

# The Spin Dependent Structure Function of Nucleon in the Meson Cloud Model

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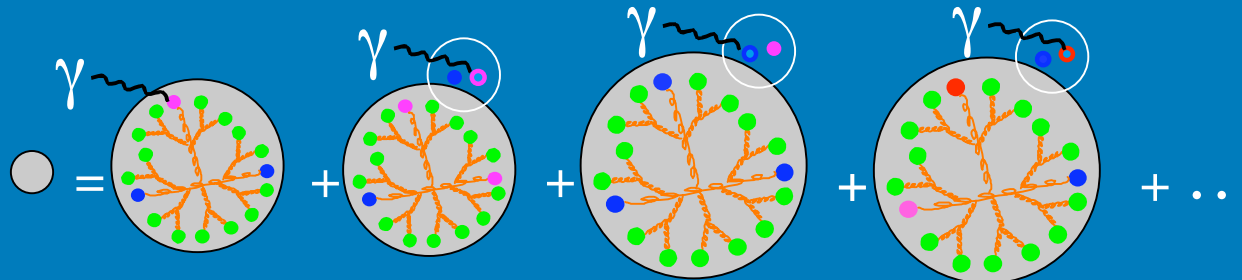
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*New Zealand*

# Overview

- Meson cloud model
- Meson cloud contributions to spin structure functions
- Conclusion

# Meson Cloud Model

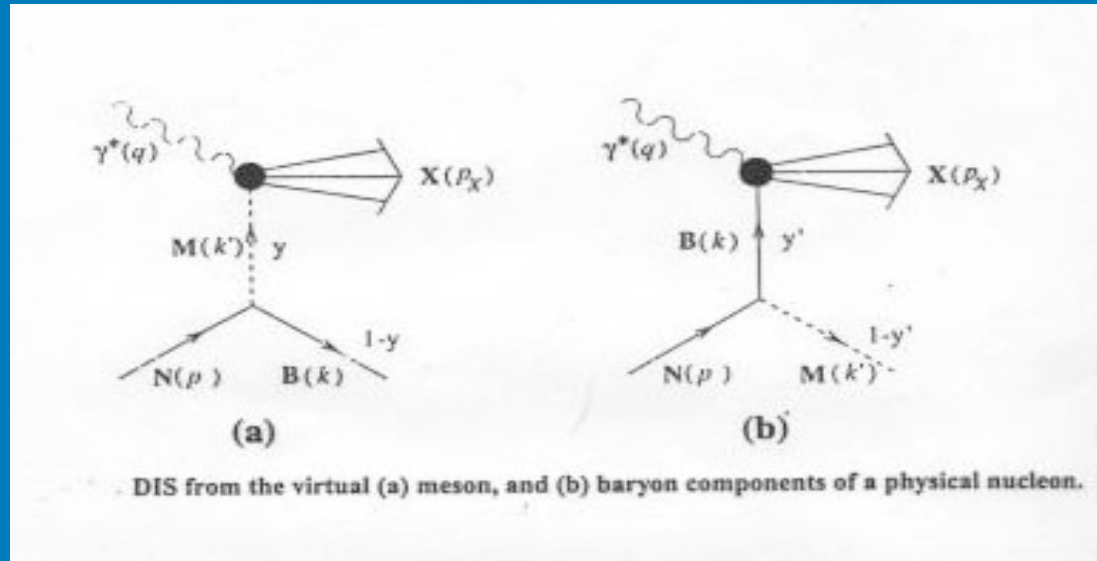


- Fock expansion of proton wavefunction.

$$|p\rangle_{\text{phys}} = \sqrt{Z}|p\rangle_{\text{bare}} + \sum_{BM} \int dy dk_{\perp}^2 \phi_{BM}(y, k_{\perp}^2) |B; M\rangle$$

- Bare states are SU(6) symmetric
- $p \rightarrow BM$  vertices described by  $L_{int}$  plus form factor
- FF constrained by elastic cross-sec
- Quick convergence  $\Leftrightarrow$  Small prob. of high mass states
- Model incorporates structure + interactions
- Can investigate high-energy  $\Leftrightarrow$  low-energy pictures, symmetry breaking etc.

# Meson Cloud Model



Crucial observation (Sullivan 72) -  
 Pion cloud contribution to DIS scales  
 Implies quark dists of proton modified

Convolution

$$\delta q^p(x) = \int_x^1 \frac{dy}{y} f_{p\pi}(y) q^\pi\left(\frac{x}{y}\right)$$

- Observed PDF:  $q_{phys} = q_{bare} + \delta q^{B(M)}$

# Flavour asymmetry in the unpolarized nucleon sea

- Gottfried sum rule 
$$S_G = \int_0^1 \left( F_2^p - F_2^n \right) / x dx$$
$$= \frac{1}{3} \int_0^1 [u_v(x) - d_v(x)] dx + \frac{2}{3} \int_0^1 [\bar{u}(x) - \bar{d}(x)] dx$$
- Experimental studies

→ NMC (DIS, CERN, 1991)  $S_G = 0.235 \pm 0.026$  ( $Q^2 = 4 \text{ GeV}^2$ )

→ NA51 (DY, CERN, 1994)  $\bar{d}/\bar{u} = 1.96 \pm 0.15 \pm 0.19$  at  $\langle x \rangle = 0.18$

→ HERMES (SIDIS, DESY, 1998)

$$(\bar{d} - \bar{u}) / (u - d), 0.02 < x < 0.3, \langle Q^2 \rangle = 2.3 \text{ GeV}^2$$

→ E866 (DY, Fermilab, 1998&2001)

$$\bar{d}/\bar{u}, 0.015 < x < 0.35, \langle Q^2 \rangle = 54 \text{ GeV}^2$$

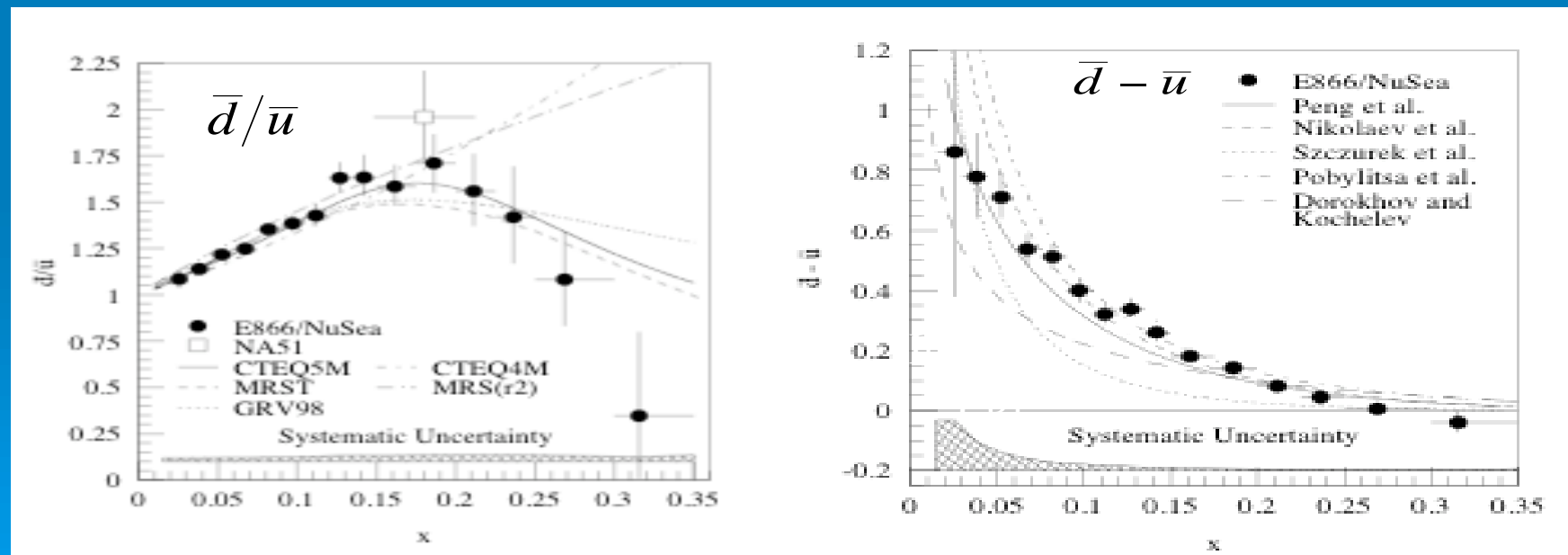
# Flavour asymmetry in the unpolarized nucleon sea

- Isospin broken in sea

$$p \rightarrow n(udd) + \pi^+(u\bar{d})$$

$$p \rightarrow \Delta^{++}(uuu) + \pi^-(d\bar{u})$$

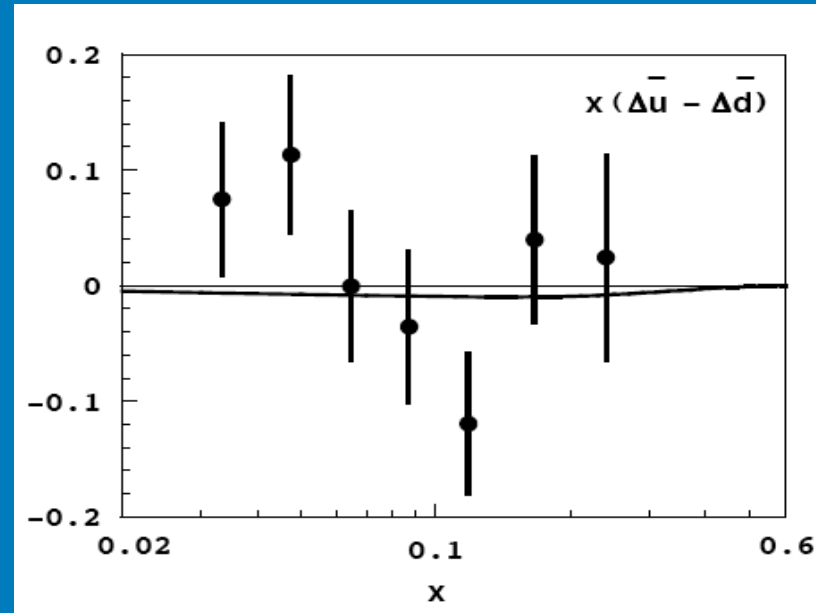
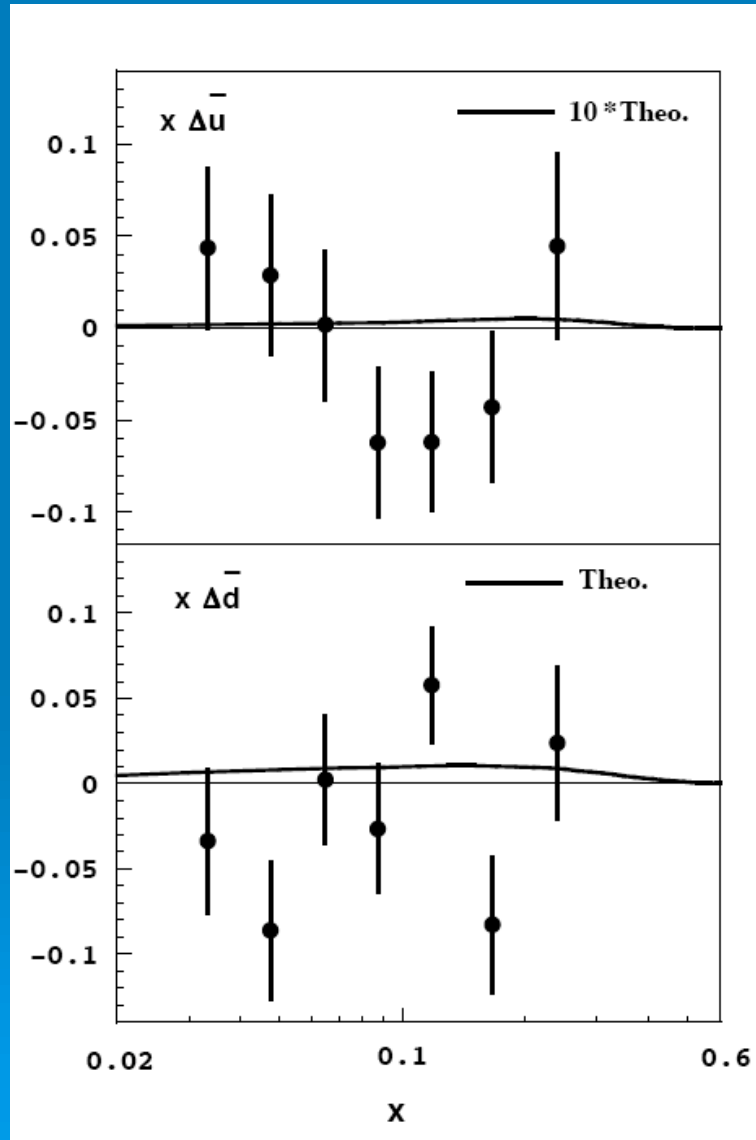
- MCM gives good fit to  $\bar{d}(x) - \bar{u}(x)$



# Spin dependent Quark Dists.

- Extend MCM to include vector mesons
  - $\pi$  cloud dilutes proton spin
  - $\rho, \omega, K^*$  able to carry spin
- Interference terms ?
- Get reasonably good agreement with HERMES semi-inclusive data for sea distributions

# Spin Dependent Sea Dists.



- Data from Hermes
- Small symmetry breaking



# Spin Dependent Structure Functions

- Dominated by valence distributions
  - $N \rightarrow N\pi, N \rightarrow \Delta\pi$  most important fluctuations

$$\mathcal{L}_{int} = ig_{NN\pi} \bar{\psi} \gamma_5 \pi \psi, f_{N\Delta\pi} \bar{\psi} \pi \partial_\mu \chi^\mu + \text{h.c.}$$

- At finite  $Q^2$  spin of cloud hadrons are not parallel with initial nucleon spin
- Both longitudinal and transverse spin components of cloud contribute to observed structure functions

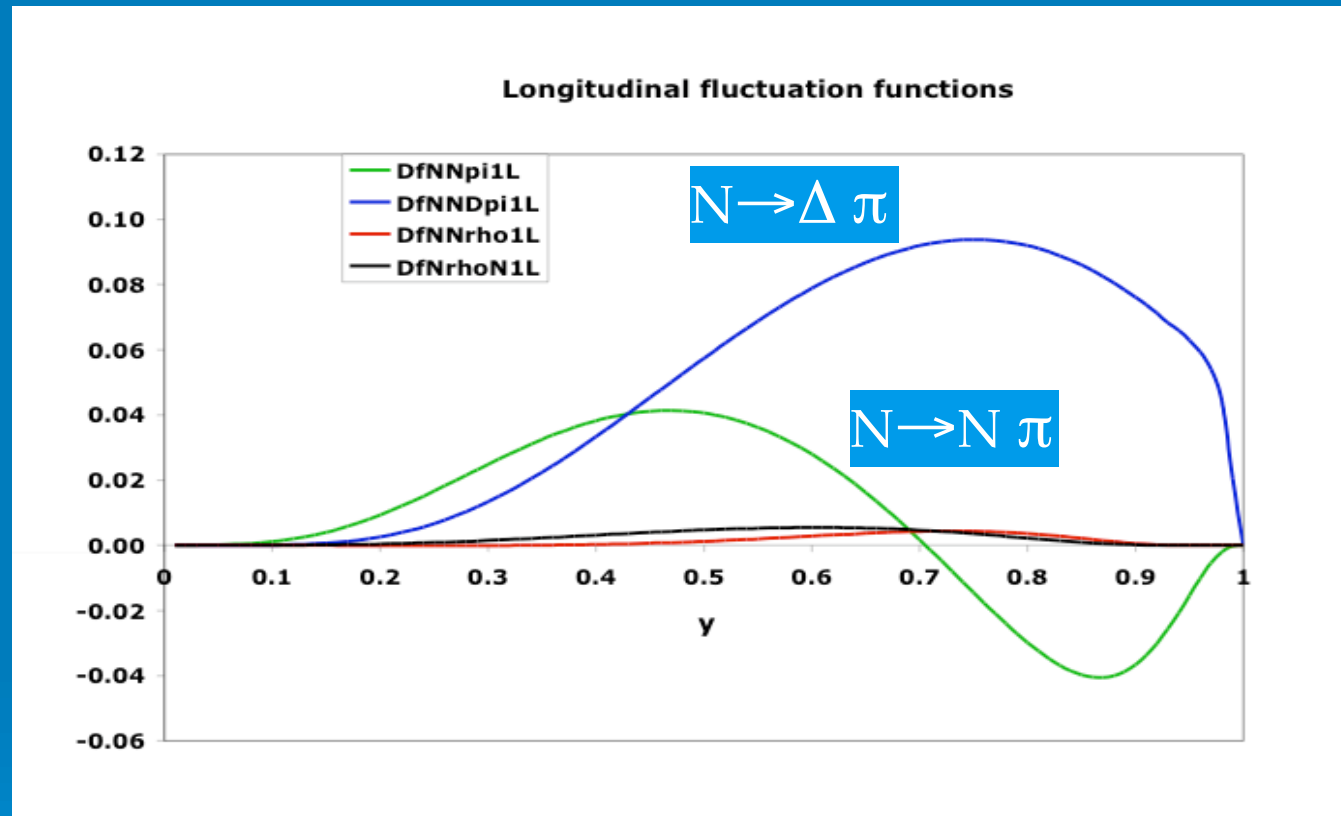
# Spin Dependent Structure Functions

$$\delta g_1(x, Q^2) = \frac{1}{1 + \gamma^2} \int_x^1 \frac{dy}{y} \left( [\Delta f_{1L}(y) + \Delta f_{1T}(y)] g_1^B\left(\frac{x}{y}, Q^2\right) + [\Delta f_{2L}(y) + \Delta f_{2T}(y)] g_2^B\left(\frac{x}{y}, Q^2\right) \right)$$

$$\delta g_2(x, Q^2) = -\frac{1}{1 + \gamma^2} \int_x^1 \frac{dy}{y} \left( [\Delta f_{1L}(y) - \Delta f_{1T}(y)/\gamma^2] g_1^B\left(\frac{x}{y}, Q^2\right) - [\Delta f_{2L}(y) - \Delta f_{2T}(y)/\gamma^2] g_2^B\left(\frac{x}{y}, Q^2\right) \right)$$

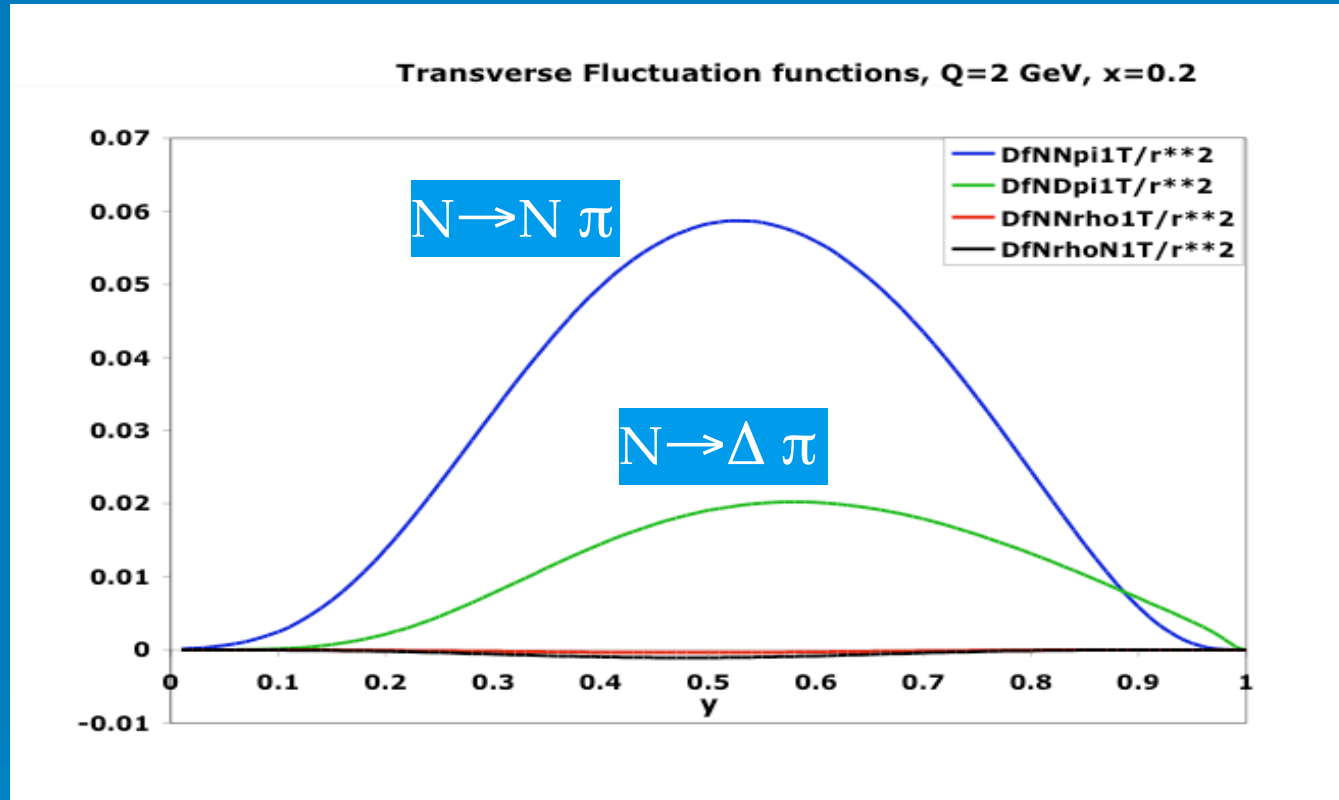
$$\gamma^2 = \frac{4x^2 m_N^2}{Q^2}$$

# Spin Dependent Fluctuations



- Long. fluctuations require both N and  $\Delta$ 
  - $s = 3/2$  state important

# Spin Dependent Fluctuations



- $N$  is more important for transverse fluct.
- n.b  $\gamma \approx 0.19$

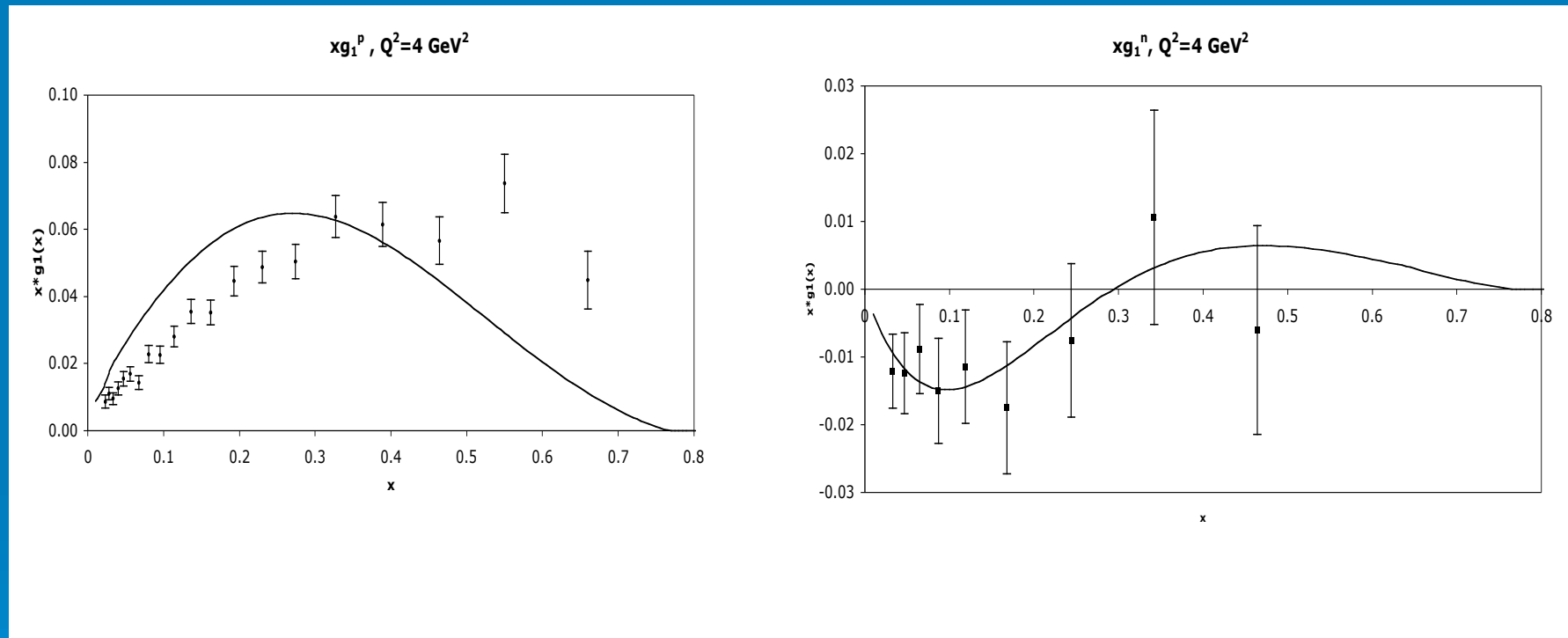
# 'Bare' Hadron SFs

- Use bag model for N,  $\Delta$  parton dists
  - Add  $\Delta g(x)$  'by hand'
  - Hyperfine splitting between N and  $\Delta$
  - Use NLO evolution
  - Unpol. dists agree with DIS data
- $g_2(x)$  from Wandzura-Wilczek

$$g_2^{WW}(x) = -g_1(x) + \int_x^1 \frac{dy}{y} g_1(y)$$

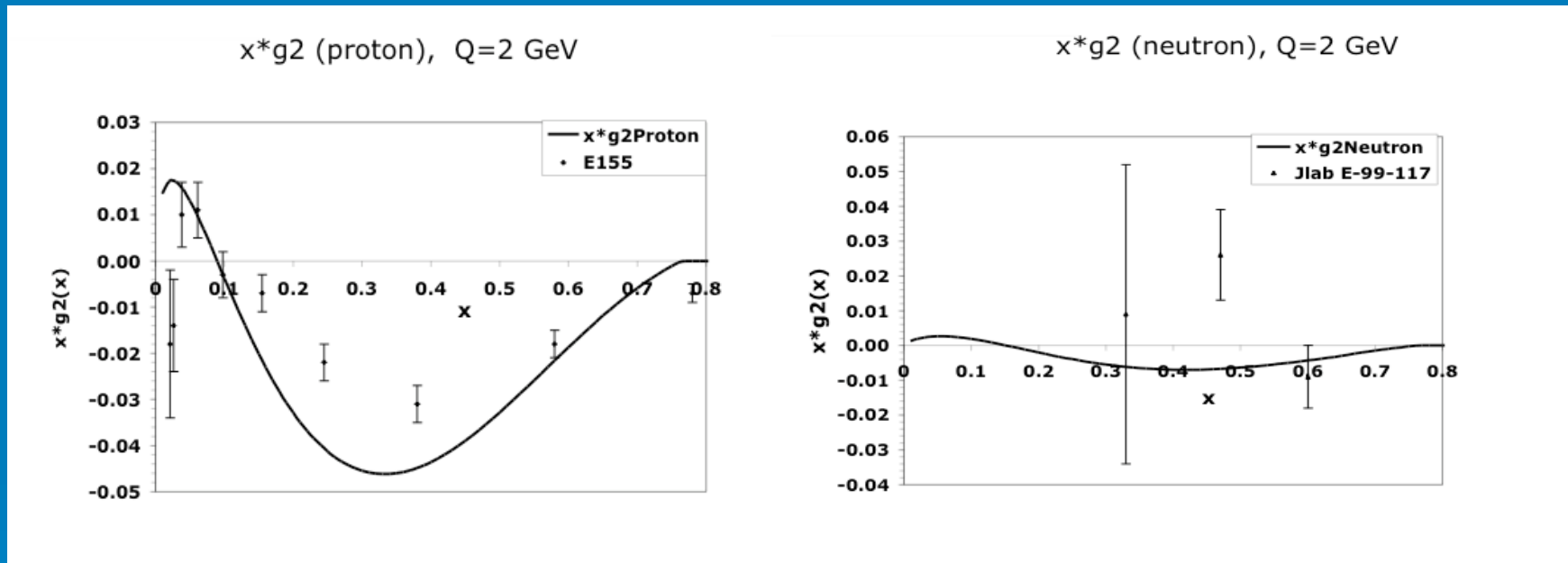
- No higher twist component

# 'Bare' Nucleon $g_1(x)$



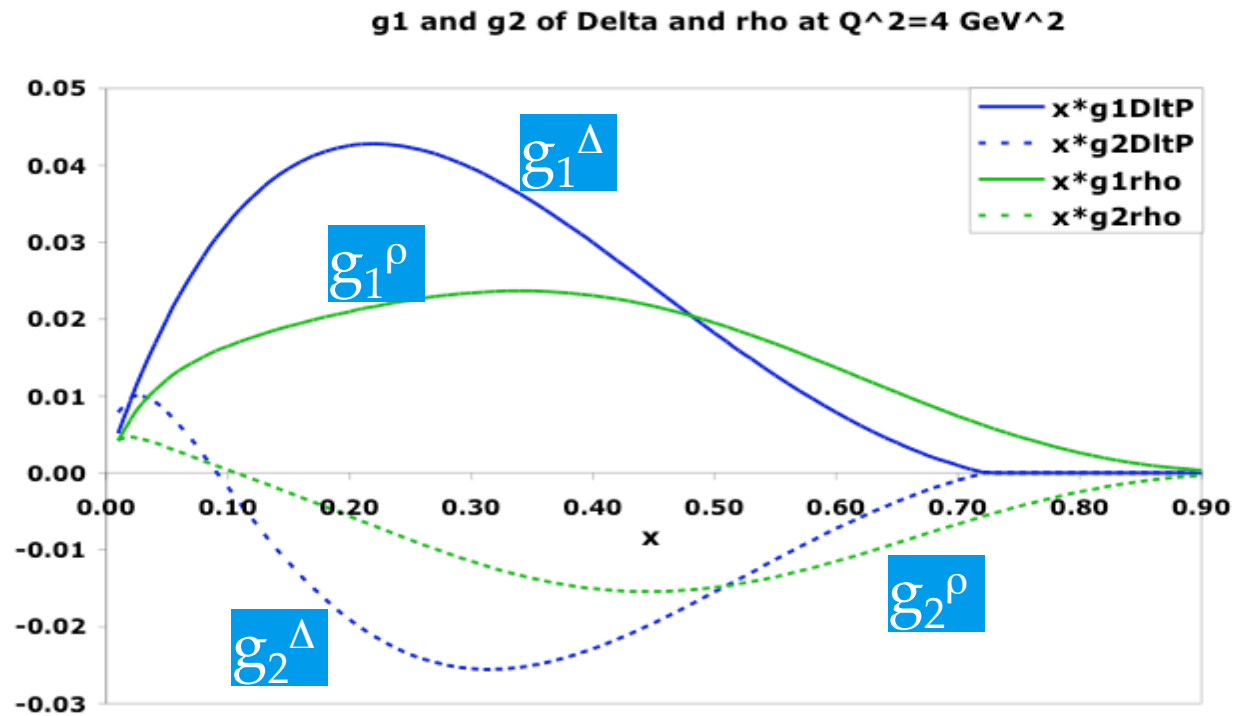
- Data from Hermes

# 'Bare' Nucleon $g_2(x)$



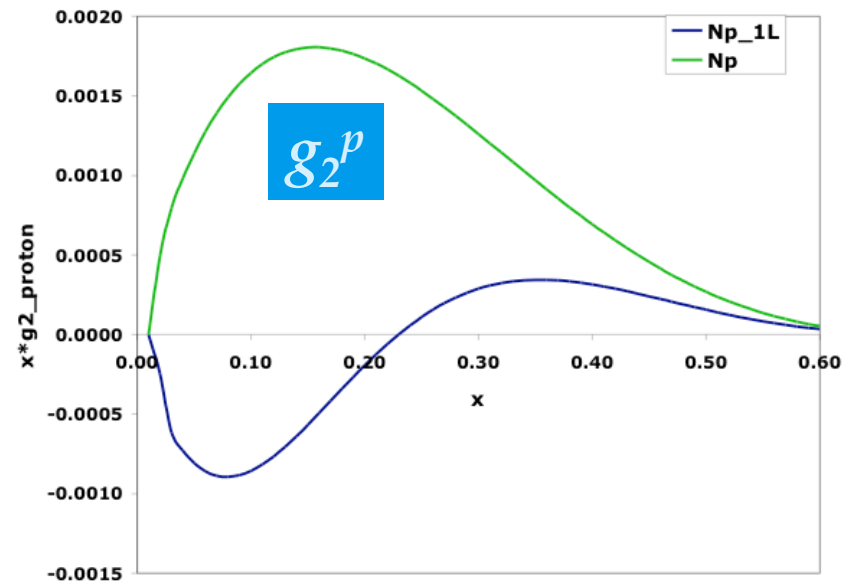
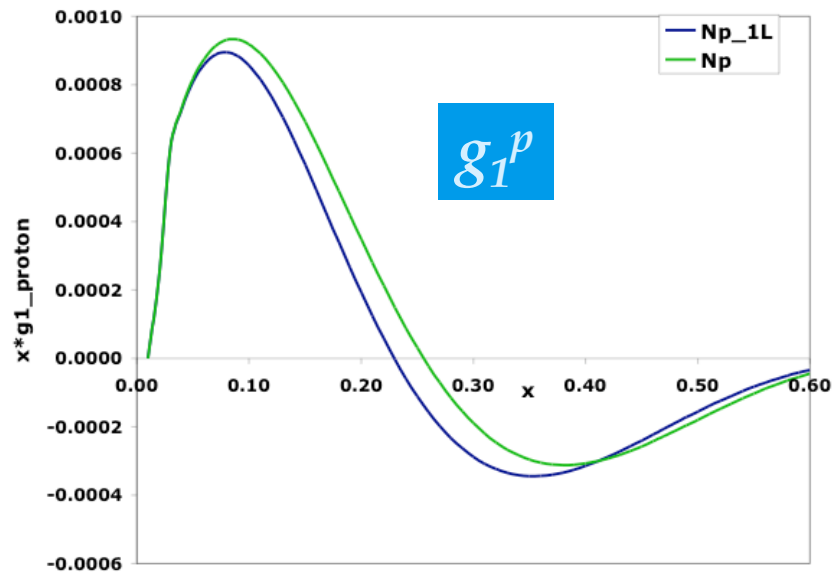
- Data from E155, Jlab E-99-117

# 'Bare' Hadrons $\Delta$ and $\rho$ , $g_1(x)$ and $g_2(x)$



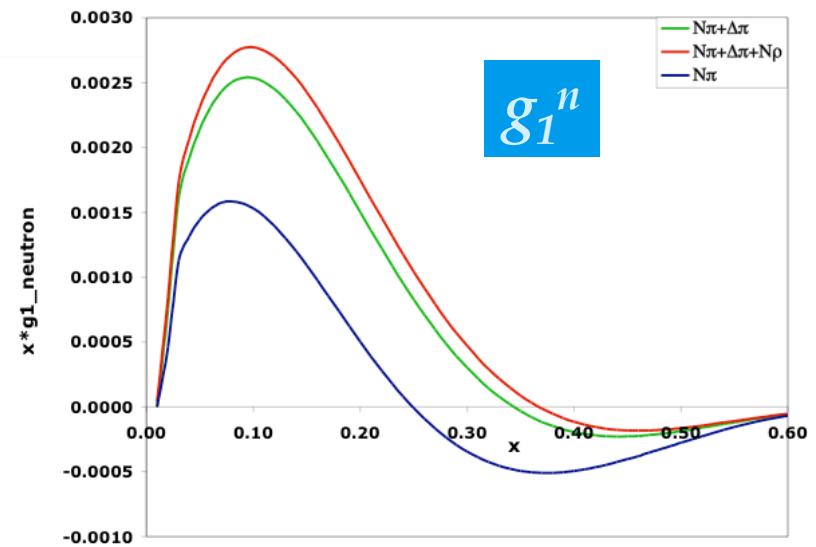
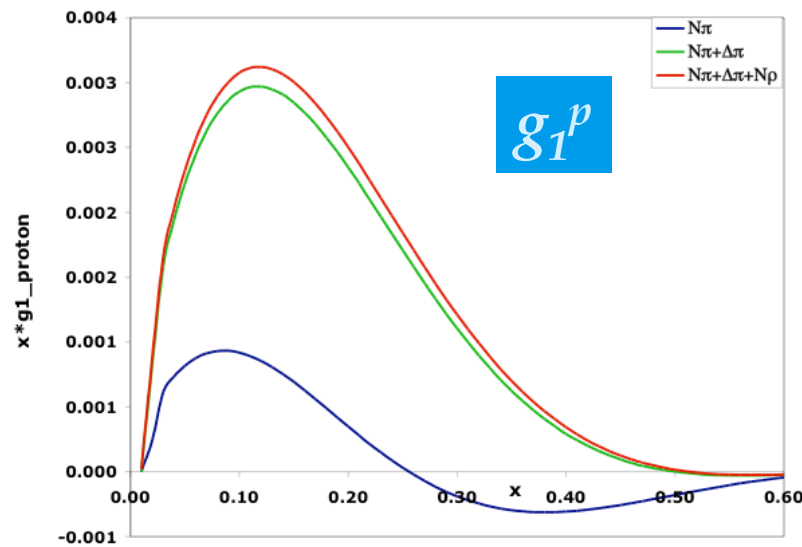


# MC Contributions to $g_1^p$ and $g_2^p$



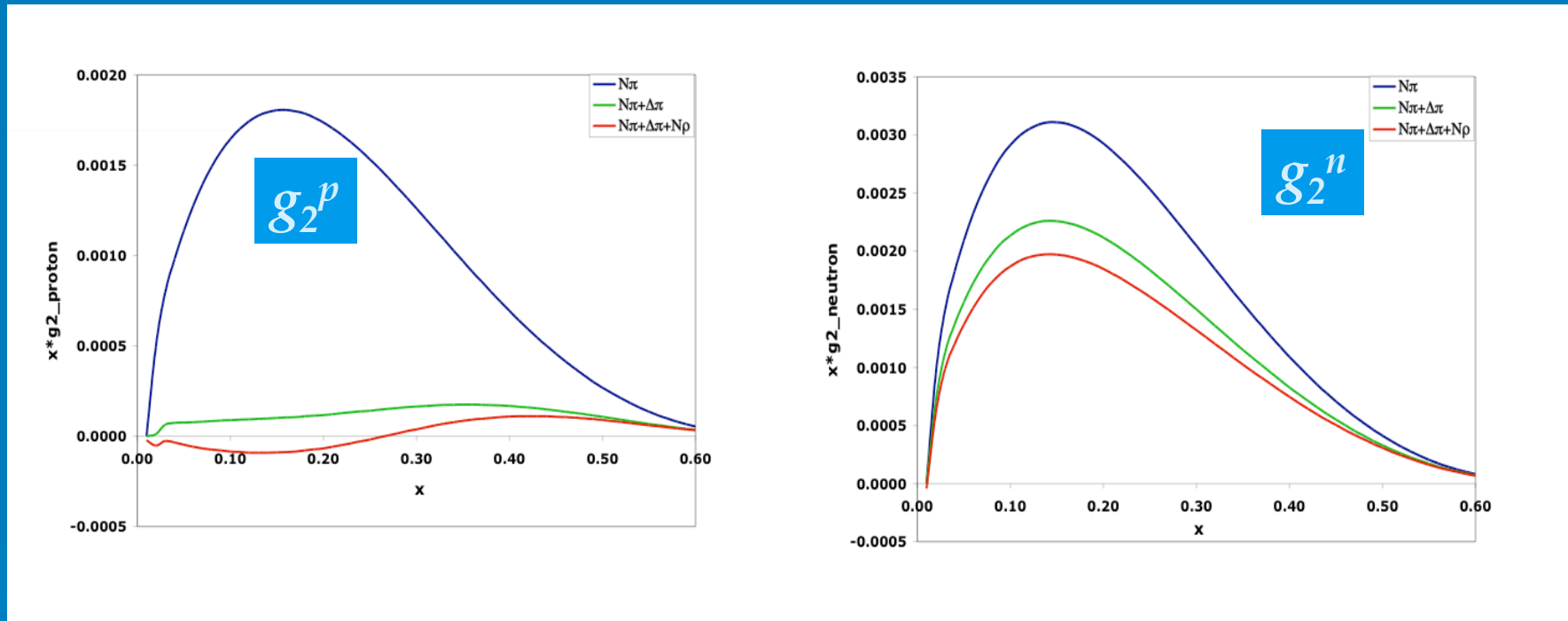
- The results for the neutron are very similar
- $\Delta f_{1T}, \Delta f_{2L}, \Delta f_{2T}$  are important to  $g_2^p$  and  $g_2^n$

# MC Contributions to $g_1^p$ and $g_1^n$



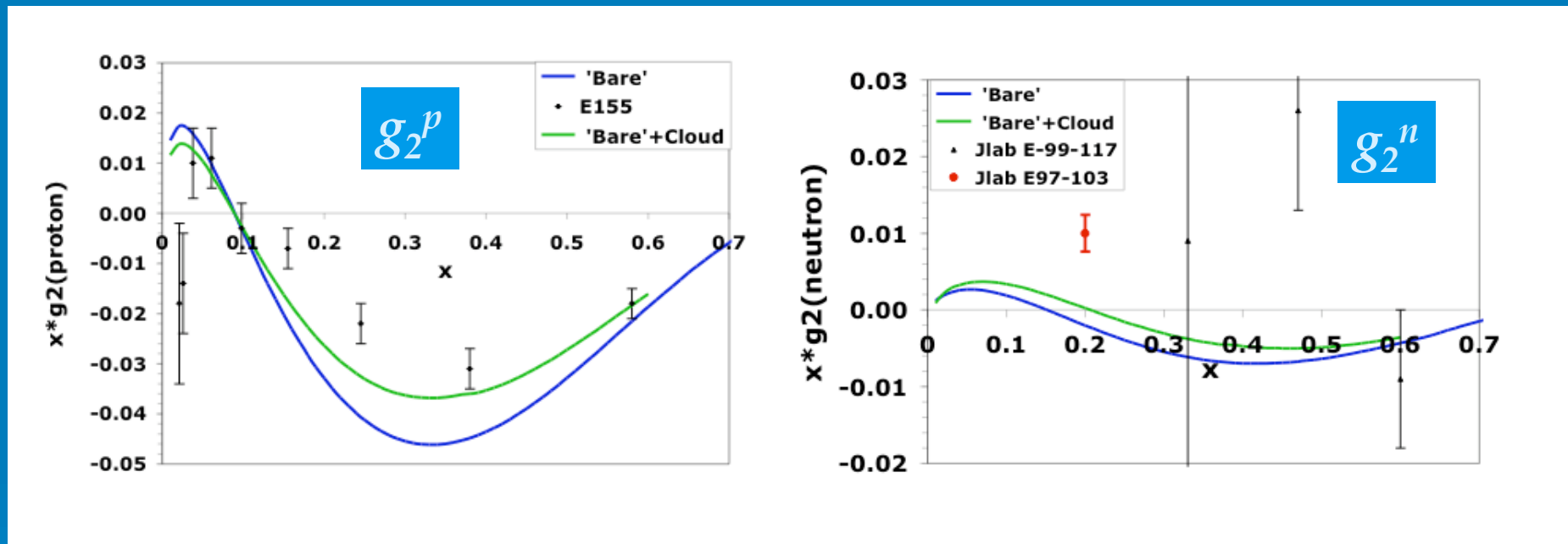
- $\Delta\pi$  is important while  $N\rho$  is not
- $\Delta\pi$  increases  $g_1^p$  more than that for  $g_1^n$

# MC Contributions to $g_2^p$ and $g_2^n$



- $\Delta\pi$  is important
- $\Delta\pi$  affects  $g_2^p$  more than that for  $g_2^n$

# Comparison with data: $g_2^p$ and $g_2^n$



- 20~30% corrections from MC
- Improve the agreement with the experiment

# Summary

- Longitudinal ( $g_1$ ) structure ftns of cloud hadrons affect observed transverse ( $g_2$ ) structure ftns
- MC contributions to  $g_1$  are small
- MC contributions to  $g_2$  are 20%
  - Similar size to higher twist in  $g_2^n$
  - Theorists have to be careful!

# Thanks

- Tony Signal (Massey)
- François Bissey (Massey)