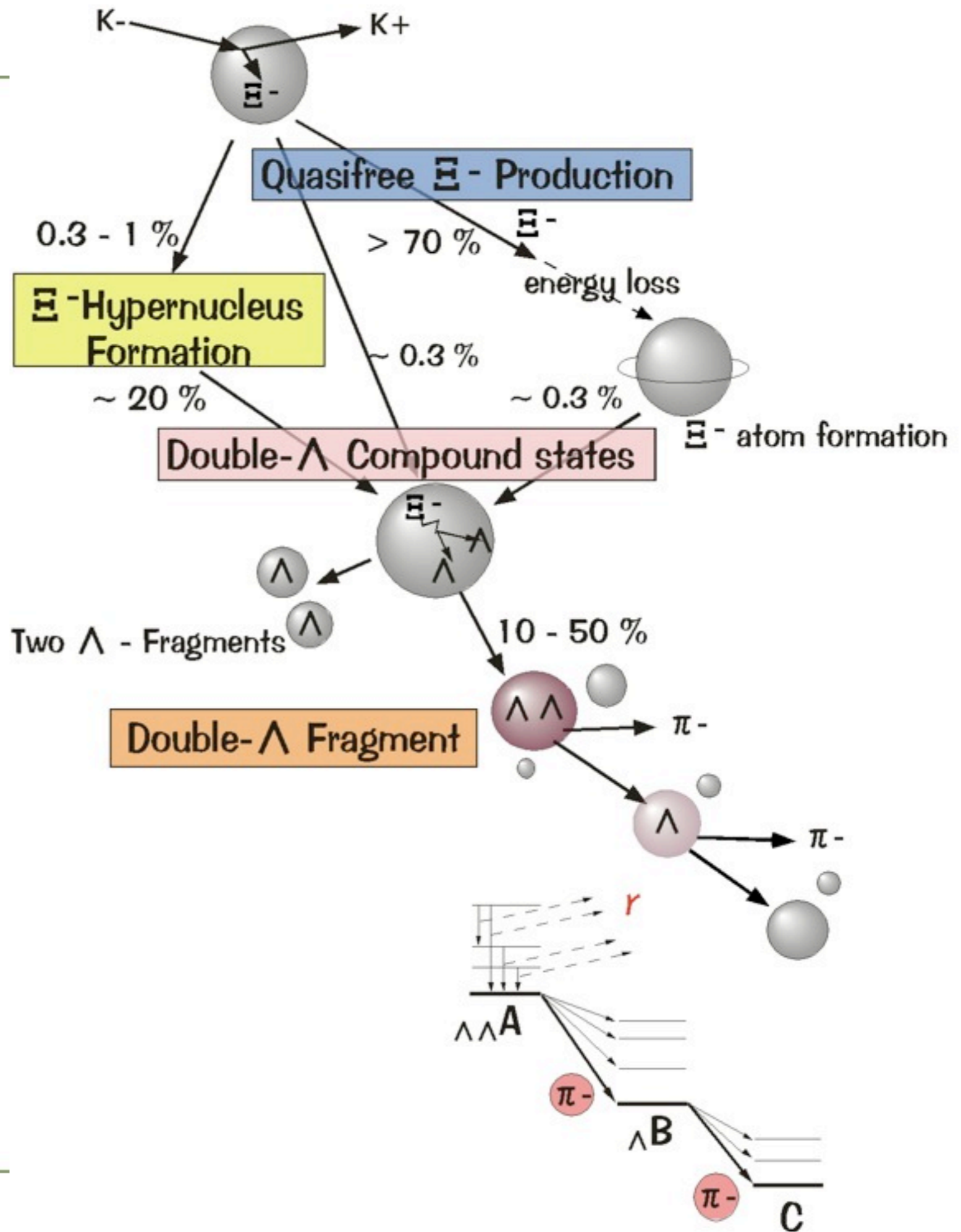
$$\Gamma_{\pi^{-}}/\Gamma_{\text{tot}} \sim 0.21$$



$$P_{\pi^{-}} = 99.2 \text{ MeV}/c$$

$$\text{Width} = 1 \text{ MeV}/c$$

$$\Gamma_{\pi^{-}}/\Gamma_{\text{tot}} \sim 0.39$$



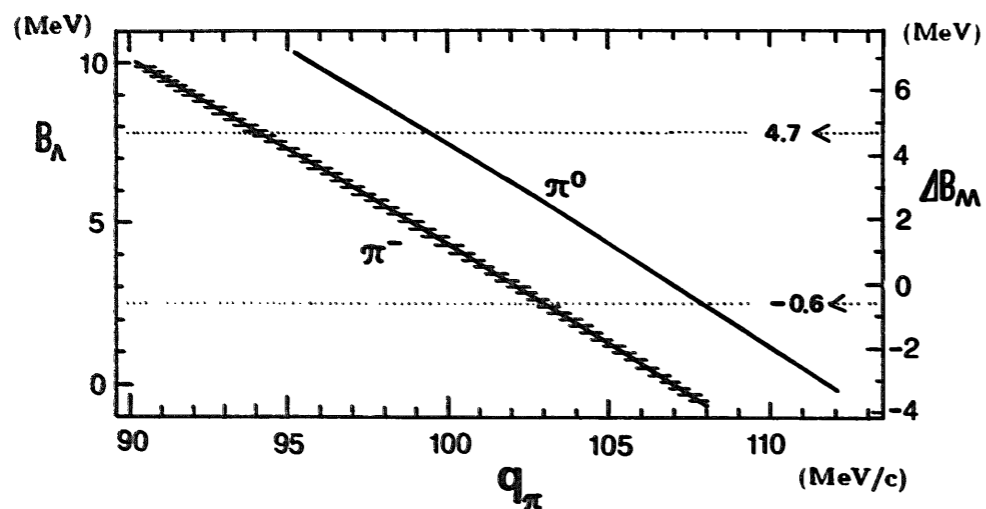


Fig. 8. The Λ -binding energy $B_\Lambda({}_{\Lambda\Lambda}^6\text{He})$ is plotted as a function of the weak decay pion momentum q_π . The corresponding $\Lambda\Lambda$ interaction matrix element $\Delta B_{\Lambda\Lambda}$ is also shown on the right scale. The hatch for the π^- decay indicates the predicted pion momentum width $\Delta q = 0.45$ MeV/c.

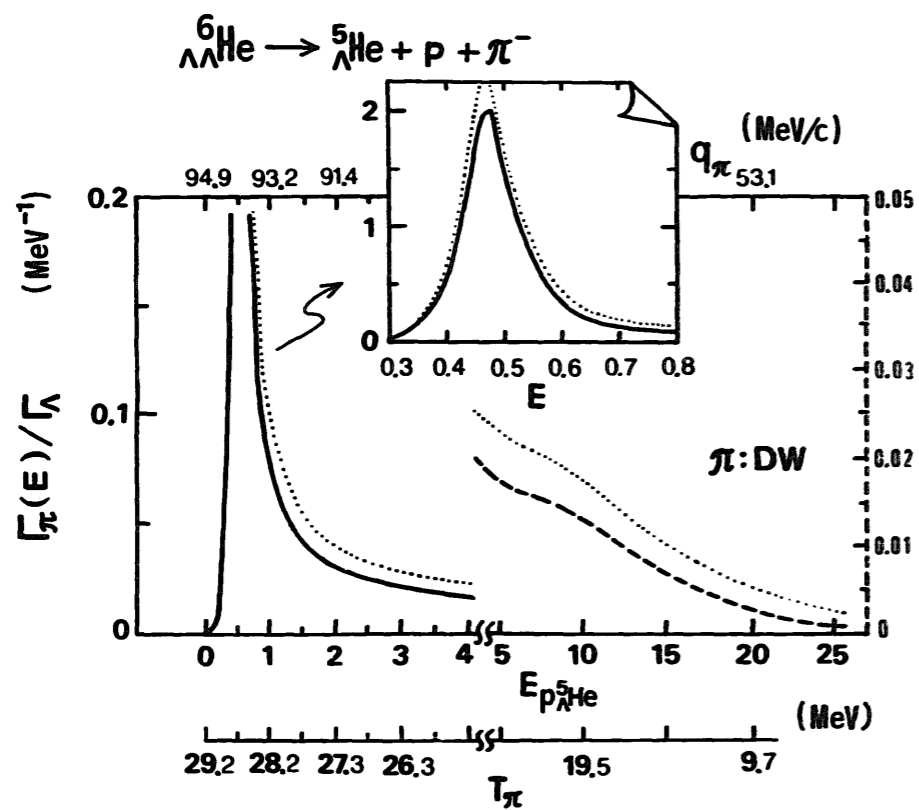
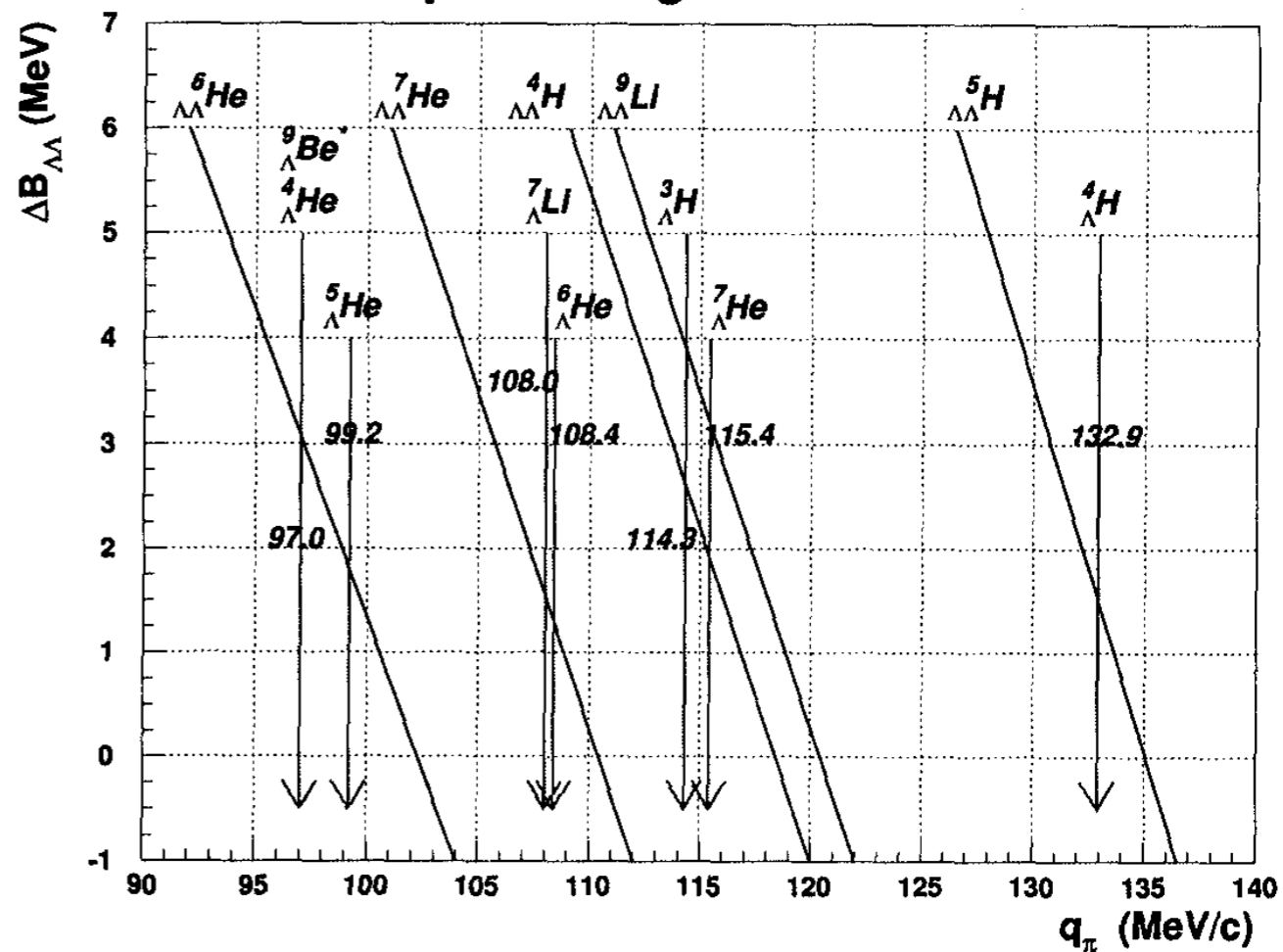


Fig. 7. The theoretical π^- decay spectrum $\Gamma_\pi(E)/\Gamma_\Lambda({}_{\Lambda\Lambda}^6\text{He})$ with YNG is drawn by solid line as a function of the proton- ${}^5_\Lambda\text{He}$ relative energy $E \equiv E_{p^5_\Lambda\text{He}}$. The shallow Λ -binding energy case described in sect. 4.2 results in the dotted curve in which case the pion momentum and energy should be shifted (cf. fig. 8).

Expected Signals and Lines



BNL E906

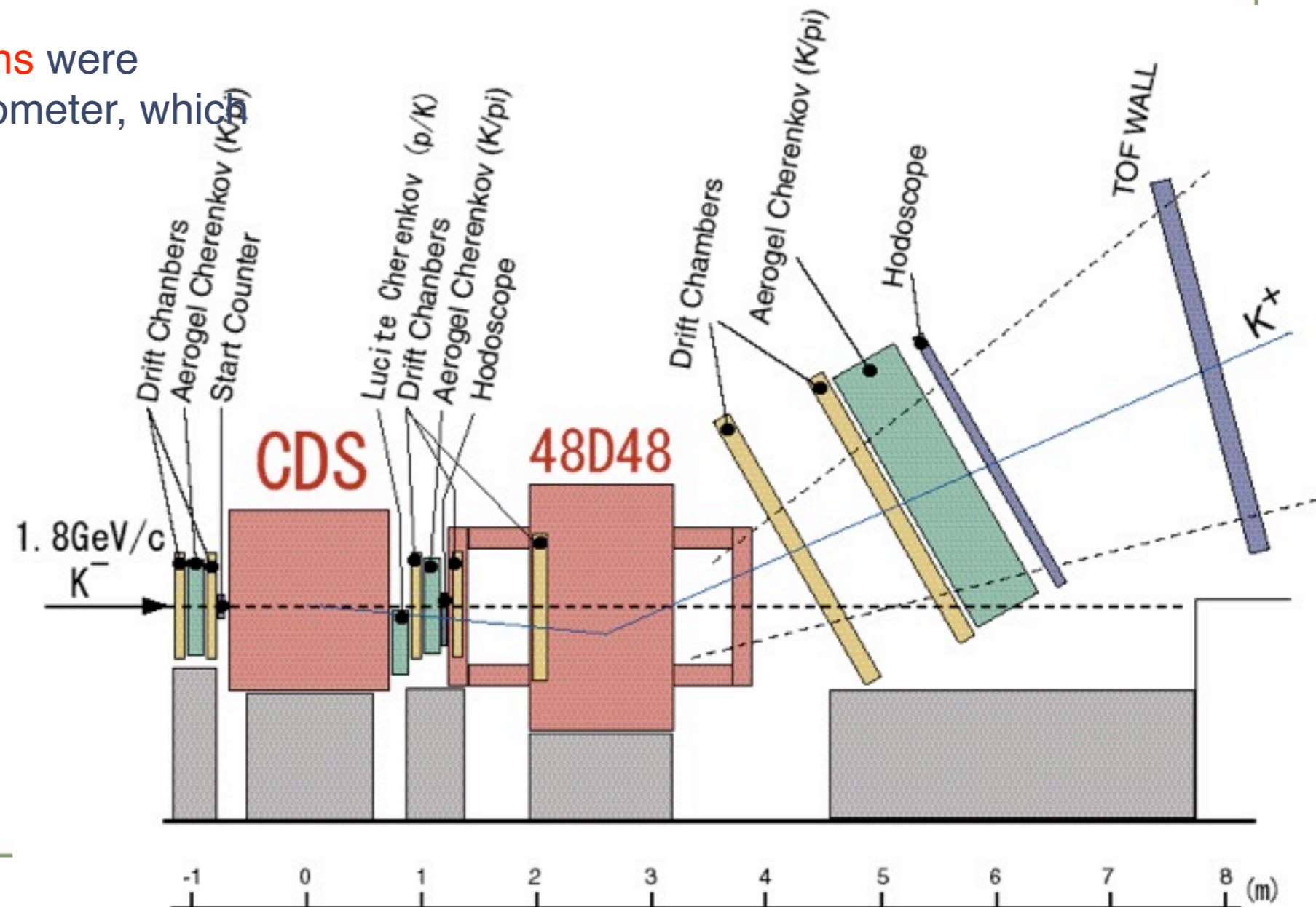
- 1998 Run Summary

- $0.9 \times 10^{12} K^-$ (1.8 GeV/c) was irradiated

- Target was a ${}^9\text{Be}$ plate (6"x 2"x1/2" high)

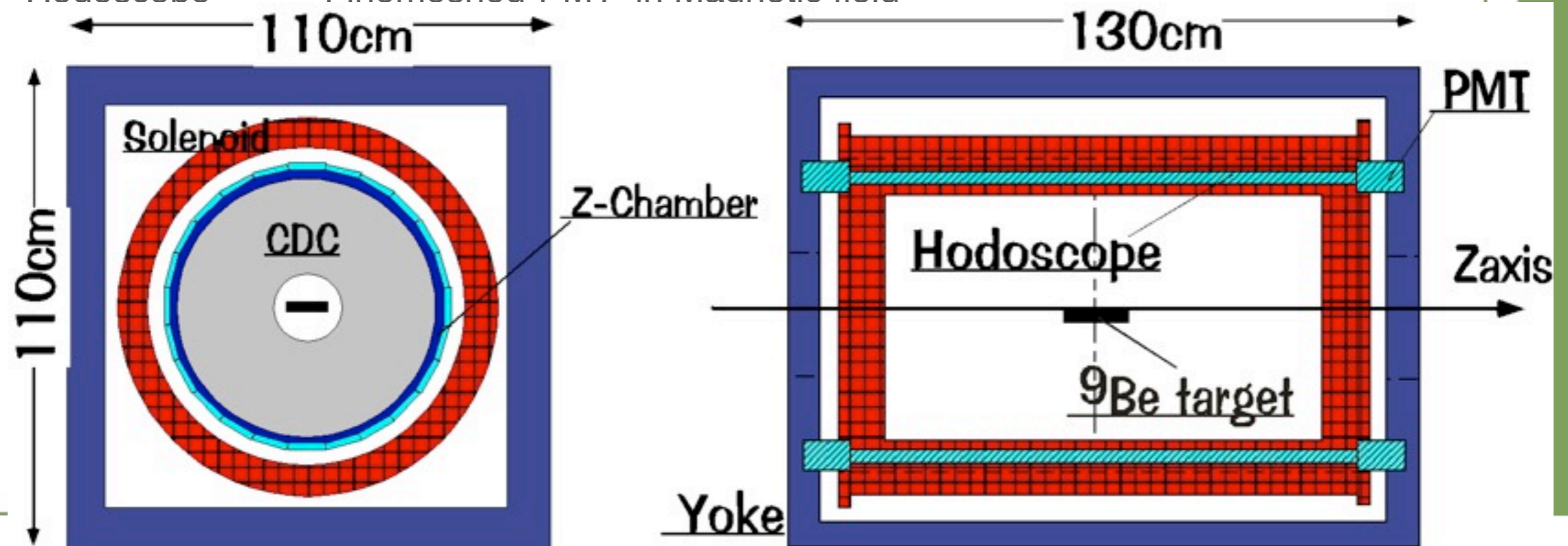
48D48 spectrometer system and CDS

- $1.1 \times 10^5 (K^-, K^+)$ reactions were identified by 48D48 spectrometer, which covers 2-10 deg.

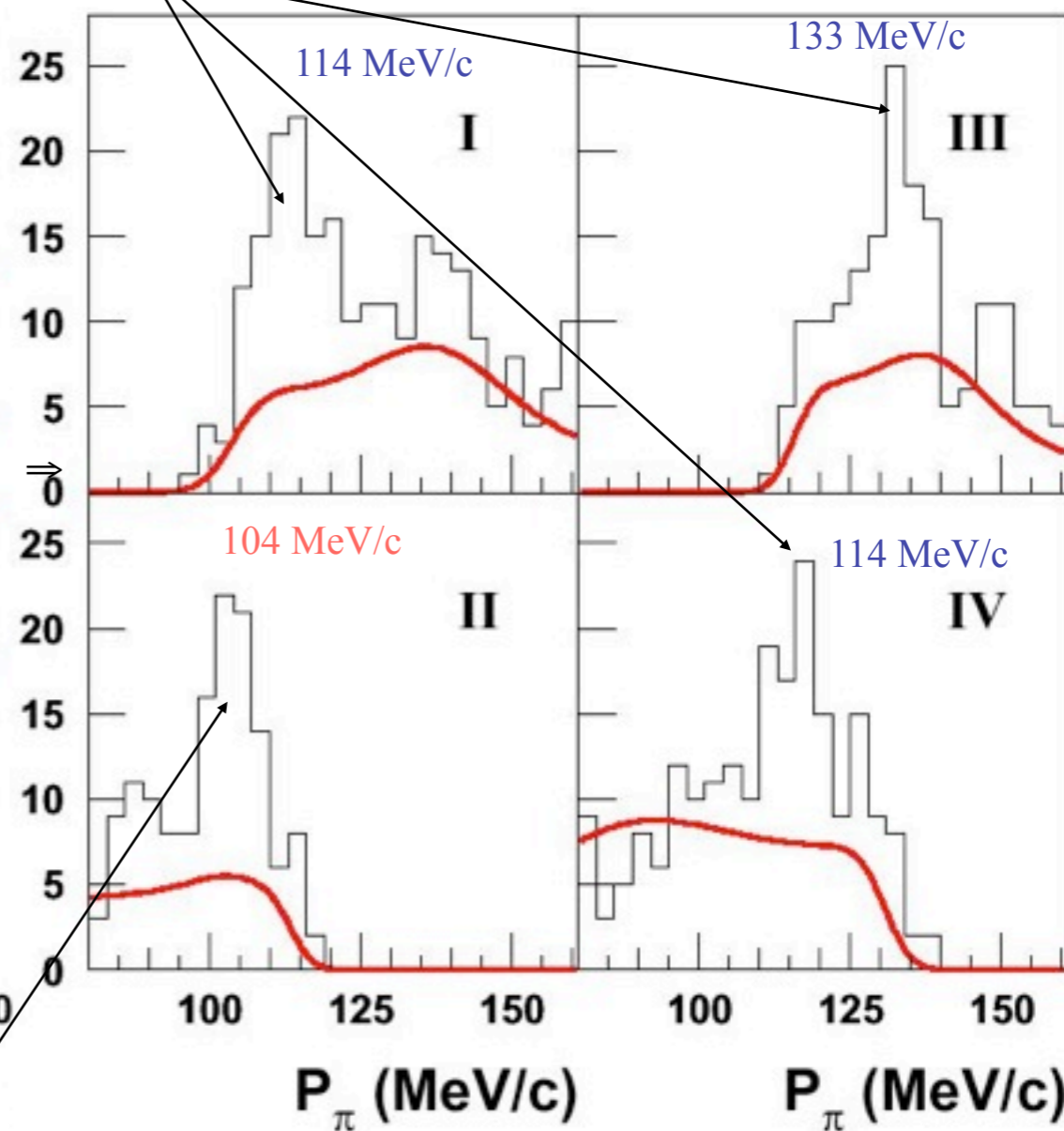
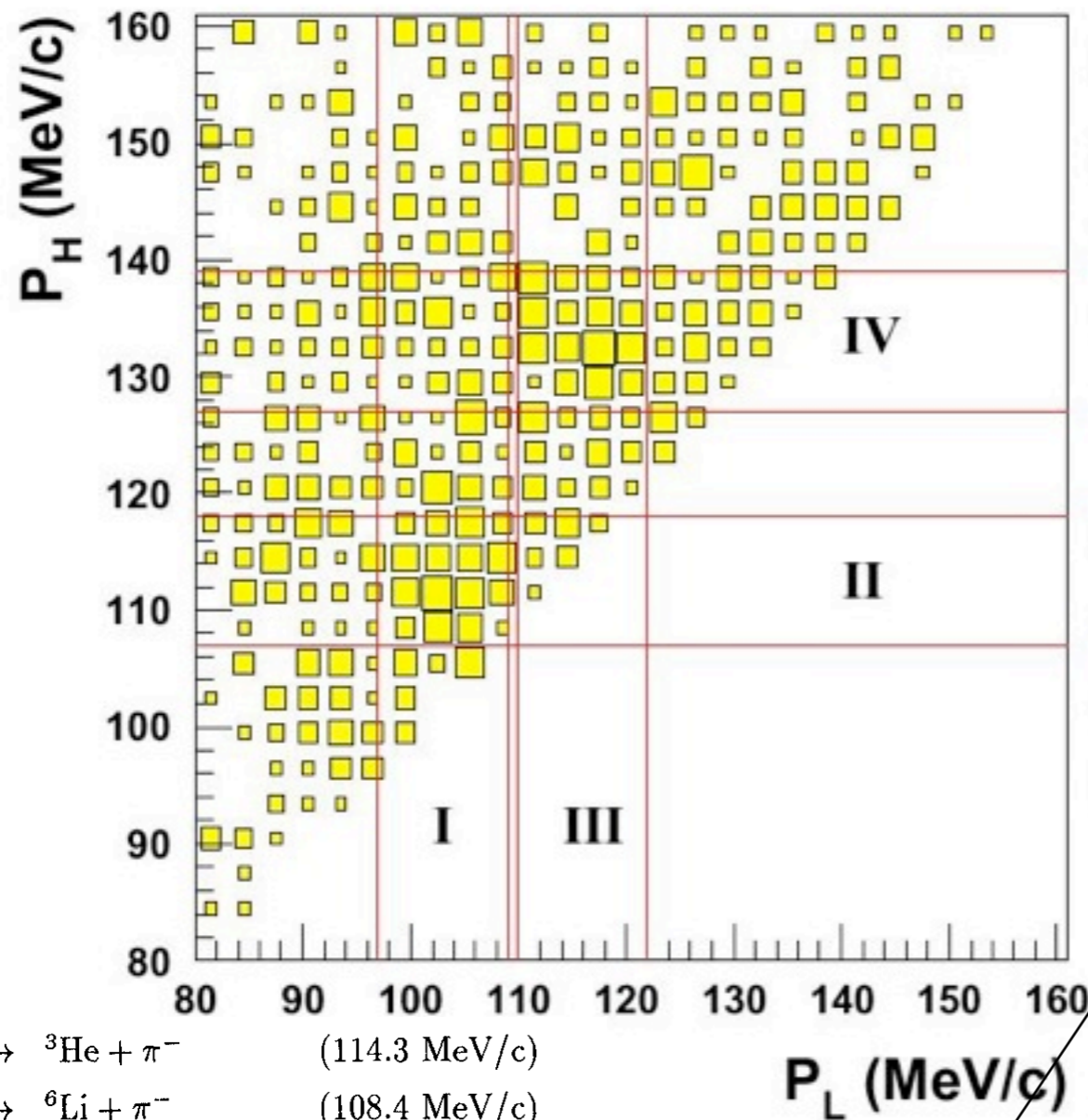
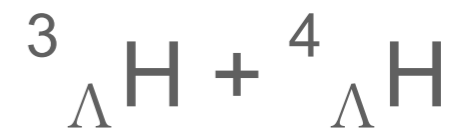


Cylindrical Detector System

- Large solid angle 72% of 4π
- Momentum resolution for 100MeV/c π 9-10MeV/c(FWHM)
- Solenoid magnet Uniform field variation less than 0.5%
- Cylindrical Drift Chamber (CDC)
 - Low Z materials
 - gas ; He:C₂H₆=50%:50%
 - field-wire ; gold plated aluminium
 - 12 layers ; 6 stereo layers, 6 axial layers, 576 cells
- Z-Chamber 5.5mm pitch Cathode strip readout-MWPC
- Hodoscope Finemeshed-PMT in Magnetic field



Consistent with known single Λ hypernuclei



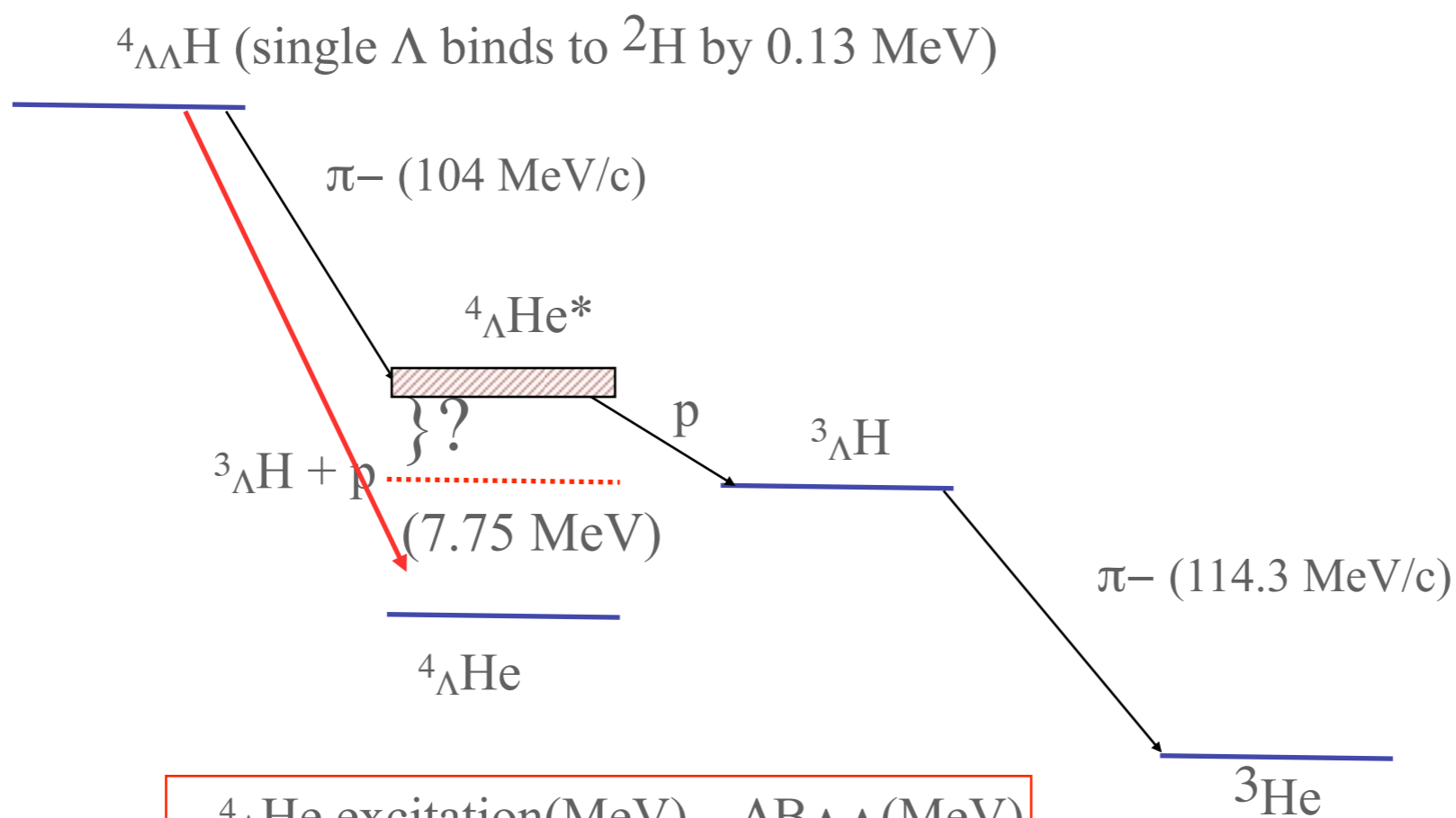
- (i) $\begin{cases} {}^3_{\Lambda}\text{H} \rightarrow {}^3\text{He} + \pi^- & (114.3 \text{ MeV}/c) \\ {}^6_{\Lambda}\text{He} \rightarrow {}^6\text{Li} + \pi^- & (108.4 \text{ MeV}/c) \end{cases}$
- (ii) $\begin{cases} {}^3_{\Lambda}\text{H} \rightarrow {}^3\text{He} + \pi^- & (114.3 \text{ MeV}/c) \\ {}^4_{\Lambda}\text{H} \rightarrow {}^3\text{H} + \text{p} + \pi^- & (\sim 98 \text{ MeV}/c) \end{cases}$
- (iii) $\begin{cases} {}^4_{\Lambda\Lambda}\text{H} \rightarrow {}^4_{\Lambda}\text{He} + \pi^- & (\sim 116 \text{ MeV}/c) \\ \quad \quad \quad \downarrow & \\ \quad \quad \quad {}^3\text{He} + \text{p} + \pi^- & (\sim 97 \text{ MeV}/c) \end{cases}$
- (iv) $\begin{cases} {}^4_{\Lambda\Lambda}\text{H} \rightarrow {}^4_{\Lambda}\text{He}^* + \pi^- & (\sim 103 \text{ MeV}/c) \\ \quad \quad \quad \downarrow & \\ \quad \quad \quad {}^3_{\Lambda}\text{H} + \text{p} & \\ \quad \quad \quad \downarrow & \\ \quad \quad \quad {}^3\text{He} + \pi^- & (114.3 \text{ MeV}/c) \end{cases}$

Phys. Rev. Lett. 87, 132504 (2001)

Candidate for $\Lambda\Lambda$ hypernucleus decay

new interpretation by S. Randeniya: ${}^7_{\Lambda\Lambda}\text{He}$

Suggested decay mode of ${}^4_{\Lambda\Lambda}\text{H}$ and limits on $\Delta B_{\Lambda\Lambda}$



${}^4_{\Lambda}\text{He}$ excitation(MeV)	$\Delta B_{\Lambda\Lambda}$ (MeV)
7.75	1.8

Search for **two body decay mode** ${}^4_{\Lambda\Lambda}\text{H} \rightarrow {}^4_{\Lambda}\text{He}(1^+) + \pi^-$

Spectroscopic Study of Ξ -Hypernucleus, $^{12}_{\Xi}\text{Be}$, via the $^{12}\text{C}(\text{K}^-, \text{K}^+)$ Reaction

E05

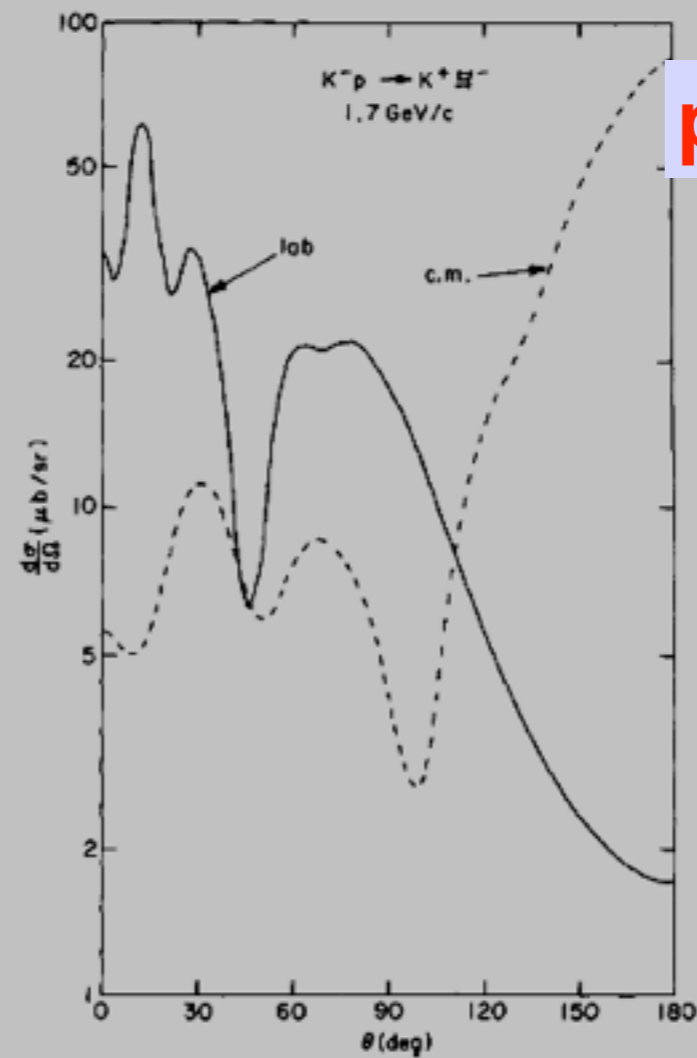
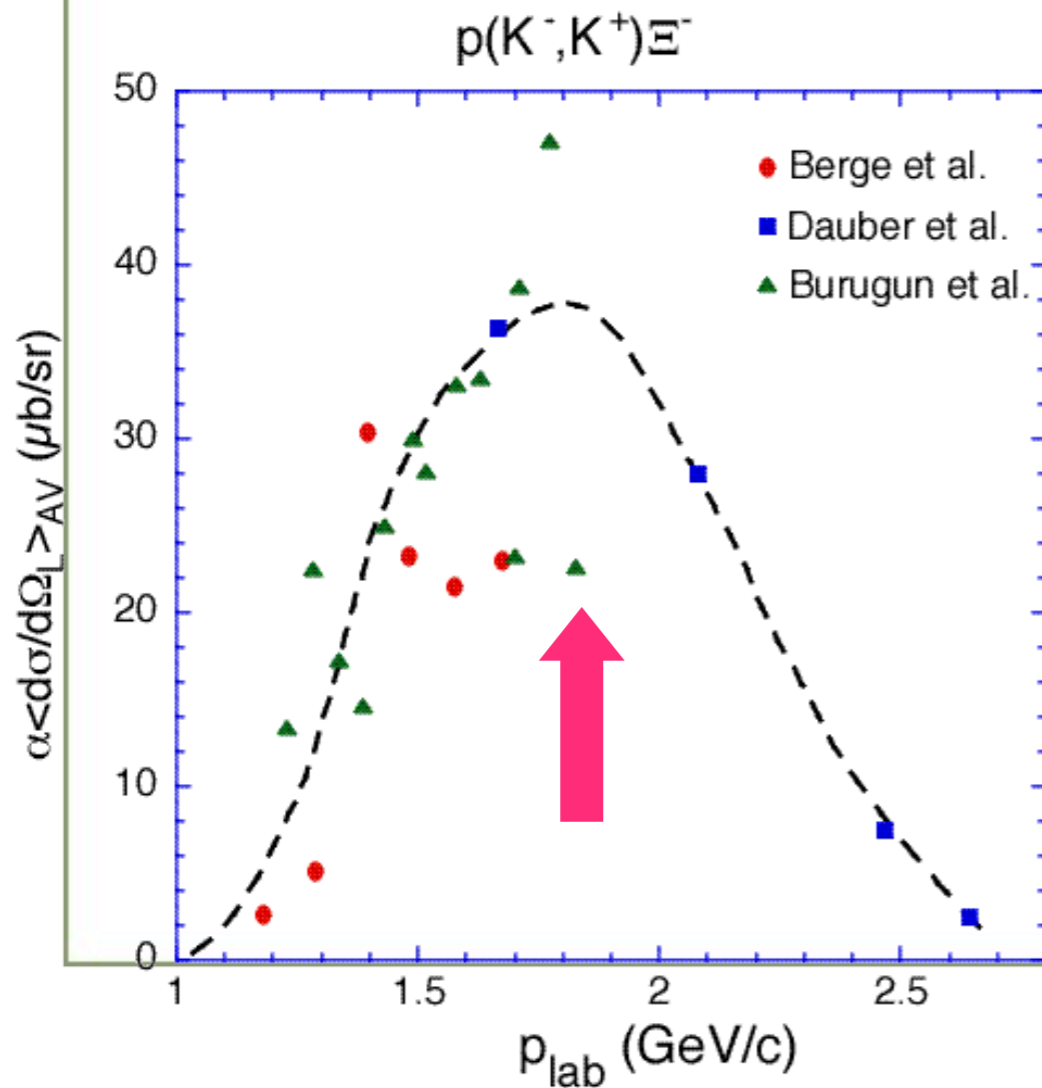
T. Nagae et al.

- ▶ Discovery of Ξ -hypernuclei
- ▶ Measurement of Ξ -nucleus potential depth and width of $^{12}_{\Xi}\text{Be}$
- ▶ Beam: K^- @ 1.8 GeV/c, 1.4×10^6 /spill
- ▶ CH_2 ~ 2 g/cm 2 : 2 weeks for tuning and calibrations
- ▶ ^{12}C 5.4 g/cm 2 : 4 weeks
- ▶ Setup: K1.8 & SKS+

Unique experiment at J-PARC :
No other place can do this experiment !

$K^- p \rightarrow K^+ \Xi^-$ Cross Section

C.B.Dover & A.Gal
Ann. of Phys. 146(1983)309



$p = 1.7 \text{ GeV}/c$

T.Iijima et al.
NPA546(1992)588

$p = 1.65 \text{ GeV}/c$
 $1.7^\circ < \theta_{\text{lab}} < 13.6^\circ$

$35 \pm 4 \mu\text{b/sr}$

Purpose of the experiment

- ▶ First Spectroscopic Study of $S=-2$ systems in (K^-, K^+) reaction
 - ▶ Ξ -hypernuclei \rightarrow double- Λ hypernuclei
 - ▶ Ξp - $\Lambda\Lambda$ mixing
 - ▶ First step for multi-strangeness baryon systems
- ▶ ΞN Interactions: almost no information
 - ▶ Attractive or repulsive ? \rightarrow potential depth
 - ▶ $\Xi p \rightarrow \Lambda\Lambda$ conversion ? \rightarrow conversion width
 - ▶ Isospin dependence ? \rightarrow Lane term $(\tau_{\Xi} \cdot \tau_C / A)$

Information on $S=-2$

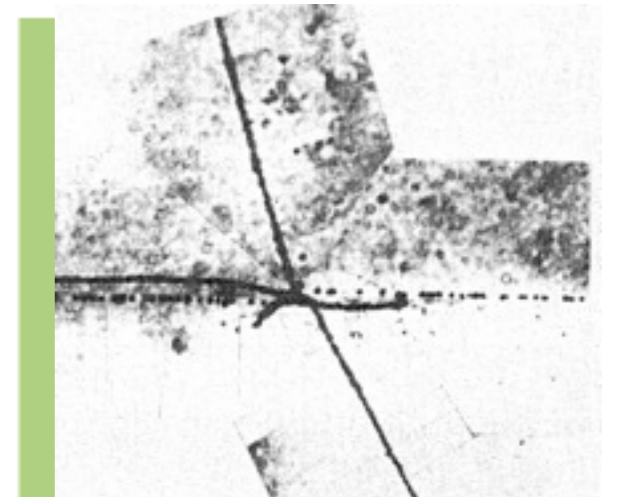
▶ Double Λ hypernuclei

- ▶ Two old emulsion events(1963,1966)
- ▶ One recent event in KEK E176(1991)
- ▶ Nagara event in KEK E373(2001)

▶ Binding energy of ${}_{\Lambda\Lambda}{}^6\text{He}$ $\Delta B_{\Lambda\Lambda} = 0.67 \pm 0.17 \text{ MeV}$

▶ $m_H > 2223.7 \text{ MeV}/c^2$ H.Takahashi et al., PRL 87 (2001) 212502

▶ [I] hypernuclei ?



$$\Delta B_{\Lambda\Lambda} = 4.3 \pm 0.4 \text{ MeV}$$

D.J.Prowse, PRL.17(1966)782



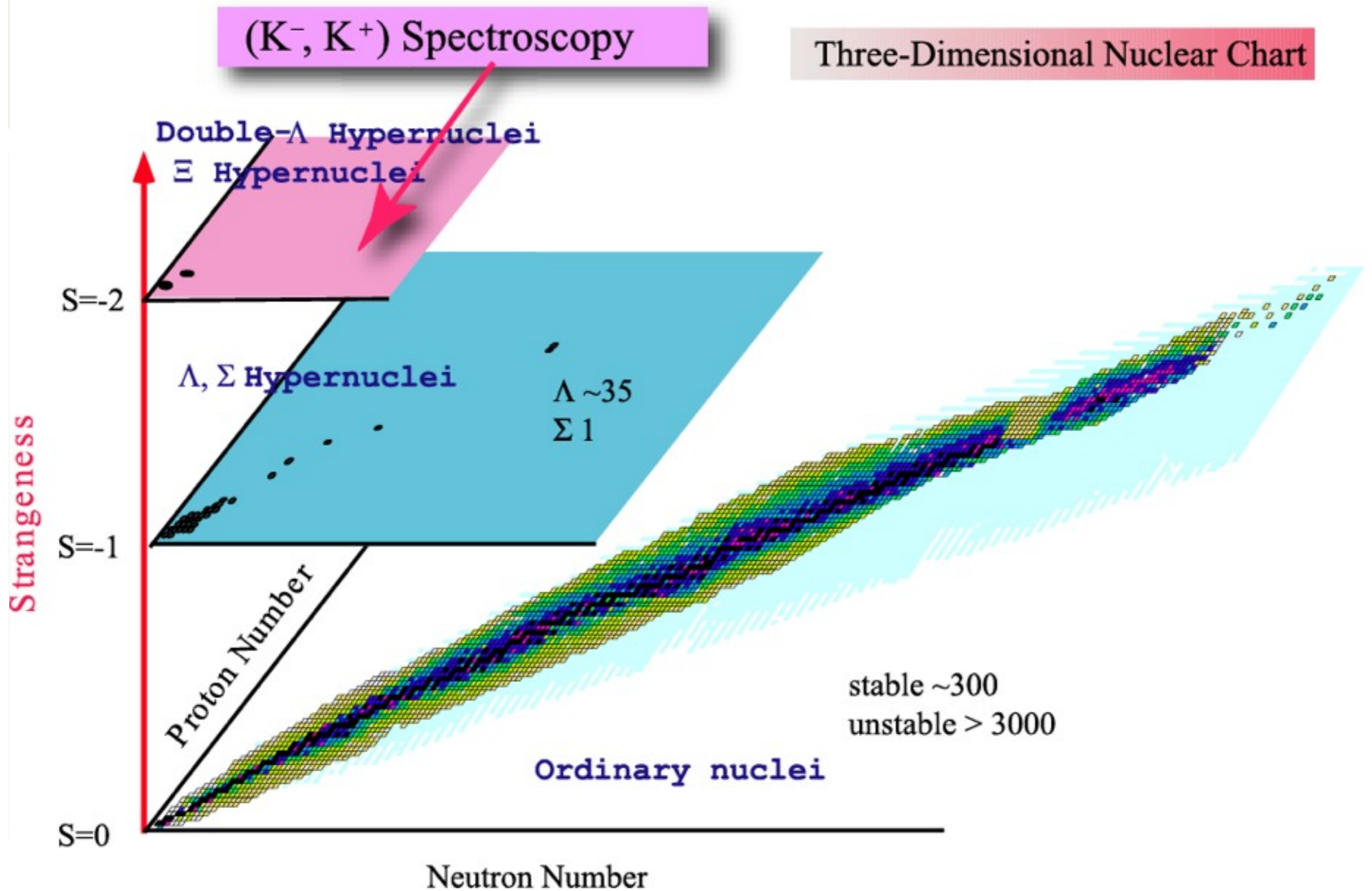
$$\Delta B_{\Lambda\Lambda} = 4.6 \pm 0.5 \text{ MeV}$$

S.Aoki et al, PTP.85(1991)1287



$$\Delta B_{\Lambda\Lambda} = 4.9 \pm 0.8 \text{ MeV}$$

Strangeness Nuclear Physics

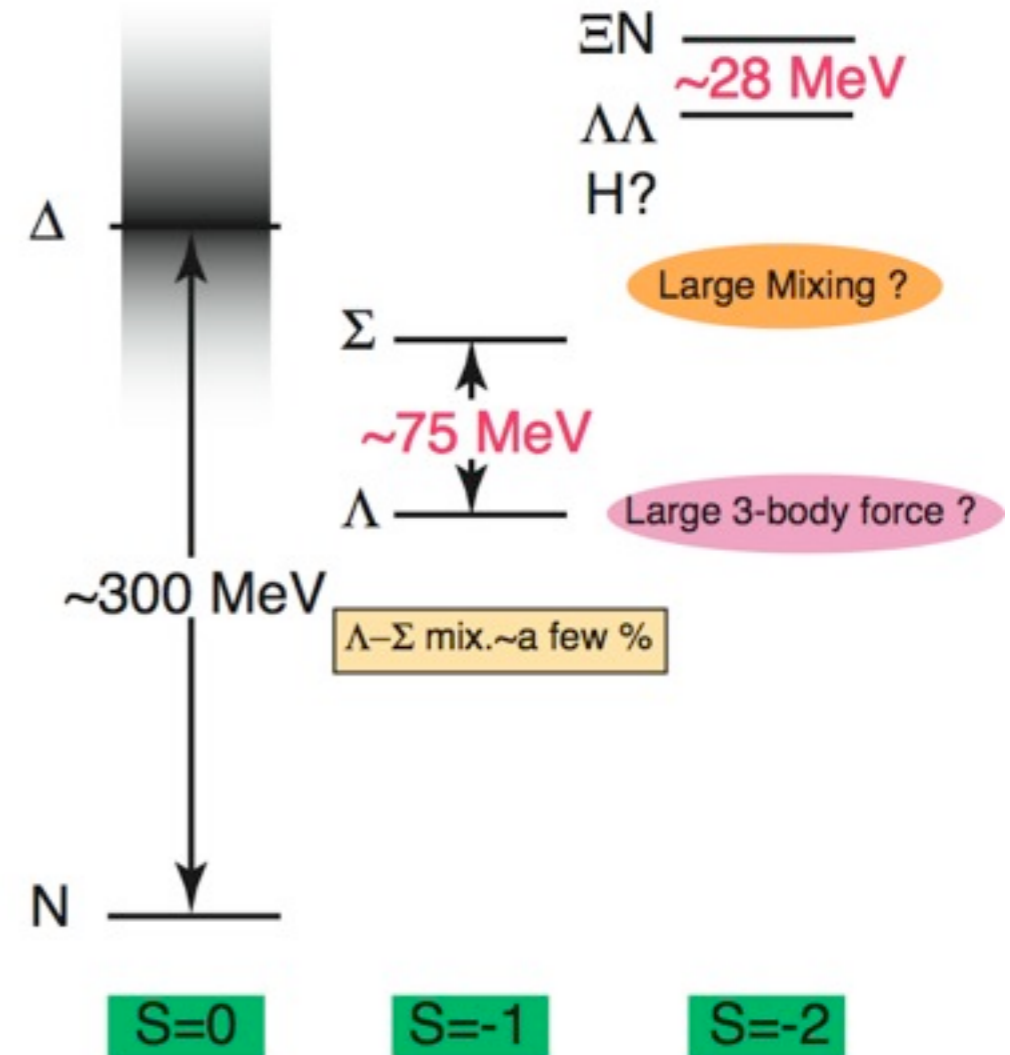
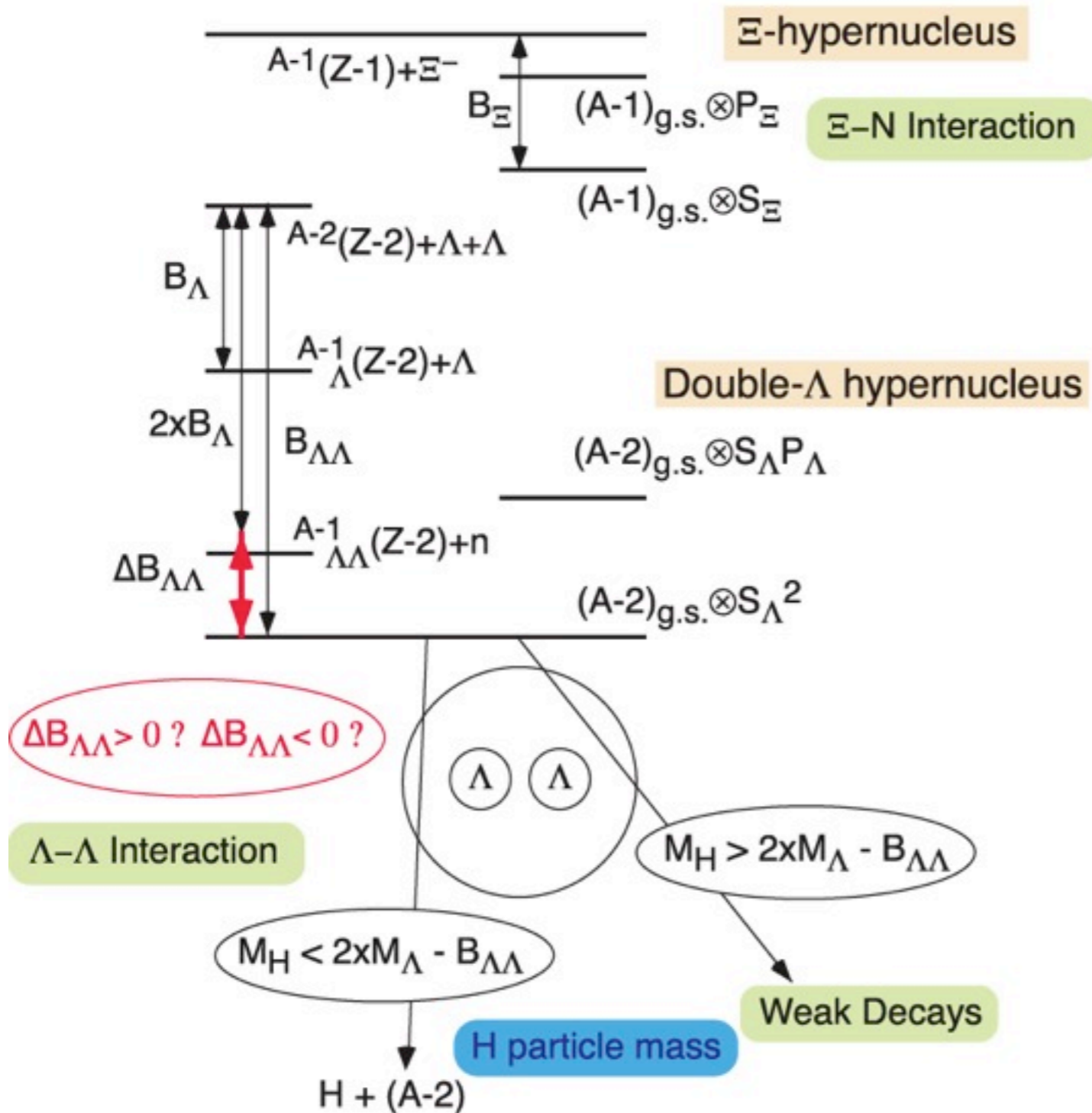


Purpose of the experiment - cont.

- ▶ **First Spectroscopic Study of $S=-2$ systems in (K^-, K^+) reaction**
 - ▶ Ξ -hypernuclei \rightarrow double- Λ hypernuclei
 - ▶ Ξp - $\Lambda\Lambda$ mixing
 - ▶ First step for multi-strangeness baryon systems
- ▶ **ΞN Interactions: almost no information**
 - ▶ Attractive or repulsive ? \rightarrow potential depth
 - ▶ $\Xi p \rightarrow \Lambda\Lambda$ conversion ? \rightarrow conversion width
 - ▶ Isospin dependence ? \rightarrow Lane term $(\tau_{\Xi} \cdot \tau_C / A)$

S=-2 Baryon Systems

Energy Spectrum of S=-2 systems



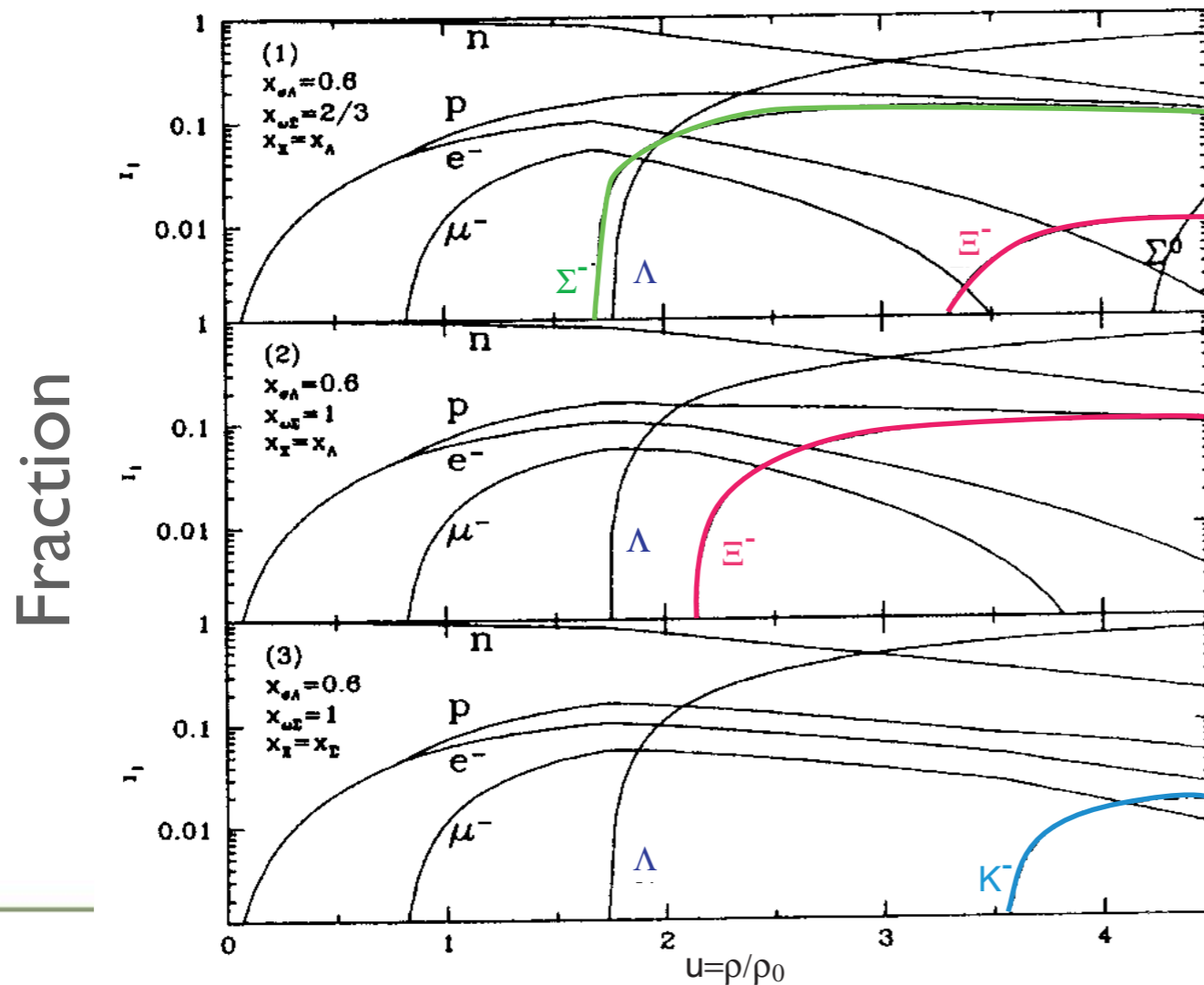
Purpose of the experiment - cont.

- ▶ **First Spectroscopic Study of $S=-2$ systems in (K^-,K^+) reaction**
 - ▶ Ξ -hypernuclei \rightarrow double- Λ hypernuclei
 - ▶ Ξp - $\Lambda\Lambda$ mixing
 - ▶ First step for multi-strangeness baryon systems
- ▶ **ΞN Interactions: almost no information**
 - ▶ Attractive or repulsive ? \rightarrow potential depth
 - ▶ $\Xi p \rightarrow \Lambda\Lambda$ conversion ? \rightarrow conversion width
 - ▶ Isospin dependence ? \rightarrow Lane term $(\tau_{\Xi} \cdot \tau_C / A)$

Ξ hypernuclei potential ?

- $\Lambda, \Sigma^-, \Xi^-, K^-$ in Neutron Star Core ?

Chemical Potential:
$$\mu_B = m_B + \frac{k_F^2}{2m_B} + U(k_F)$$



$$U_{\Sigma} < 0, U_{\Xi} < 0$$

$$U_{\Sigma} > 0, U_{\Xi} < 0$$

$$U_{\Sigma} > 0, U_{\Xi} > 0$$

Purpose of the experiment - cont.

- ▶ First Spectroscopic Study of $S=-2$ systems in (K^-, K^+) reaction
 - ▶ Ξ -hypernuclei \rightarrow double- Λ hypernuclei
 - ▶ Ξp - $\Lambda\Lambda$ mixing
 - ▶ First step for multi-strangeness baryon systems
- ▶ ΞN Interactions: almost no information
 - ▶ Attractive or repulsive ? \rightarrow potential depth
 - ▶ $\Xi p \rightarrow \Lambda\Lambda$ conversion ? \rightarrow conversion width
 - ▶ Isospin dependence ? \rightarrow Lane term $(\tau_{\Xi} \cdot \tau_C / A)$

U_E and Partial Wave Contributions in Nuclear Matter

Model	T	1S_0	3S_1	1P_1	3P_0	3P_1	3P_2	U_E	Γ_E
NHC-D	0	-2.6	0.1	-2.1	-0.2	-0.7	-1.9	-25.2	0.9
	1	-3.2	-2.3	-3.0	-0.0	-3.1	-6.3		
Ehime	0	-0.9	-0.5	-1.0	0.3	-2.4	-0.7	-22.3	0.5
	1	-1.3	-8.6	-0.8	-0.4	-1.7	-4.2		
ESC04d*	0	6.3	-18.4	1.2	1.5	-1.3	-1.9	-12.1	12.7
	1	7.2	-1.7	-0.8	-0.5	-1.2	-2.8		

- ▶ OBE (NHC-D, Ehime)
 - ▶ odd-state attraction
 - ▶ strong A-dependence of V_E
- ▶ ESC04d*
 - ▶ strong attraction of 3S_1 (T=0)

Hyperon-Nucleus Potentials

	Central	Spin-Orbit	Imaginary
ΛN	$V^\Lambda \sim 2/3 \times V^N$ $\sim 30 \text{ MeV}$	very small	—
$\Lambda\Lambda$	weak attraction $\Delta B_{\Lambda\Lambda} \sim 1 \text{ MeV}$		
ΣN	Strongly Repulsive, Large Isospin-dep.	$V_{so}^\Sigma \sim V_{so}^N$	Large
ΞN	Weakly Attractive, Isospin-dep.: Large or Small ??	$V_{so}^\Xi \ll -V_{so}^N ??$	Small or Large ??

Previous Measurements on $^{12}\text{C}(K^-,K^+)$

BNL-AGS E885

PHYSICAL REVIEW C 61 054603

Evidence!? $V_{\Xi} = -14 \text{ MeV}$

$P_K = 1.8 \text{ GeV}/c$

$\Delta M = 9.9 \text{ MeV}/c^2$ (FWHM) for $p(K^-,K^+)\Xi^-$

$-20 < E_{\Xi} < 0 \text{ MeV}$

$89 \pm 14 \text{ nb/sr } \theta < 8^\circ$

$42 \pm 5 \text{ nb/sr } \theta < 14^\circ$

P. Khaustov et al,
PRC 61 (2000) 0546

P. KHAUSTOV *et al.*

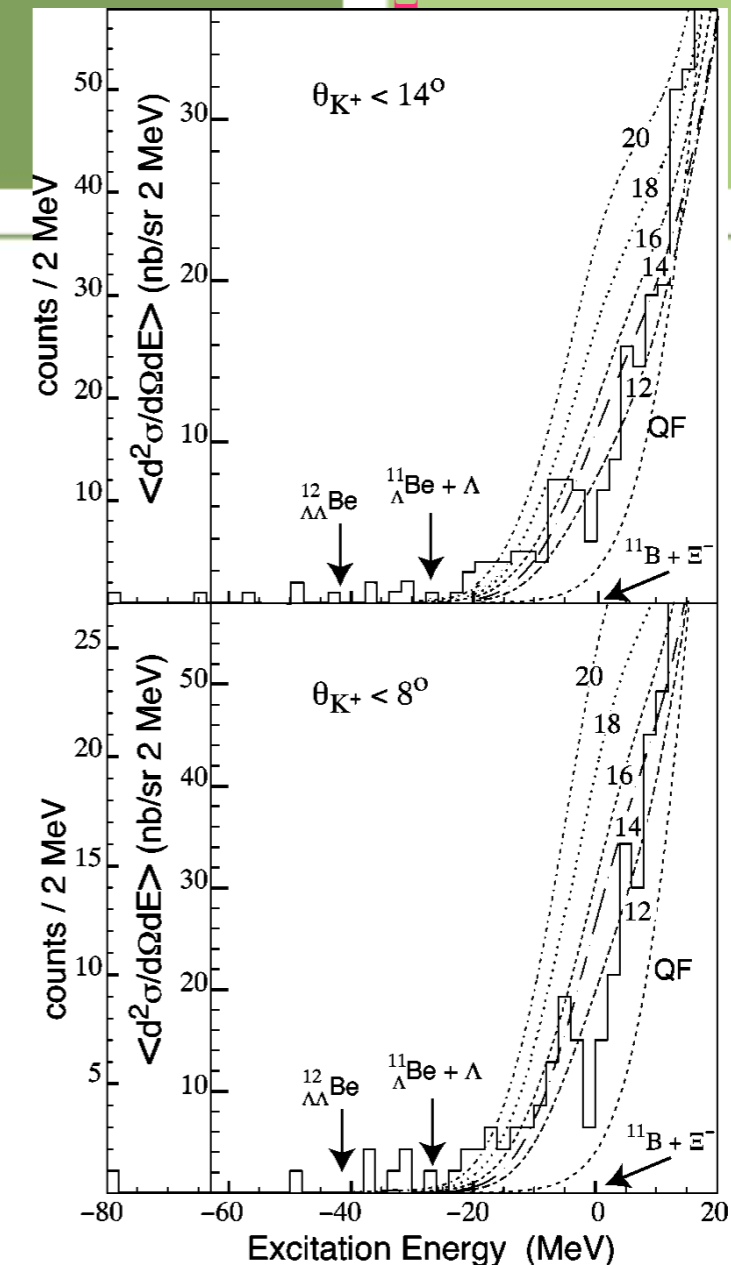
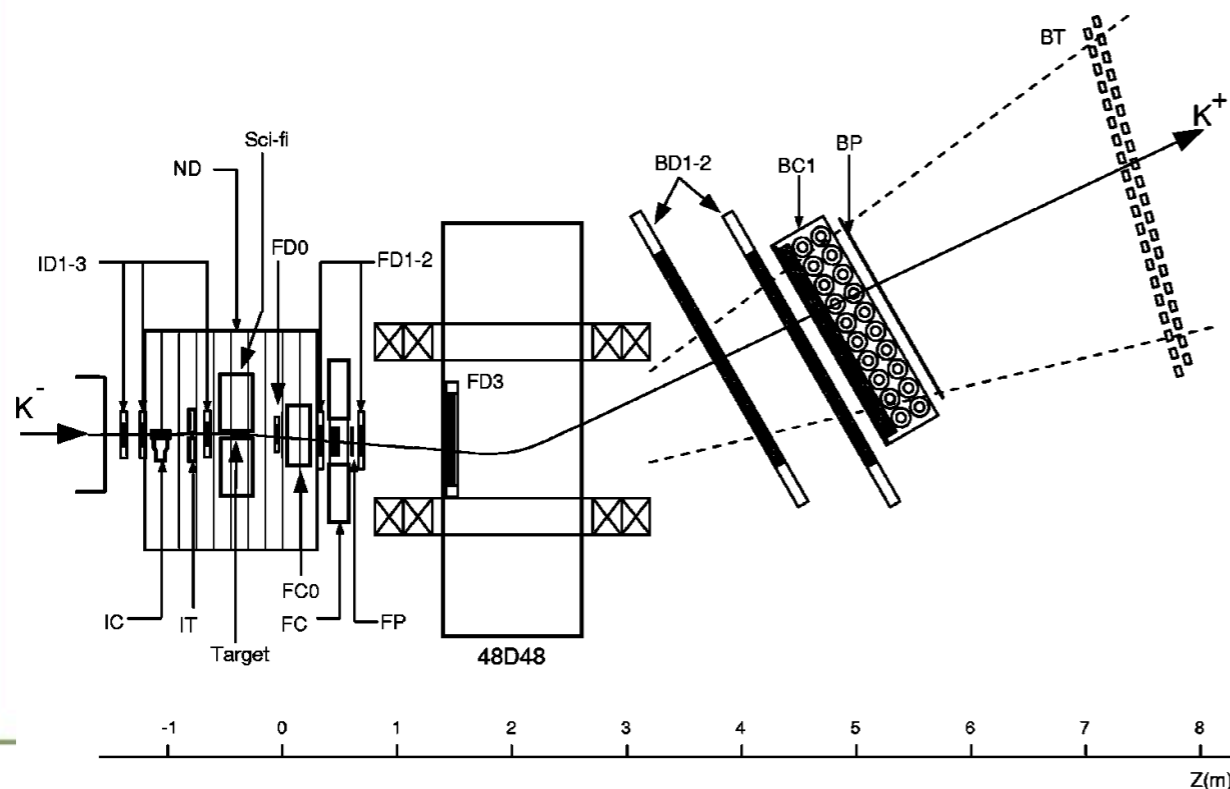
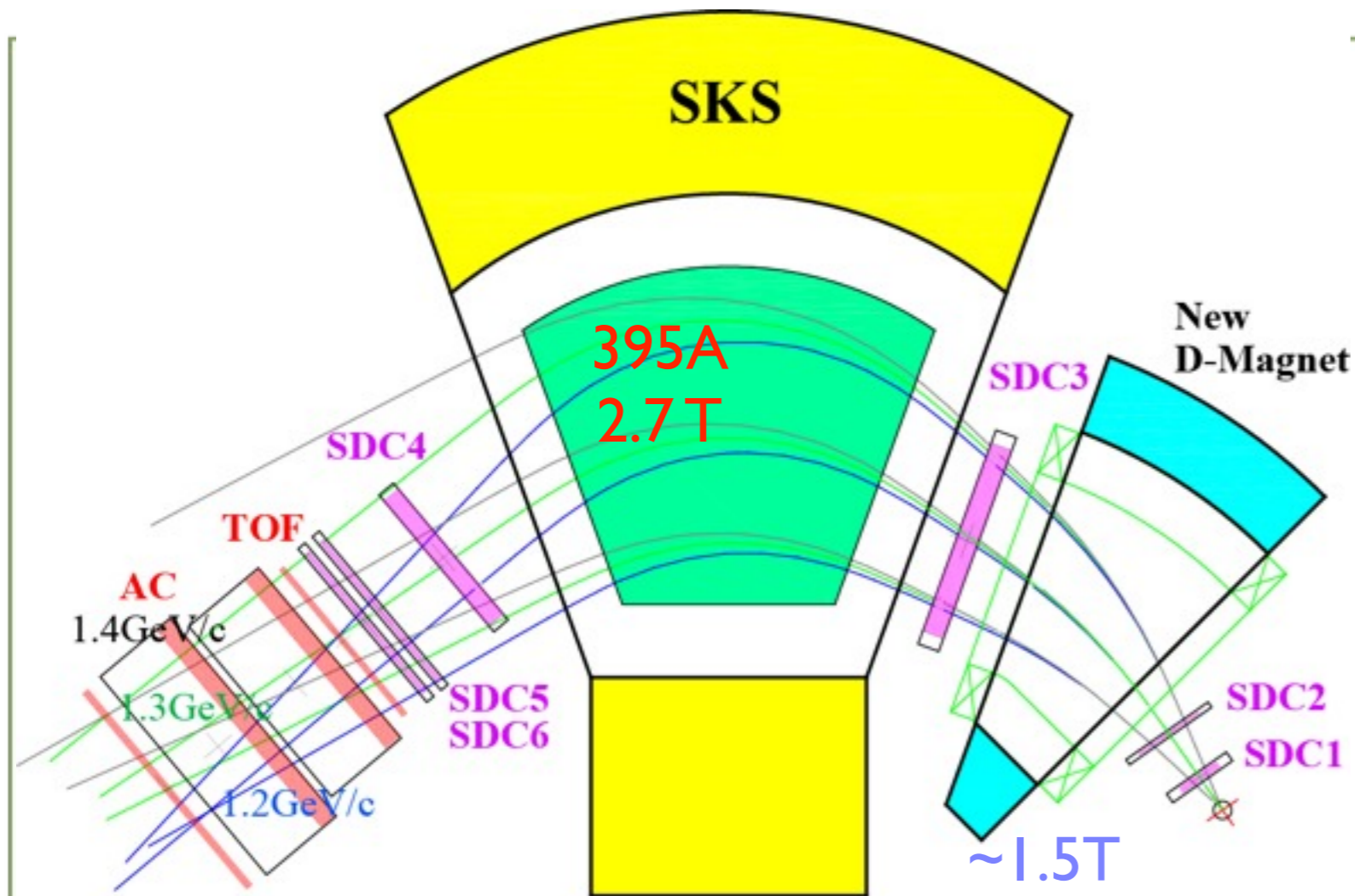


FIG. 6. Excitation-energy spectra from E885 for $^{12}\text{C}(K^-,K^+)X$ for $\theta_{K^+} < 14^\circ$ (top figure) and $\theta_{K^+} < 8^\circ$ (bottom figure) along with $^{12}_{\Lambda\Lambda}\text{Be}$ production theoretical curves for $V_{0\Xi}$ equal to 20, 18, 16, 14, and 12 MeV. The results of a quasifree Ξ production calculation are also shown (curve QF). The expected location of the ground state of $^{12}_{\Lambda\Lambda}\text{Be}$ and the thresholds for $^{11}_{\Lambda}\text{Be} + \Lambda$ and $^{11}\text{B} + \Xi^-$ production are indicated with arrows.

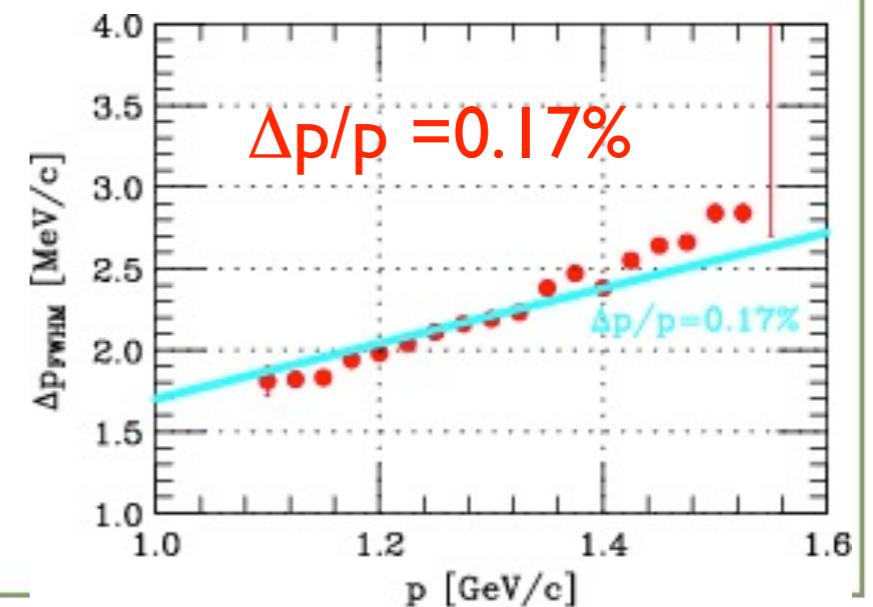
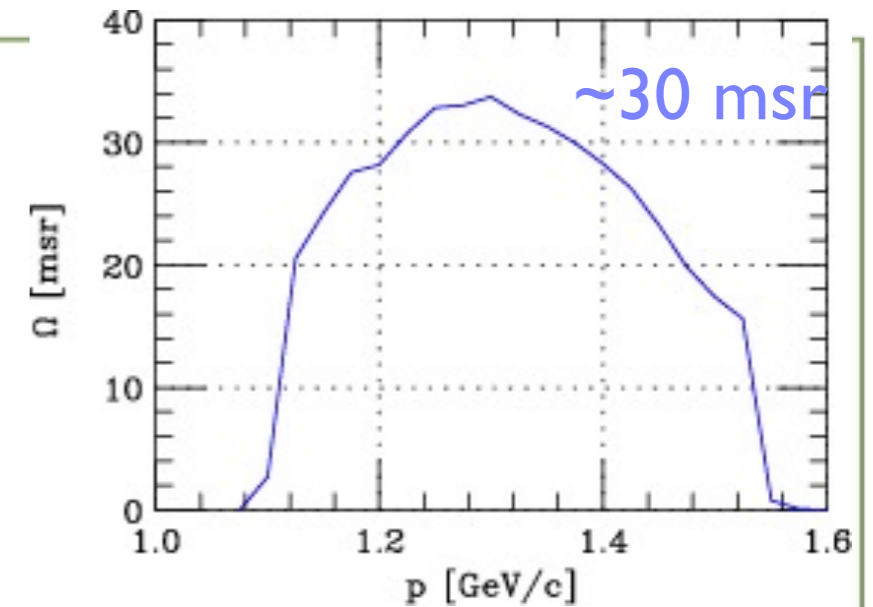
Experimental Setup

- ▶ K1.8 beam line
 - ▶ Double Electro-static Separators $\rightarrow K^-/\pi^- = 6.9$
 - ▶ High Intensity: 1.4×10^6 K^- /spill @ 30 GeV ($9 \mu A$)
 - ▶ Beam Spectrometer (QQDQQ): $\Delta p/p = 3.3 \times 10^{-4}$ (FWHM)
- ▶ SKS+ spectrometer
 - ▶ A new dipole magnet in front of SKS
 - ▶ Acceptance: 30 msr
 - ▶ Momentum Resolution: $\Delta p/p = 1.7 \times 10^{-3}$ (FWHM)
 - ▶ New simple cryogenics system

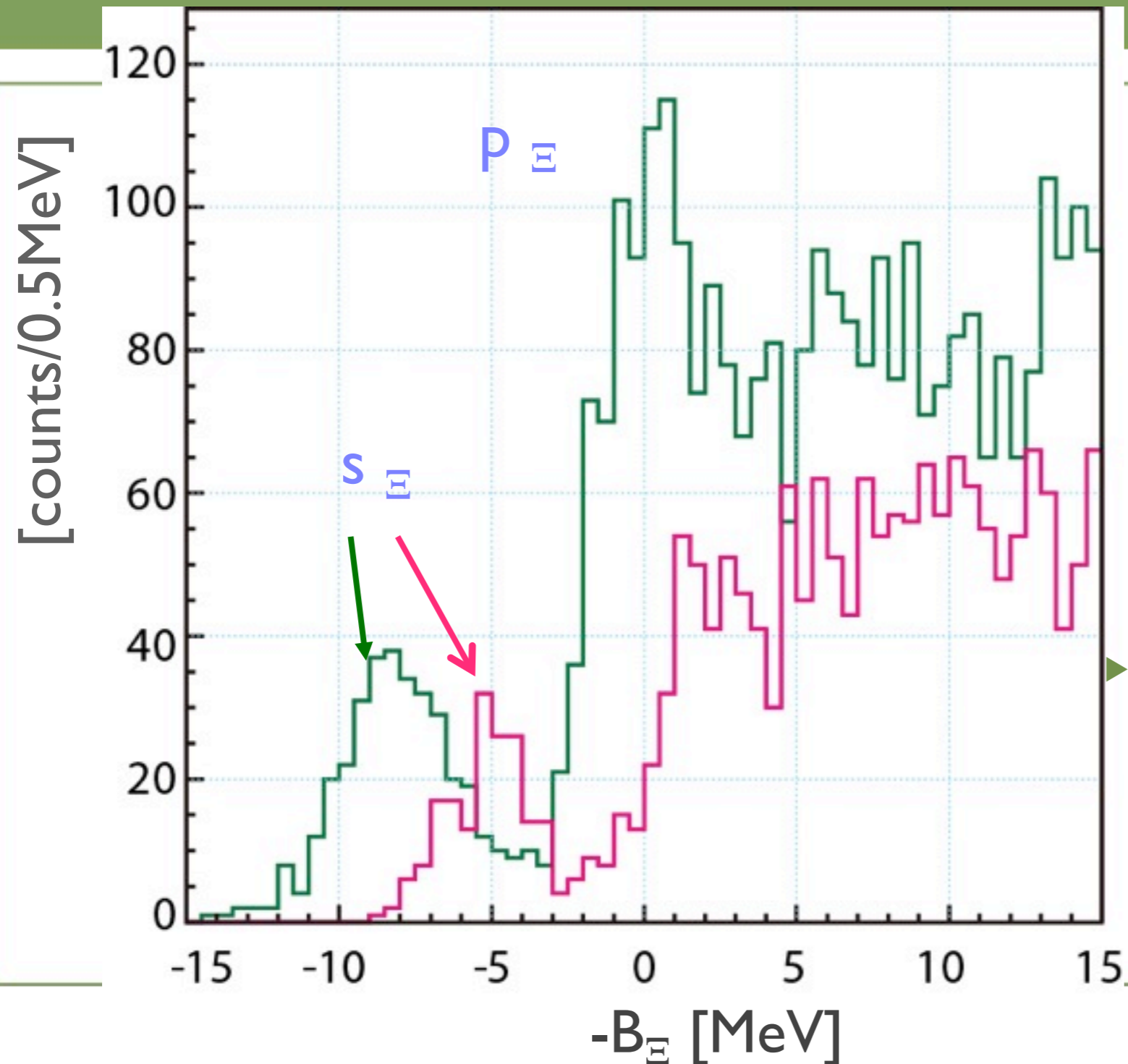
SKS+ Spectrometer



- ▶ 95° total bend
- ▶ ~7m flight path
- ▶ $\Delta x = 0.3$ mm (RMS)



Expected $^{12}_{\text{E}}\text{Be}$ Spectrum



$\Delta E_{\text{meas.}} < 3 \text{ MeV}_{\text{FWHM}}$

$V_{\text{E}} = -20 \text{ MeV}$

$V_{\text{E}} = -14 \text{ MeV}$

Precision:

- ▶ Peak Position: 0.1 - 0.3 MeV
- ▶ Width: 0.2 - 1 MeV

Summary

- ▶ J-PARC Construction: 2001 ~ 2009
 - ▶ Beam commissioning: LINAC(Oct., 06), RCS (Sep., 07), MR(May, 08)
 - ▶ Beam from MR: Jan., 09
- ▶ Day-I Experiments in preparation
 - ▶ Ξ hypernuclei
 - ▶ Deeply-bound Kaonic nuclei
 - ▶ Hypernuclear gamma-ray spectroscopy
 - ▶ etc.